

2004

MC<sup>2</sup>-2

**Improvement of The Fuel Assmebly Heterogeneity Analysis Model of MC<sup>2</sup>-2 Code  
Using an Analytic Method of Resonance Escape Cross Sections**

150

가 MC<sup>2</sup>-2  
Dancoff Bell  
가 Bell  
annulus  
가 MC<sup>2</sup>-2/ONEDANT  
MCNP  
MC<sup>2</sup>-2

**Abstract**

The MC<sup>2</sup>-2 code models a single fuel rod. The shadowing effect due to the lattice geometry of fuel rods is considered using the Bell factor together with the Dancoff correction to evaluate the heterogeneity of a fuel assembly. This model requires a pre-calculated Bell factor of the considered assembly and is inappropriate in representing the effect of other structural materials in the fuel assembly such as a duct. To overcome this drawback the annular model of the fuel assembly is proposed and an analytic method accounting for resonance escape is applied to the model. To evaluate the validity of the fuel assembly model, a criticality calculation was performed using MC<sup>2</sup>-2/ONEDANT and heterogeneity effect is compared with that of MCNP. The results obtained show that the improved MC<sup>2</sup>-2 herein can represent the heterogeneity of a fuel assembly more accurately than the original one.

# 1

가

가

(in-current of resonance neutrons)

가

(shadowing

effect)

Dancoff Ginsburg [1].

Dancoff

(effective surface)

$$S_{eff} = (1 - C)S \quad (1)$$

,  $S_{eff}$ ,  $S$ ,  $C$  Dancoff correction

$$\text{Dancoff factor } D = 1 - C$$

가

. Dancoff

가

,  $D$

$\cos \theta$  가

가

가

Dancoff factor

, Dancoff factor

. MC<sup>2</sup>-2

Dancoff factor

$$\Sigma_e^* = \Sigma_e \frac{a_1(1-c)}{1+(a-1)C} \quad (2)$$

,  $a_1$ ,  $a_2$  Bell approximation

. MC<sup>2</sup>-2

Bell approximation

Dancoff factor

Bell

approximation

가

MC<sup>2</sup>-2

가

가

annulus

가

blackness

Stoker Weiss

[2].

가

annulus

Stoker Weiss가

annulus

annulus

, MC<sup>2</sup>-2

Bell

approximation

2

annulus

annulus

annulus

. 3 2

annulus

MC<sup>2</sup>-2

MCNP

. 4

2

2.1

annulus

annulus

[5, 6]

가

annulus i

annulus first flight blackness  $\gamma_i(E)$

$$P_{esc}^i(E) = \frac{\gamma_i(E)}{\sum_{ti}(E)L_i} \quad (3)$$

,  $L_i = 4V_i / S_o$  (mean chord length) .  $\Sigma_{ti}(E)$

$i$

blackness                      blackness                      blackness  
 $\rho = r / R, R\Sigma_{tf}$                       blacknes

$$\gamma_i = \gamma(\rho_i, R\Sigma_{tf}) - \gamma(\rho_{i-1}, R\Sigma_{tf}) \quad (4)$$

,  $R$                        $\rho_i = r_i / R$  가

$$L_i = 4V_i / S_o = \frac{4(\pi r_i^2 - \pi r_{i-1}^2)}{2\pi R} = 2R(\rho_i^2 - \rho_{i-1}^2) \quad (5)$$

(3), (4), (5)                      , annulus i

$$P_{esc}^i(E) = \frac{\gamma(\rho_i, R\Sigma_{tf}) - \gamma(\rho_{i-1}, R\Sigma_{tf})}{2R\Sigma_{tf}(\rho_i^2 - \rho_{i-1}^2)} \quad (6)$$

blackness

가

blackness가

가

solid

Carlvik

[4].

$$P_{esc}(x) = \frac{4}{x+2} - \frac{3}{x+3} \quad (7)$$

$x = L\Sigma_{tf}$

solid

1

$\Sigma_{tf} \rightarrow \infty$

blackness 1

$1/(\Sigma_{tf}L)$

가

annulus

$\Sigma_{tf} \rightarrow \infty$

가

annulus

blackness가 1

solid

가

,

annuli

$\Sigma_{tf} \rightarrow \infty$

blackness 0

annuli

$1/(\Sigma_{tf}L)$

0

3

annulus

$1/\Sigma_{tf}$  가 ,  
 가 .  
 annuli  $1/\Sigma_{tf}$  가  
 가 가 Stoker Wiess  
 $1/\Sigma_{tf}$  가  $P_{esc}$   
 $1/\Sigma_{tf}$  가 가 .  
 blackness  $R(x)$  가 .  $x$   
 (mean free path) (average  
 chord length)  $\bar{l}_{\Sigma_{tf}}$  .

$$\rho \quad \text{blackness} \quad \gamma(\rho, R\Sigma_{tf})$$

2 .

Blackness .

$$\gamma(\rho_i, x) = \gamma_{BC}(\rho_i, x) - \gamma_{AB}(\rho_i, x) \quad (8)$$

,  $\gamma_{BC}$   $\gamma_{AB}$  2 “OBC” “OAB”

blackness .  $\gamma_{\alpha} (\alpha = AB, BC)$  .

$$\gamma_{\alpha} \approx X(1 - e^{-\bar{l}_{\alpha}\Sigma_{tf}}) \quad (9)$$

$X$  가 “OAB” “OBC”  
 $\rho$   $X(\rho) = \rho$  .  $l_{\alpha}$   $O$   
 $\alpha$  .

$$\bar{l}_{\alpha}(\rho) = \frac{2R}{\pi} \left( \sqrt{1 - \rho^2} + \frac{1}{\rho} \sin^{-1} \pm \frac{\pi}{2} \rho \right) \quad (10)$$

“+”  $\alpha = BC$  “-“  $\alpha = AB$  .

Blackness  $\gamma_{\alpha}$   $1 - e^{-x}$   $x/(1+x)$   
 ,  $\gamma(\rho, x)$  2 . Blackness

$$\gamma(\rho, x) \approx X(\rho)R(x) \quad (11)$$

$$R(x) = x \sum_n^{N_R} a_n \frac{b_n}{x + b_n} \quad (12)$$

$$x \rightarrow \infty \quad a_n \quad b_n \quad x \rightarrow 0 \quad R(x)/x \cong P_{esc}(x) \rightarrow 1$$

$$\sum_n a_n = 1 \quad \sum_n a_n b_n = 1 \quad (13)$$

$x$  가

$$R(x \rightarrow \infty) = 1 - \frac{1}{x} \sum a_n b_n^2 \quad (14)$$

$$(8) \quad (14) \quad \Sigma_{if} \rightarrow \infty \quad \gamma(\rho, R\Sigma_{if}) \quad (1/\bar{l}_{AB} - 1/\bar{l}_{BC})/\Sigma_{if}$$

$$P_{esc}^i \quad 2 \quad 0 \quad \text{annulus}$$

2 가

2

$$(6) \quad (8) \quad (12) \quad \text{annulus } i$$

$$P_{esc}^i(E) = \frac{1}{\Sigma_{i,i}(E)L_i} \left\{ \rho_i [R(x_{BC}^i) - R(x_{AB}^i)] - \rho_{i-1} [R(x_{BC}^{i-1}) - R(x_{AB}^{i-1})] \right\} \quad (15)$$

$$3 \quad (15) \quad 5 \quad \text{annulus} \quad \text{blackness}$$

$$4 \quad \text{solid}$$

5

## 2.2

annulus ,  $i$  가

$$j \quad (11) \quad \text{blackness} \quad (15) \quad ,$$

(16)

$$P_{esc}^{ij} = \frac{\gamma(\rho_{ij-1}, x_{ij-1}) - \gamma(\rho_{i-1j-1}, x_{i-1j-1})}{2r_{j-1} \sum_{tf,i} (\rho_{ij-1}^2 - \rho_{i-1j-1}^2)} - \frac{\gamma(\rho_{ij}, x_{ij}) - \gamma(\rho_{i-1j}, x_{i-1j})}{2r_j \sum_{tf,i} (\rho_{ij}^2 - \rho_{i-1j}^2)} \quad (16)$$

(19)

$$P_{esc}^{ij} = \frac{1}{\sum_{tf,i} (E) L_{ij-1}} \left\{ \rho_{ij-1} [R(x_{BC}^{ij-1}) - R(x_{AB}^{ij-1})] - \rho_{i-1j-1} [R(x_{BC}^{i-1j-1}) - R(x_{AB}^{i-1j-1})] \right\} - \frac{1}{\sum_{tf,i} (E) L_{ij}} \left\{ \rho_{ij} [R(x_{BC}^{ij}) - R(x_{AB}^{ij})] - \rho_{i-1j} [R(x_{BC}^{i-1j}) - R(x_{AB}^{i-1j})] \right\} \quad (17)$$

$$L_{ij} = 2r_j (\rho_{ij}^2 - \rho_{i-1j}^2), \quad \rho_{ij} = r_i / r_j$$

가  
 2  
 6  
 1 3 , 2  
 4 1 0.447 2  
 1 3 Δr 가 2 4  
 0.5 cm<sup>-1</sup> 1 1  
 2 (P<sub>12</sub>) 1 4  
 (P<sub>14</sub>) 6 1 3 1  
 black ,  
 1 P<sub>12</sub> 6 2  
 , i i  
 j

3

MCNP [5] MC<sup>2</sup>-2 MC<sup>2</sup>-2  
 KALIMER-150[6] 1  
 (10 annulus) (10 annulus)  
 22 annulus MC<sup>2</sup>-2 80  
 , ONEDANT [7]

$\Delta k$  MCNP  
 2 MCNP  $\Delta k$  0.00290  
 annulus MCNP  $\Delta k$  0.00385 MC<sup>2</sup>-2  
 Bell approximation 1.0 가 가  $\Delta k$  0.00152  
 MC<sup>2</sup>-2가 MCNP  $\Delta k$  가 MC<sup>2</sup>-2  $\Delta k$  가 0.00207

4

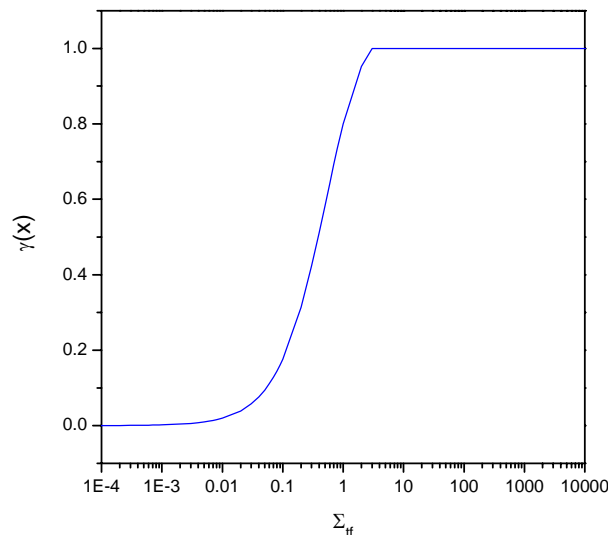
가 MC<sup>2</sup>-2  
 Dancoff Bell 가  
 Bell  
 가 annulus  
 , Stoker Weiss가 annulus  
 annulus MC<sup>2</sup>-2  
 MC<sup>2</sup>-2/ONEDANT MCNP KALIMER-150  
 $\Delta k$  , MC<sup>2</sup>-2  
 $\Delta k$  가 가  
 annulus 가 가

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- [2] H. Henryson II, B. J. Toppel, and C. G. Stenberg, "MC<sup>2</sup>-2 Code System for Calculating Fast Neutron Spectra and Multigroup Cross-Section," PSR-350 MC2-



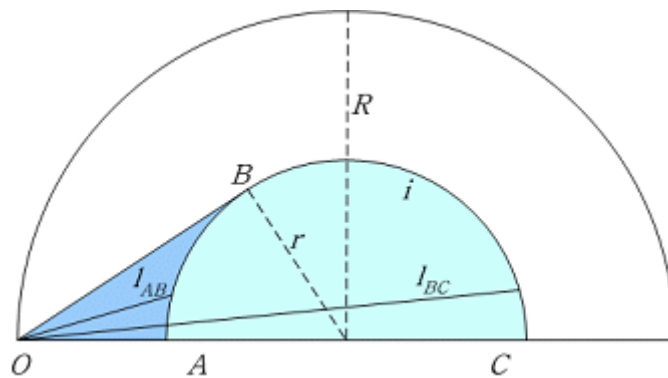
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- [4] R.J.J. Stamm'ler and M.J. Abbate, "Methods of Steady-state Reactor Physics in Nuclear Design," Academic Press New York, ISBN 0-12663320-7, 1983.
- [5] J. F. Briesmeister, et al., "MCNP4C2 - A General Monte Carlo N-Particle Transport Code, Version 4C," LA-13709-M, 2000.
- [6] , , , "Nuclear and Thermal-Hydraulic Design and Analysis of KALIMER Breakeven Equilibrium Core," LMR/CD112-ER-01, KAERI, 2000.
- [7] R. E. Alcouffe, et al., "DANTSYS: A Diffusion Accelerated Neutral Particle Transport Code System," LA-12969-M, LANL, 1995.

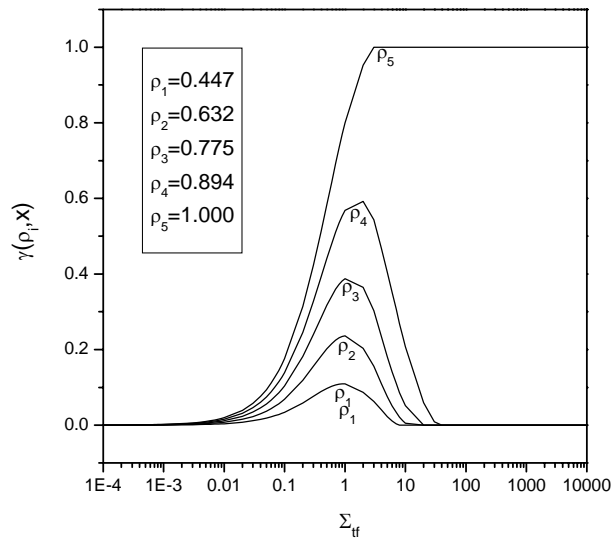


1 Solid

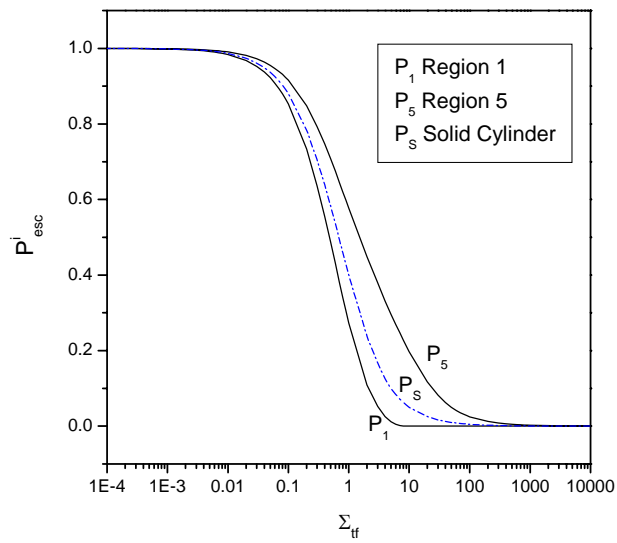
blackness



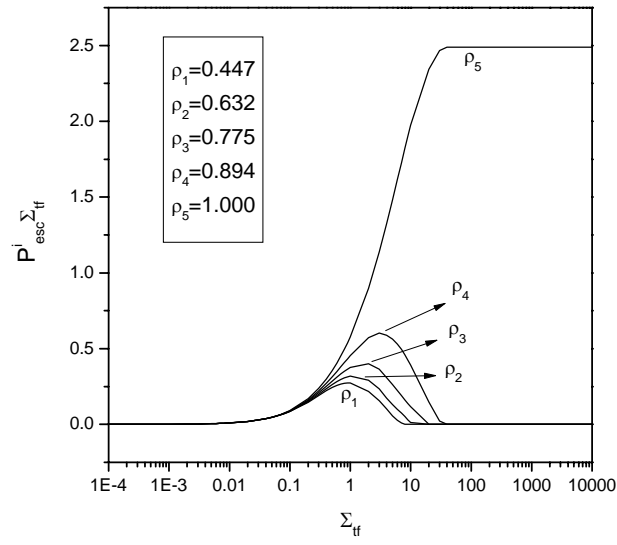
2 Half cylinder



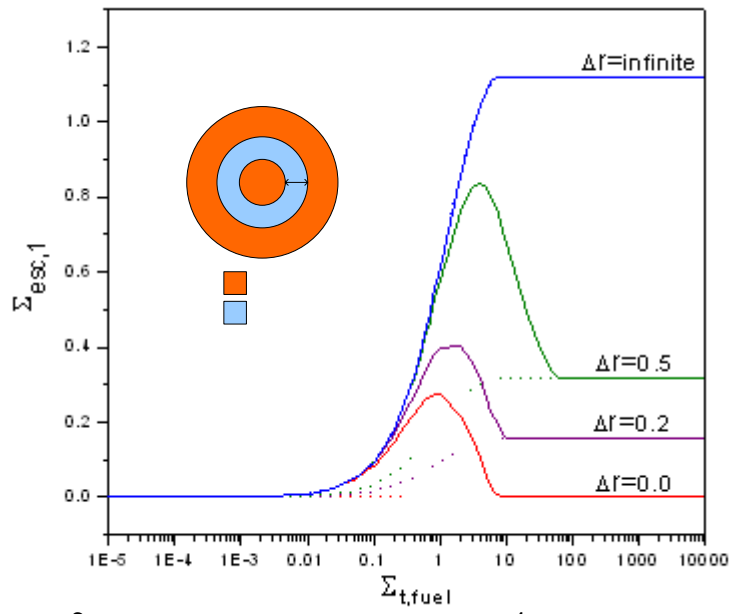
3 annulus blackness  $\gamma(\rho, x)$



4 annulus



5 annulus



6

1

## 1 KALIMER

<u>ASSEMBLY DATA</u>	
Number of Pins per Assembly	271
Fuel smeared density (%)	75.0%
Duct Material	HT9
Duct Wall Thickness (cm)	0.37
Duct Outer Flat to Flat (cm)	15.7
Duct Inner Flat to Flat (cm)	14.96
Active Length (cm)	100.00
Fuel Element Length (cm)	346.68
Gap Distance between Ducts (cm)	0.40
Assembly Lattice Pitch (cm)	16.10
Assembly Area (cm <sup>2</sup> )	224.482
<u>PIN DATA</u>	
Fuel Type	U-Pu-10%Zr
Fuel Fabrication Density (%TD)	100.0
Cladding Material	HT9
Pin Overall Length (cm)	346.8
Pin Outer Diameter (cm)	0.74
Pin Inner Diameter (cm)	0.63
Cladding Thickness (cm)	0.055
Fuel Slug Diameter (cm)	0.546
Fuel Cladding Gap (cm)	0.042
Pin Pitch (cm)	0.89
Pin P/D Ration	1.203
Wire Wrap Diameter (cm)	0.14
Wire Wrap Pitch (cm)	20.49
Bond	Na

## 2

	MCNP (Real )	MCNP (Annulus )	MC <sup>2</sup> -2 <sup>†</sup> / ONEDANT ( )	MC <sup>2</sup> -2/ ONEDANT ( )
	1.72184, 0.00048	1.72279, 0.00054	1.71186	1.71241
	1.71894, 0.00058	1.71894, 0.00058	1.71034	1.71034
k	0.00290	0.00385	0.00152	0.00207

†Bell factor = 1.0