

MCCARD

Development and Verification of MCCARD Gamma-Ray Transport Routine

56-1

MCCARD(Monte Carlo Code for Advanced Reactor Design) , 가 가 .
 MCCARD ,
 SMART 2
 MCNP ,
 가 .

Abstract

MCCARD, which is an abbreviation of Monte Carlo Code for Advanced Reactor Design, is developed at SNU and is designed exclusively for the neutron transport calculation. The MCCARD is capable of depletion analysis and taking into account the temperature feedback effect. Till now, the code does not have the ability of simulating gamma-ray transport behavior. In this study, however, a calculation module for the gamma-ray transport is designed and a capability of estimating gamma-ray contribution to the nuclear characteristics of a given system is added into MCCARD. For verifications of the gamma-ray transport module, benchmark calculations are performed through the SMART 2D pin cell and fuel assembly problems. They are compared with these of MCNP and it is demonstrated that two results agree with each other within the statistical deviations of the Monte Carlo calculations.

1.

3 (transport equation)

MCCARD(Monte Carlo Calculations for Advanced Reactor Design)[1]

(pointwise energy cross-section library)

MCCARD

MCCARD

MCNP[2] SMART 2

2.

MCCARD

(Gamma Bank)

2.1 가

[4]

$$W_r = W_n \frac{\sigma_r}{\sigma_T}$$

- , W_r = gamma weight
- W_n = neutron weight
- σ_r = gamma production cross section
- σ_T = total neutron cross section

가 가 가 (W^{min}) (splitting)

, 가 (Russian roulette)
 가 .

2.2

MCCARD

가

$$\sum_{i=1}^{n-1} \sigma_i < \xi \sum_{i=1}^N \sigma_i \leq \sum_{i=1}^n \sigma_i$$

, ξ = random number on the interval (0,1)

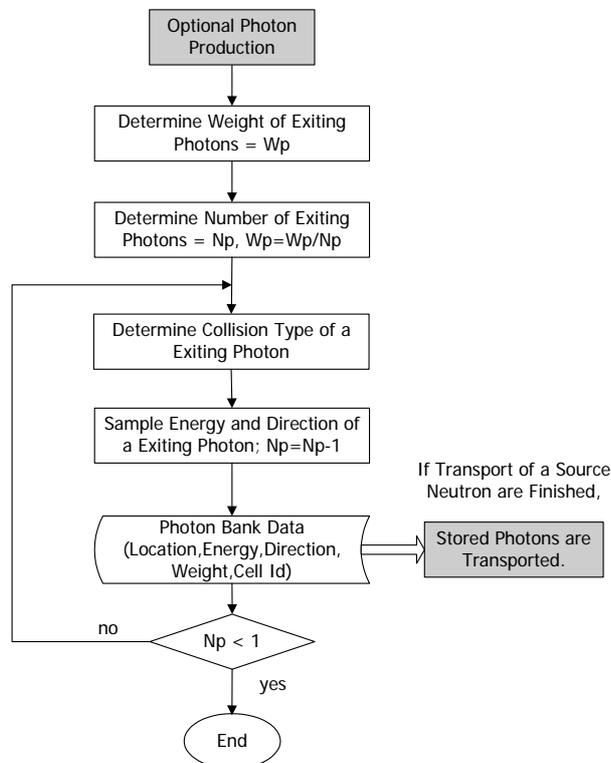
N = number of gamma production reactions

σ_i = gamma production cross section for reaction i

2.3

가 ,

32 (equiprobable cosine bins) ,
 ENDF/B (tabulated spectra)
 (discrete line)
 1 MCCARD



1. Flowchart of Optional Photon Production

3.

가

$$\sum_{j=1}^{t-1} [\sigma_k^j(E)] < \xi \sigma_k^{tot}(E) \leq \sum_{j=1}^t [\sigma_k^j(E)]$$

, $\xi = \text{random number on } [0,1)$

$$\sigma_k^{tot}(E) = \sigma_k^{in}(E) + \sigma_k^{co}(E) + \sigma_k^{pe}(E) + \sigma_k^{pp}(E)$$

3.1 (Incoherent Scattering)

Klein - Nishina

(incoherent

scattering factor)

Klein -

Nishina

$$\sigma^i(Z, \alpha, \mu) d\mu = I(Z, \nu) K(\alpha, \mu) d\mu$$

$$, K(\alpha, \mu) d\mu = \pi r_0^2 \left(\frac{\alpha'}{\alpha} \right)^2 \left(\frac{\alpha'}{\alpha} + \frac{\alpha}{\alpha'} + \mu^2 - 1 \right) d\mu$$

$$\alpha' = \frac{\alpha}{1 + \alpha(1 - \mu)}, \quad \mu = \cos\theta$$

$$I(Z, \nu) = \text{Incoherent scattering factor}, \quad \nu = \kappa \alpha \sqrt{1 - \mu}, \quad \kappa = 10^{-8} \text{ cm}$$

Klein - Nishina

[5]

. Klein - Nishina

가 1.5MeV

Kahn's method[6]

1.5MeV

Koblinger's method[7]

3.2 (Coherent Scattering)

Thomson

Thomson

$$\sigma^c(Z, \alpha, \mu) d\mu = C^2(Z, \nu) T(\mu) d\mu$$

$$, T(\mu) d\mu = \pi r_0^2 (1 + \mu^2) d\mu$$

$$C^2(Z, \nu) : \text{Coherent scattering factor}, \quad \nu = \kappa \alpha \sqrt{1 - \mu}, \quad \kappa = 10^{-8} \text{ cm}$$

Thomson

3.3 (Photoelectric Effect)

fluorescent gamma-ray
fluorescent gamma-ray

가 11 가 가 1KeV 가
가 12 30 가
1KeV , 가 31 가
1KeV .[8]

3.4 (Pair Production)

$$1.022MeV \cong 2mc^2[1 + (m/M)]$$

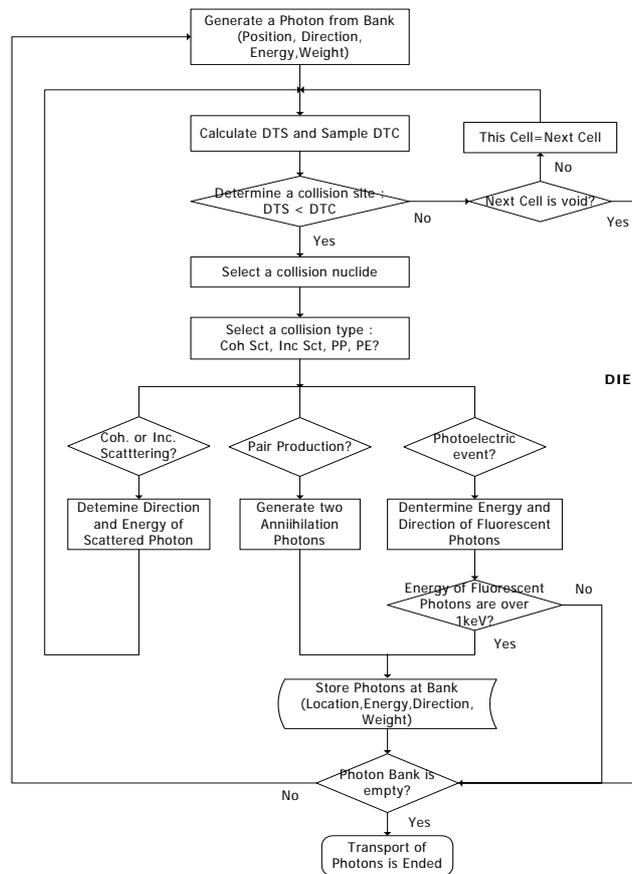
$$(- (= E - 1.022MeV))$$

annihilation

gamma - ray , annihilation gamma - ray
가 0.511MeV

.[3]

2 MCCARD



2. Flowchart of Photon Transport

4.

MCCARD

(track length

estimate of energy deposition)

. [2]

$$F = \rho_a / \rho_m \int_V \int_t \int_E H(E) \Phi(r, E, t) dE dt dV / V$$

, $\rho_a = \text{atom density (atoms / barn - cm)}$

$\rho_m = \text{gram density (grams / cm}^3\text{)}$

$H(E) = \text{heating response (summed over nuclides in a material)}$

MeV/gm , MCCRAD heating response

가

가 .

$$F_{1,2} = W \times T_l \times \sigma_T(E) \times H_{avg}(E) \times \rho_a / m$$

$$F_3 = W \times T_l \times \sigma_f(E) \times Q \times \rho_a / m$$

, $W = \text{particle weight}$

$T_l = \text{track length (cm)} = \text{transit time} \times \text{velocity}$

$H_{avg}(E) = \text{average heating number (MeV/collisions)}$

$Q = \text{fission } Q\text{-value (MeV)}$

$m = \text{cell mass (gm)}$

F_1 F_2

, F_3

. F_1

, F_2

. F_3

1. Emitted and Recoverable Energies for Fission of U235

Form	Emitted Energy, MeV	Recoverable Energy, MeV	Remarks
Fission fragments	168	168	Neutron heating
Fission product decay			
- beta - rays	8	8	
- gamma - rays	7	7	
- neutrinos	12	-	
Prompt gamma - rays	7	7	Photon heating
Fission neutrons (kinetic energy)	5	5	Neutron heating
Capture gamma - rays	-	3 - 12	Photon heating
Total	207	198 - 207	
Fission Heating: Total – Fission product decay			

* "Introduction to Nuclear Reactor Theory", John R. Lamarsh, p.104

5.

MCCARD

SMART 2

MCPLIB02[9]

600K 가

5.1 SMART 2

4.95w/o UO2

20,000

1,200

200

2

가

3

4

MCNP

가

(=3)

4

96.9%,

0.9%,

2.3%

가

93.9%

6.1%

2. Photon Creation and Loss(2D Pin Cell)

Photon Creation(per source particles)					Photon Loss(per source particles)				
weight	MCCARD	sd(%)	MCNP	error(%)	weight	MCCARD	sd(%)	MCNP	error(%)
from neutrons	6.572E+00	0.006	6.572E+00	0.011					
annihilation	4.464E-01	0.077	4.467E-01	-0.065					
1st fluorescence	6.677E+00	0.012	6.678E+00	-0.020	pair production	2.232E-01	0.077	2.234E-01	-0.067
2nd fluorescence	1.546E+00	0.027	1.547E+00	-0.064	photoelectric capture	1.502E+01	0.009	1.502E+01	-0.010
total	1.524E+01		1.524E+01	-0.013	total	1.524E+01		1.524E+01	-0.011
energy	MCCARD	sd(%)	MCNP	error(%)	energy	MCCARD	sd(%)	MCNP	error(%)
from neutrons	6.283E+00	0.015	6.283E+00	0.007	incoherent scattering	2.975E+00	0.024	2.977E+00	0.045
annihilation	2.281E-01	0.077	2.283E-01	-0.069	coherent scattering	3.154E-03	0.061		
1st fluorescence	4.700E-01	0.012	4.702E-01	-0.028	pair production	6.879E-01	0.085	6.883E-01	-0.056
2nd fluorescence	2.512E-02	0.027	2.513E-02	-0.055	photoelectric capture	3.340E+00	0.013	3.341E+00	-0.025
total	7.006E+00		7.006E+00	0.002	total	7.006E+00		7.006E+00	0.002

3. Track Length Estimate of Particle Flux(2D Pin Cell)

Region	Tally	MCCARD		MCNP		error(%)
		flux(1/cm^2)	sd(%)	flux(1/cm^2)	sd(%)	
Fuel	Neutron	1.403E-01	0.010	1.404E-01	0.010	-0.020
	Photon	8.236E-02	0.019	8.234E-02	0.020	0.018
Cladding	Neutron	1.406E-01	0.010	1.407E-01	0.010	-0.016
	Photon	8.163E-02	0.022	8.161E-02	0.020	0.025
Coolant	Neutron	1.406E-01	0.009	1.406E-01	0.010	-0.011
	Photon	8.198E-02	0.023	8.196E-02	0.020	0.024

mccard		sd(%)		mcpn		sd(%)		error(%)		unit=mev/gm		in pellet region	
7.04E-05	0.19												
7.01E-05	0.19												
0.31													
1.35E-04	0.10	1.33E-04	0.09										
1.35E-04	0.10	1.33E-04	0.09										
0.01		0.06											
1.33E-04	0.09	1.32E-04	0.07	1.28E-04	0.09								
1.33E-04	0.09	1.32E-04	0.07	1.28E-04	0.09								
0.13		0.00		-0.11									
6.80E-05	0.10	1.30E-04	0.07	1.27E-04	0.07	6.43E-05	0.10						
6.79E-05	0.10	1.30E-04	0.07	1.27E-04	0.07	6.43E-05	0.10						
0.15		-0.08		-0.05		0.04							
1.28E-04	0.09	1.27E-04	0.06	6.05E-05	0.08	1.21E-04	0.07	6.33E-05	0.10				
1.29E-04	0.09	1.27E-04	0.06	6.04E-05	0.08	1.21E-04	0.07	6.33E-05	0.10				
-0.08		0.08		0.08		-0.08		0.08					
1.27E-04	0.09	1.26E-04	0.06	1.23E-04	0.06	1.23E-04	0.06	1.21E-04	0.07	6.26E-05	0.10		
1.27E-04	0.09	1.26E-04	0.06	1.23E-04	0.06	1.23E-04	0.06	1.21E-04	0.07	6.28E-05	0.10		
-0.06		0.06		0.03		-0.09		-0.01		-0.22			
6.54E-05	0.10	1.26E-04	0.07	1.24E-04	0.06	6.40E-05	0.07	1.24E-04	0.06	1.23E-04	0.07	1.22E-04	0.09
6.53E-05	0.10	1.26E-04	0.07	1.24E-04	0.06	6.41E-05	0.07	1.24E-04	0.06	1.23E-04	0.07	1.22E-04	0.09
0.06		-0.08		0.04		-0.09		-0.10		-0.08		-0.42	
1.24E-04	0.09	1.23E-04	0.07	5.92E-05	0.08	1.22E-04	0.06	1.22E-04	0.06	5.86E-05	0.08	1.21E-04	0.07
1.24E-04	0.09	1.23E-04	0.07	5.92E-05	0.08	1.22E-04	0.06	1.22E-04	0.06	5.86E-05	0.08	1.22E-04	0.07
-0.02		-0.03		0.04		0.01		-0.16		-0.05		-0.27	-0.44
1.23E-04	0.10	1.22E-04	0.07	1.20E-04	0.07	1.22E-04	0.07	1.22E-04	0.07	1.20E-04	0.07	1.22E-04	0.08
1.23E-04	0.10	1.22E-04	0.07	1.20E-04	0.07	1.22E-04	0.07	1.22E-04	0.07	1.20E-04	0.07	1.22E-04	0.08
-0.11		-0.01		-0.04		0.03		-0.22		-0.11		-0.01	-0.23

4. Track Length Estimate of Heating for Photon(2D Assembly)

mccard		sd(%)		mcpn		sd(%)		error(%)		unit=mev/gm		in pellet region	
3.03E-03	0.12	2.90E-03	0.11										
3.02E-03	0.12	2.90E-03	0.11										
0.19		0.08											
2.95E-03	0.11	2.82E-03	0.08	2.70E-03	0.11								
2.95E-03	0.11	2.81E-03	0.08	2.70E-03	0.11								
0.02		0.16		-0.05									
		2.76E-03	0.08	2.57E-03	0.08								
		2.77E-03	0.08	2.57E-03	0.08								
		-0.20		0.06									
2.75E-03	0.11	2.50E-03	0.08			2.35E-03	0.08	2.68E-03	0.08				
2.74E-03	0.11	2.50E-03	0.08			2.35E-03	0.08	2.68E-03	0.08				
0.29		-0.07		0.07		0.12							
2.72E-03	0.11	2.55E-03	0.08	2.39E-03	0.08	2.54E-03	0.08	2.56E-03	0.08				
2.72E-03	0.11	2.55E-03	0.08	2.39E-03	0.08	2.54E-03	0.08	2.56E-03	0.08				
-0.02		0.00		0.01		-0.09		-0.06					
		2.61E-03	0.08	2.46E-03	0.08			2.59E-03	0.08	2.49E-03	0.08	2.41E-03	0.11
		2.61E-03	0.08	2.46E-03	0.08			2.59E-03	0.08	2.49E-03	0.08	2.42E-03	0.11
		0.04		-0.32				-0.02		0.02		-0.15	
2.58E-03	0.11	2.37E-03	0.08			2.39E-03	0.08	2.34E-03	0.08	2.31E-03	0.08	2.43E-03	0.11
2.59E-03	0.11	2.37E-03	0.08			2.39E-03	0.08	2.34E-03	0.08	2.31E-03	0.08	2.43E-03	0.11
-0.30		0.06		-0.04		-0.07				-0.13		0.13	
2.46E-03	0.12	2.37E-03	0.09	2.23E-03	0.09	2.34E-03	0.08	2.34E-03	0.08	2.26E-03	0.09	2.38E-03	0.09
2.46E-03	0.12	2.37E-03	0.09	2.23E-03	0.09	2.34E-03	0.08	2.34E-03	0.08	2.26E-03	0.09	2.38E-03	0.09
0.00		0.04		0.17		0.02		-0.04		0.05		-0.07	-0.23

5. Track Length Estimate of Fission Heating(2D Assembly)

6.

MCCARD

, MCNP

. MCCARD

(gamma flux)

(track length estimate of energy deposition)

, MCCARD

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