

2 2

Development of two step two stage Fission Gas Release Model and Verification of High Burn-up UO₂ Thermal Conductivity Models

150

2 가

2 2

FRAPCON-3 in-pile

가 9

Abstract

In the first part of this study, 2 stages – 2 steps fission gas release model is developed, especially for high burn-up prediction. The mechanistic model mathematically simulates the two steps diffusion processes, matrix diffusion and grain boundary diffusion along with the two steps burn-up enhancement factor. For the benchmarking of the model, popular in-pile data sets already used in FRAPCON-3 code are taken. It turns out that at least within the burn-up limitation of the data sets predictions of the fractional release are comparatively better agreement with those of in-pile experimental results.

In the second part, recent models and experimental results of UO₂ thermal conductivity are collected and reviewed since it is one of the most influencing factors on the high burn-up nuclear fuel performance. Then they are thoroughly analyzed for the benchmarking of the models with the in-pile data sets also used in FRAPCON-3 code.

vs.

$$\frac{\partial C_v}{\partial t} = D_v^{eff} \frac{1}{R^2} \frac{\partial}{\partial R} \left(R^2 \frac{\partial C_v}{\partial R} \right) + \beta$$

$$: C_v(R, 0) = 0$$

$$: C_v(0, t) = \text{finite}$$

$$C_v(a, t) = \bar{C}_{gb}(t)$$

$$\beta \quad y\dot{F} \quad C_v$$

가

가

가

가

a

D_v^{eff}

Speight

$$w \frac{\partial C_{gb}}{\partial t} = w D_{gb}^{eff} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial C_{gb}}{\partial r} \right) - 2 D_v^{eff} \left(\frac{\partial C_v}{\partial R} \right)_{R=a}$$

$$: C_{gb}(r, 0) = 0$$

$$: C_{gb}(0, t) = \text{finite}$$

$$C_{gb}(b, t) = 0$$

w

가

, D_{gb}^{eff}

effective

D_v^{eff}

가

가

가

b 가 가

2 가

3

Green function

1

\bar{C}_{gb}

quasi-steady state

3

$$\alpha \frac{\partial C_v}{\partial R} \Big|_{R=a} - C_v(a, t) = 0$$

$$\alpha = \frac{2D_v^{eff}}{w\beta_1^2 D_{gb}^{eff}}$$

in-pile case

F

$$F \cong \frac{4}{\sqrt{\pi}} \left(\frac{a}{\alpha + a} \right)^2 \left(\frac{D_v^{eff} t}{a^2} \right)^{1/2} - \frac{3}{2} \left(\frac{a}{\alpha + a} \right) \left(\frac{D_v^{eff} t}{a^2} \right)$$

in-pile case

$\alpha = 0$

가

in-pile Booth model

가

$\alpha \gg a$

$$\left(\frac{a}{\alpha + a} \right)^2 \cong \left(\frac{a}{\alpha} \right)^2$$

α

$$\alpha \cong \frac{D_v^{eff}}{D_{gb}^{eff}} = \frac{D_{v_0}^{eff}}{D_{gb_0}^{eff}} e^{-(Q_v^{eff} - Q_{gb}^{eff})/RT}$$

$$Q_{gb}^{eff} \quad f_{Bu} Q_{gb}^{eff}$$

$$\alpha = \frac{D_{v_0}^{eff}}{D_{gb_0}^{eff}} e^{-Q/(RT + \beta Bu)}$$

$$\left(\frac{a}{\alpha + a}\right)^2 \cong \alpha_0 e^{-Q_2/(RT + \beta Bu)}$$

$$\alpha_0 = \left(\frac{a D_{gb_0}^{eff}}{D_{v_0}^{eff}}\right)^2 \quad Q_2 = -2Q$$

2 2

F

$$F = \frac{4}{\sqrt{\pi}} \exp\left(-\frac{Q_2}{RT + \beta Bu}\right) \left[\left(\frac{D_0}{a^2}\right) \exp\left(-\frac{Q_1}{RT}\right) t\right]^{1/2}$$

Bu Max(0, Burnup-25000)

25000 MWd/MtU

best-curve fitting

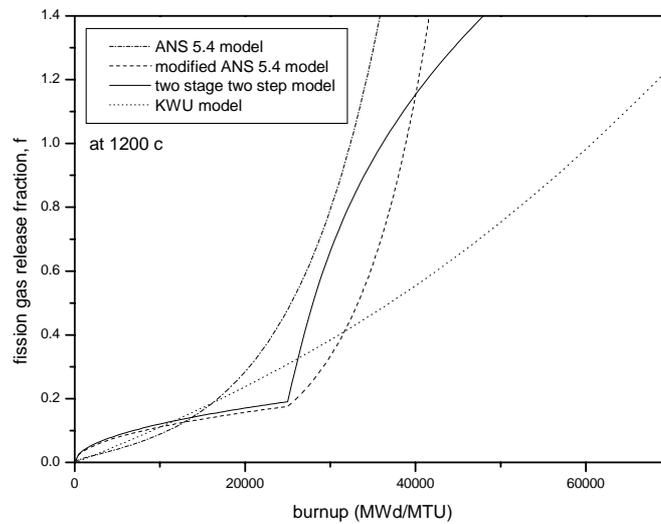
$$Q_1 = 45,527$$

$$Q_2 = 5,577$$

$$\alpha_0 = 1.8174$$

$$\left(\frac{D_0}{a^2}\right) = 0.00856$$

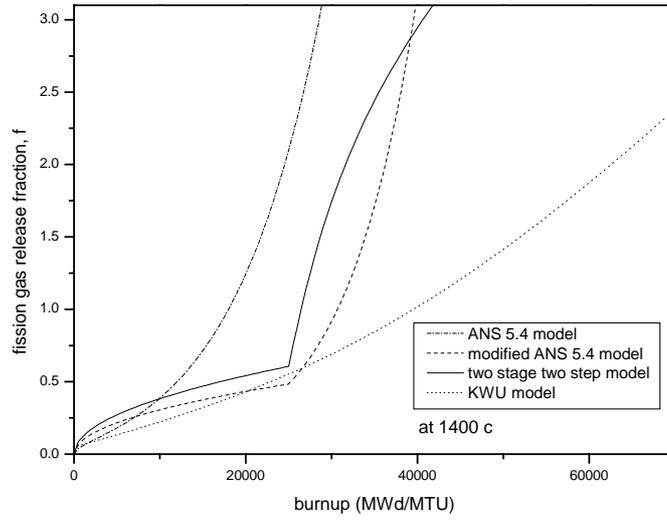
$$= 0.9$$



2.1

FGR vs.

(1200)



2.2 FGR vs. (1400)

1

modified ANS

5.4

2

가

가 가

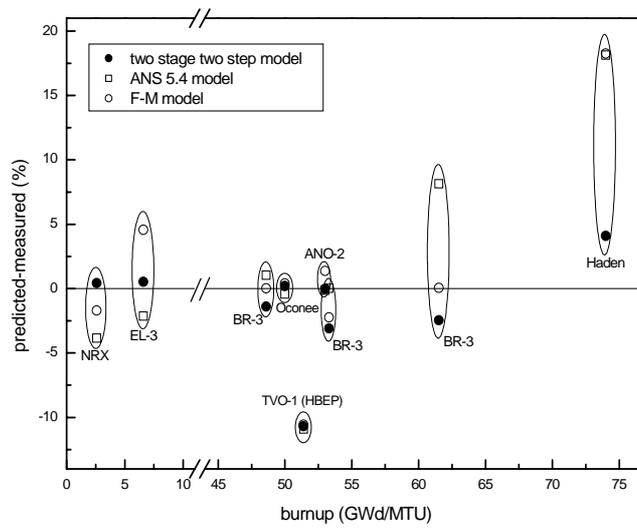
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2 2

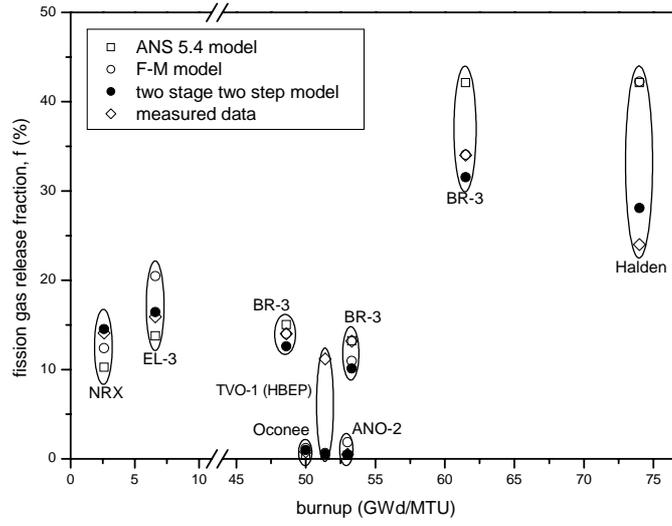
가

가

2 2 in-pile data



2.3 2 2



2.4 2 2

2 2

ANS5.4

Forsberg-Massih

2.4

2.3

2 2

가

가

2

ANS5.4

F-M

가

가

가

가 가

가

가

가 가

1

100%

가

가

2

가

2

가

100%

가 가

2 2

가

2 2

F

2 2

$$C_v(R,t) = \beta t \left[1 - 4 \left(\frac{a}{R} \right) \sum_{n=0}^{\infty} \left\{ i^2 \cdot \operatorname{erfc} \left(\frac{(2n+1)a-R}{2\sqrt{D_v^{\text{eff}} t}} \right) - i^2 \cdot \operatorname{erfc} \left(\frac{(2n+1)a+R}{2\sqrt{D_v^{\text{eff}} t}} \right) \right\} \right] \\ - \frac{2\pi D_v^{\text{eff}}}{aR} \sum_{n=1}^{\infty} (-1)^n \cdot n \cdot \sin \left(\frac{n\pi R}{a} \right) \int_0^t \exp \left(-\frac{D_v^{\text{eff}} n^2 \pi^2 (\lambda - t)}{a^2} \right) \phi(\lambda) d\lambda$$

$$w \frac{\partial C_{gb}}{\partial t} = w D_{gb}^{\text{eff}} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial C_{gb}}{\partial r} \right) - 2D_v^{\text{eff}} \left(\frac{\partial C_v}{\partial R} \right)_{R=a}$$

$$C_v(R,T) \quad C_{gb}(r,t) \quad F \\ C_{gb}(r,t) \quad 0 \quad \text{가}$$

3.

UO₂

가

가

가

가

UO₂

FRAPCON-3

/ 가

Lucuta (1996)

Harding

100%

가 UO₂

K₀

burn-up

(factorized)

$$K = f_{1d} f_{1p} f_{2p} f_{3x} f_{4r} K_0 \quad (W/mK)$$

▶

, $f_{1d}(\beta)$:

$$f_d(\beta) = \left(\frac{1.09}{\beta^{3.265}} + \frac{0.0643}{\sqrt{\beta}} \sqrt{T} \right) \arctan \left\{ \frac{1}{1.09 / \beta^{3.265} + (0.0643 / \sqrt{\beta}) \sqrt{T}} \right\}$$

▶

, $f_{1p}(p)$:

$$f_{1p}(p) = 1 + \left(\frac{0.019\beta}{3 - 0.019\beta} \right) \frac{1}{1 + \exp\{-(T - 1200)/100\}}$$

▶ Porosity Bubble, f_{2p} : $f_{2p} = \frac{1 - p}{1 + (1 - \sigma)p}$

▶ U/O, f_{3x} : $f_{3x} = 1$

▶ Radiation damage, f_{4r} : $f_{4r} = 1 - \frac{0.2}{1 + \exp\{(T - 900)/80\}}$

, T (Kelvin), β (%), p pore bubble, σ pore shape factor

FRAPCON-3 (1997)

FRAPCON-3 radiation damage, burn-up, porosity

$$K = f_d f_p f_m f_r K_o$$

▶, f_d :

$$f_d = \left(\frac{1.09}{B^{3.265}} + \frac{0.0643}{\sqrt{B}} \sqrt{T} \right) \arctan \left\{ \frac{1}{1.09 / B^{3.265} + (0.0643 / \sqrt{B}) \sqrt{T}} \right\}$$

▶, f_p :

$$f_p = 1 + \left(\frac{0.019\beta}{3 - 0.019\beta} \right) \frac{1}{1 + \exp\{-(T - 1200)/100\}}$$

▶ Porosity Bubble, f_m : $f_m = \frac{1 - p}{1 + (s - 1)p}$

▶ Radiation damage, f_r : $f_r = 1 - \frac{0.2}{1 + \exp\{(T - 900)/80\}}$

, T (Kelvin), B (%), p pore bubble, s pore shape factor

Halden (1997)

Halden

Halden model

가

, in-pile

UO₂ phonon interaction

phonon

$$1 / (A + BT)$$

‘A’

가

MATPRO

95%

UO₂

$$K = \frac{1}{0.1148 + 0.0035B + 2.475 \times 10^{-4}(1 - 0.00333B)T} + 0.0132 \exp^{(-0.001887T)}$$

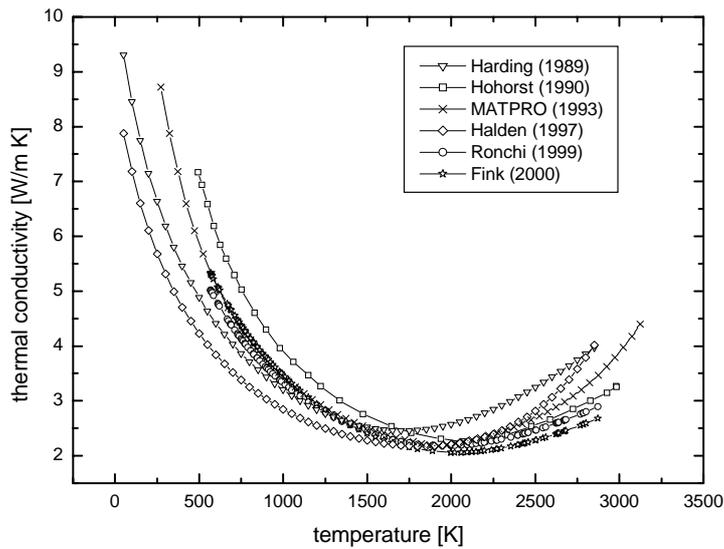
, T (), B (MWd/kgU)

Fink (2000)

Fink가 UO₂ (transport) , Ronchi phonon lattice term 95% UO₂

$$K = \frac{100}{7.5408 + 17.692(T/1000) + 3.6142(T/1000)^2} + \frac{6400}{(T/1000)^{5/2}} \exp\left\{-\frac{16.35}{(T/1000)}\right\}$$

, T



3.1 1989

UO₂

. UO₂

가

UO₂

FRAPCON-3

creep,

가 in-pile 가 Halden
가 가
가 UO₂ in-pile
가

4.

70,000 MWd/MtU

가 가
/
가 , 가
2 2 in-pile
/
Massih ANS 5.4 Forsberg-
in-pile 가가 가
가 가
in-pile / 가
/
/ 가 in-pile 가 Halden
가 가 가 UO₂
in-pile 가

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