

## Comparison of Theoretical Models and Finite Element Simulation of ZrO<sub>2</sub>-based Composites for Inert Matrix Fuel

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### 1. Introduction

The improvement of thermal properties of ZrO<sub>2</sub> has been investigated in many ways to enhance the performance of inert matrix fuel (IMF). Inert matrix fuel is a useful concept to burn transuranic elements (TRU) without increasing extra plutonium [1]. The addition of reinforcements with a high thermal conductivity has been proposed in the previous studies [2-4]. Molybdenum and silicon carbide are good candidate materials for the reinforcement because of their high thermal conductivities and low neutron absorption cross sections. Recently, ZrO<sub>2</sub>-based composites reinforced with Mo-wire mesh or carbon foam were fabricated by spark plasma sintering [5, 6]. When the effects of the structures of reinforcements were compared, interconnected structures provided more enhanced thermal conductivity than discrete structures. The effective thermal conductivity of composite materials with various reinforcement structures can be calculated by using the finite element analyses. Raj et al calculated the effective thermal conductivities of ZrO<sub>2</sub>-based composites with various structured Mo reinforcements as schematically shown in Fig. 1 [7].

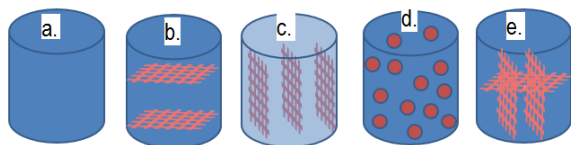


Fig. 1. a) ZrO<sub>2</sub> b) ZrO<sub>2</sub>-Perpendicular Mo Mesh Plane c) ZrO<sub>2</sub>-Parallel Mo Mesh Plane d) ZrO<sub>2</sub>- Mo Powder reinforcement e) ZrO<sub>2</sub>- Mo 3D Network

The objective of this study is to compare the results of finite element analyses and the analytical models in predicting the thermal conductivity of ZrO<sub>2</sub> composites reinforced with discrete phase Mo particles and interconnected Mo structure.

### 2. Finite Element Simulation

In this study, various structures of Mo reinforcements have been used as shown in Fig. 2. They are three dimensional interconnected Mo wire, particulate discrete Mo powder, Mo wire mesh, Mo fiber and Mo sheet. 3D model of ZrO<sub>2</sub>-Mo unit cells has been constructed using Solidworks<sup>TM</sup> and finite element analyses have been

performed by using ANSYS<sup>TM</sup>. The effective thermal conductivities of the ZrO<sub>2</sub>-Mo composites can be calculated using the thermal conductivity equation:

$$K = \frac{Q * L}{A * \Delta T} \quad (1)$$

Where Q is the heat flux applied, L is the length along which heat flows, A is the cross sectional area, ΔT is the temperature difference between the two surfaces where constant temperature and heat flux conditions are applied.

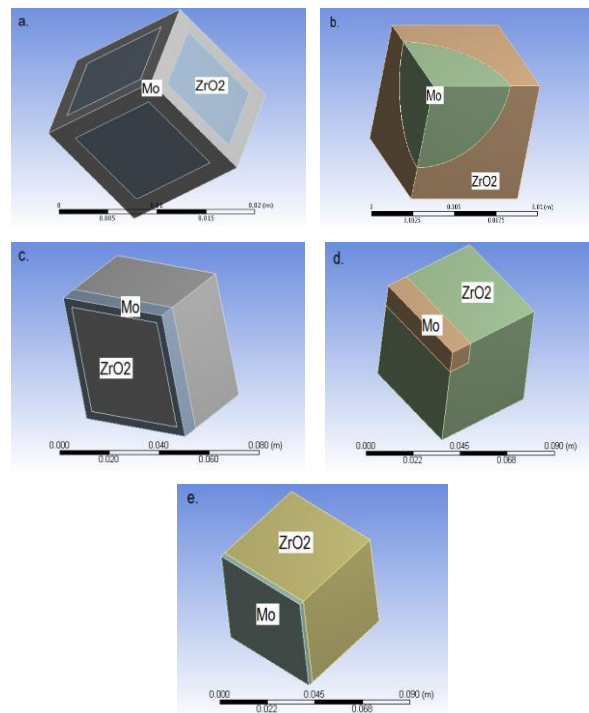


Fig. 2. Solid models of various structured Mo reinforced ZrO<sub>2</sub> composites; a) 3D Mo, b) Mo particle, c) Mo mesh, d) Mo fiber, e) Mo sheet.

### 3. Theoretical Models

The Maxwell's model of composite materials predicts the effective thermal conductivity with a good accuracy for spherical, non-interacting reinforcement particles with a low volume fraction (less than 10%) [8].

$$K = K_m \frac{(2 - 2V_r)K_m + (1 + 2V_r)K_r}{(2 + V_r)K_m + (1 - V_r)K_r} \quad (2)$$

Dul'nev et al. proposed a 3D model with a cubic unit cell structure to predict the thermal conductivity of interconnected reinforcement materials [9]. The effective thermal conductivity is expressed by equation 3.

$$K = K_r t^2 + K_m(1 - t)^2 + \frac{2t(1 - t)K_r K_m}{K_m t + K_r(1 - t)} \quad (3)$$

$$t = \frac{1}{2} + \cos\left(\frac{1}{3}\cos^{-1}(2p - 1) + \frac{4\pi}{3}\right)$$

where  $K_r$ ,  $K_m$  and  $K$  is the thermal conductivity of the reinforcement, the matrix and the composite, respectively,  $V_r$  is the volume fraction of the reinforcement,  $P$  is the porosity,  $t$  is dimensionless thickness of the foam skeleton.

Fig. 3 shows the thermal conductivity of ZrO<sub>2</sub>-Mo (5 vol. %) composites at different temperature as predicted by FEM method and analytical models (Maxwell and Dul'nev) for discrete particles and interconnected phase and Fig. 4 shows the effect of the volume fraction of Mo phase. As can be seen from Fig. 3 and Fig. 4, a good agreement was found between the analytical models and FEM method.

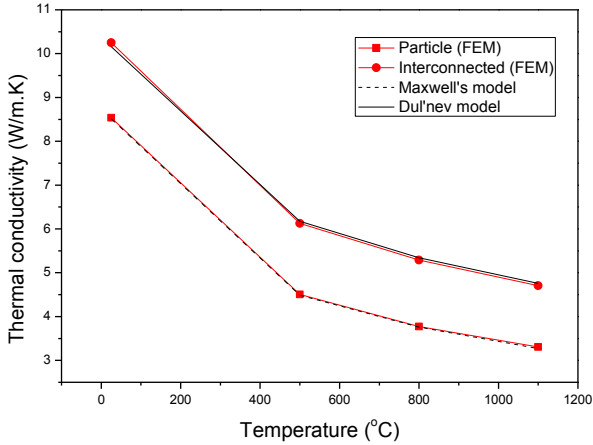


Fig. 3. Calculated thermal Conductivities of 5 vol.%Mo reinforced ZrO<sub>2</sub> composites as function of temperature.

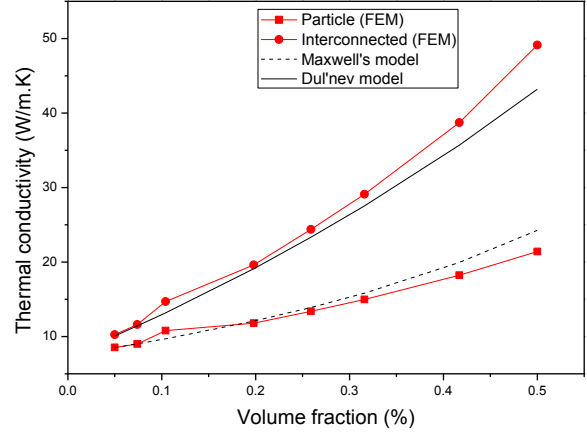


Fig. 4. Calculated thermal Conductivities of Mo reinforced ZrO<sub>2</sub> composites as function of volume fraction.

#### 4. Conclusions

The finite element analyses presented a good agreement with theoretical models in estimating the effects of the reinforcement on the thermal conductivities of discrete Mo reinforced ZrO<sub>2</sub> nanocomposites. It is found that the effects of interconnected thermal reinforcements on the effective thermal conductivity can be estimated by using the percolation model.

#### REFERENCES

- [1] C. Degueldre, T. Arima, and Y.W. Lee, Thermal conductivity of zirconia based inert matrix fuel: use and abuse of the formal models for testing new experimental data. *Journal of nuclear materials*, Vol.319, p.6, 2003.
- [2] S. Yeo, E. Mckenna, R. Baney, G. Subhash, and J. Tulenko, Enhanced thermal conductivity of uranium dioxide-silicon carbide composite fuel pellets prepared by Spark Plasma Sintering (SPS). *Journal of Nuclear Materials*, Vol.433, p.66, 2013.
- [3] X.D. Liu, J.S. Zhang, X.M. Cao, and H. Zhang, Finite element simulation of the thermal properties of particulate and continuous network-reinforced, *Proceedings of the Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture*, Vol.219, p.111, 2005.
- [4] Tae Won Cho, Dong-Seong Sohn, and Yeon Soo Kim, Thermal conductivity of U-Mo/Al dispersion fuel: effects of particle shape and size, stereography, and heat generation, School of Mechanical and Nuclear Engineering, Ulsan National Institute of Science and Technology (UNIST), UNIST-gil 50, Ulsan 689-798, Republic of Korea, Argonne National Laboratory, 9700 S. Cass Ave, Argonne, IL 60439, USA, Published online: 10 Apr 2015.
- [5] Joon Hui Kim, Soon H. Hong, and Ho Jin Ryu, Enhanced Thermal Conductivities of Mo wire reinforced Zirconium Oxide Pellets, Korean Nuclear Society Spring meeting, 2014.
- [6] Malik Adeel Umer, Qusai Mahmoud Mistarihi, Jun Hui Kim, Ho Jin Ryu, Enhanced thermal conductivity of carbon reinforced ZrO<sub>2</sub> composites, Korean Nuclear Society Fall meeting, 2014.

- [7] V. Raj, Q. M. Mistarih, and H. J. Ryu, Thermal Property Simulation of ZrO<sub>2</sub>-based Nanocomposites for Inert Matrix Fuel, , Korean Nuclear Society Spring meeting, 2015.
- [8] W.D. Kingery, Introduction to Ceramics, 2nd ed., p. 636, Wiley, New York (1976).
- [9] G.N. Dul'nev, Heat transfer through solid disperse systems, Journal of engineering physics, vol. 9, p. 275 (1965).