
Impairment of Heat Transfer in the Passive Cooling System due to Mixed Convection

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Myeong-Seon Chae and Bum-Jin Chung

Dept. of Nuclear Engineering, Kyung Hee University



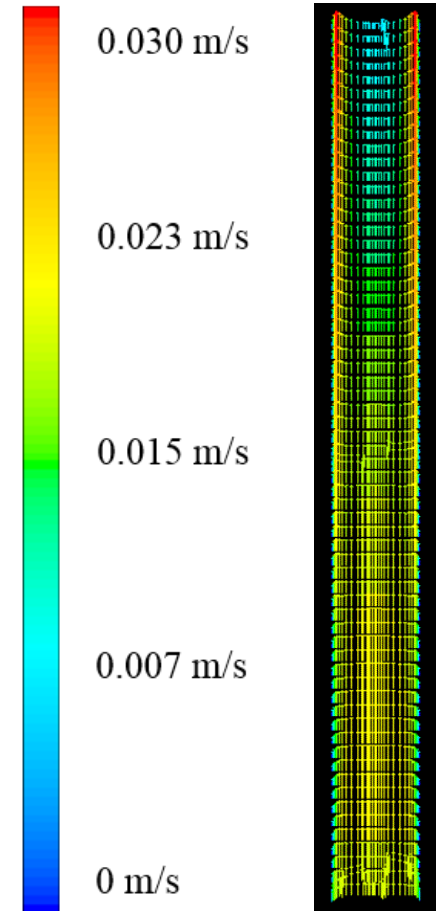
Introduction (1/3)

- Adoption of the **Passive Cooling System** has been increasing
 - The concept of passive safety is emphasized in design of NPP to accomplish the enhanced safety goal
- The passive cooling system focused on the **Natural convection cooling** and **heat transfer**
 - Under accident conditions to remove the residual heat out of the containment
- The **Reactor Cavity Cooling System (RCCS)** is the passive cooling system
 - Very High Temperature Reactor (VHTR) designed to remove the residual and decay heat



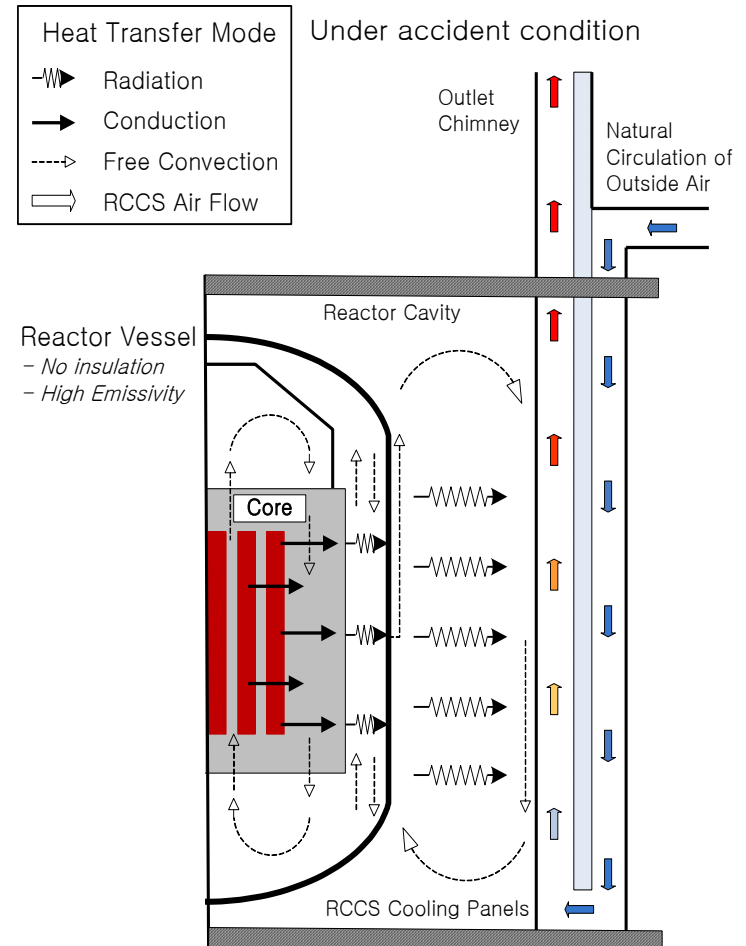
Introduction (2/3)

- When the natural convection occurs in the long enough heated section,
- The flow regime becomes similar to the **forced convection**
 - Due to the duct flow condition
- This **force convective flow** together with the **local buoyancy effect** can form
 - Complex **mixed convective flow condition**



Introduction (3/3)

- RCCS(Reactor Cavity Cooling System)?
 - The decay heat transfers from the fuels to the graphite by **Conduction**
 - It transfers to reactor vessel and RCCS cooling panels (Riser tube) by **Radiation** and **Convection**
 - **The buoyant flows are induced** in riser tubes (The fluid temperature \uparrow , Density \downarrow)
 - Natural circulation of fluid in riser tubes occurs
- This paper discuss
 - Local heat transfer rate in riser tube can be impaired due to the **Mixed convective flows**



[J.H. Kim et al., KAERI, 2015]

Background (1/4)

- Convective heat transfer is described in one mode **which mode is mainly dominated as heat transfer phenomena** (Mode : Natural convection, Forced convection)
- Pure forced convection
 - When the flow is generated by external force, **effect of natural convection can be neglected** in heat transfer
- Mixed convection
 - When the flow is generated by internal and external force, **the natural convection should be considered**
 - The Mixed Convective flow is influenced both by Re and Gr
 - The governing parameter B_o should be the combination of both numbers
- B_o , lots of different combinations were used depending on the investigators

$$\frac{Gr}{Re^2}$$

[Easby, 1978]

$$\frac{Gr}{Re}{}^{3.636} Pr^{0.818}$$

[Alferov et al., 1973]

$$\frac{Gr}{Re}{}^{3.425} Pr^{0.8}$$

[Rouai, 1987]

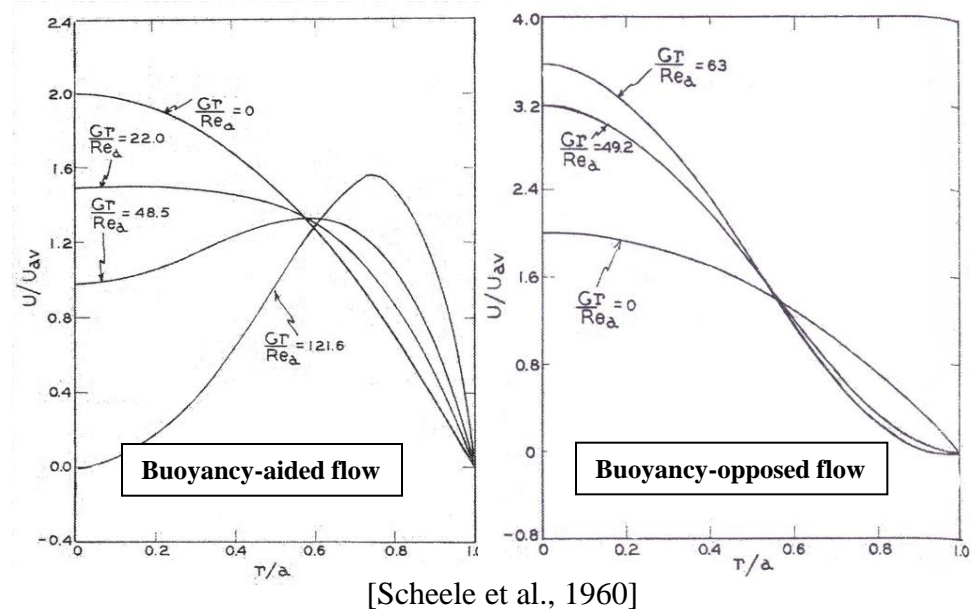
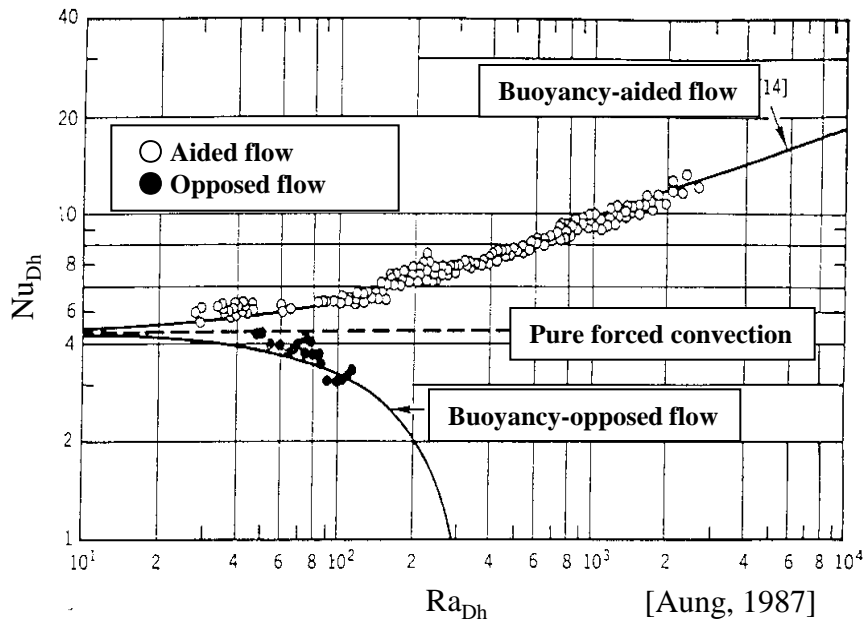
$$8 \times 10^4 \frac{Gr}{Re}{}^{3.425} Pr^{0.8}$$

[Hall and Jackson, 1969]



Background (2/4)

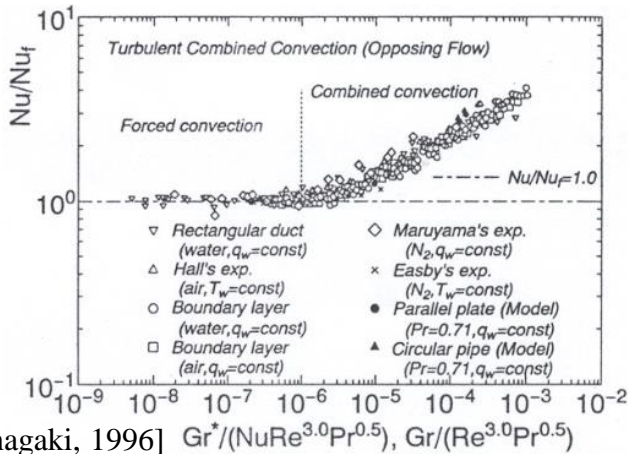
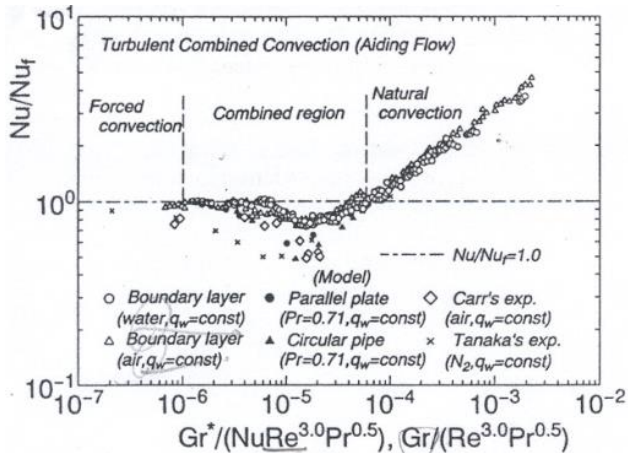
- Heat transfer behavior in Laminar flow



- Buoyancy-aided flow : **Enhanced Nu** compared to the forced convection
→ Velocity enhances near the heated wall
- Buoyancy-opposed flow : **Impaired Nu** compared to the forced convection
→ Flow velocity reduced

Background (3/4)

- Heat transfer behavior in Turbulent flow



- Buoyancy-aided flow

- An impairment of the heat transfer rate for small buoyancy

- **Laminarization**

- Same direction of buoyancy impaired turbulence production

- Then, a gradational enhancement for large buoyancy (over critical Gr)

- Buoyancy-opposed flow

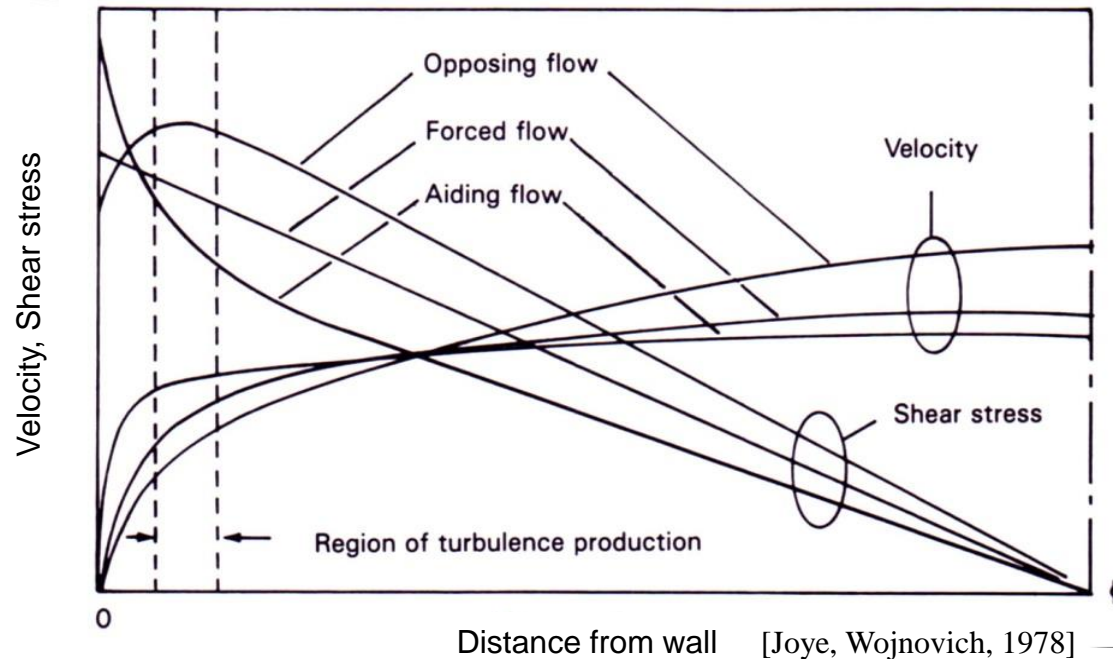
- Enhanced of the heat transfer rate

- **Increased turbulence production**



Background (4/4)

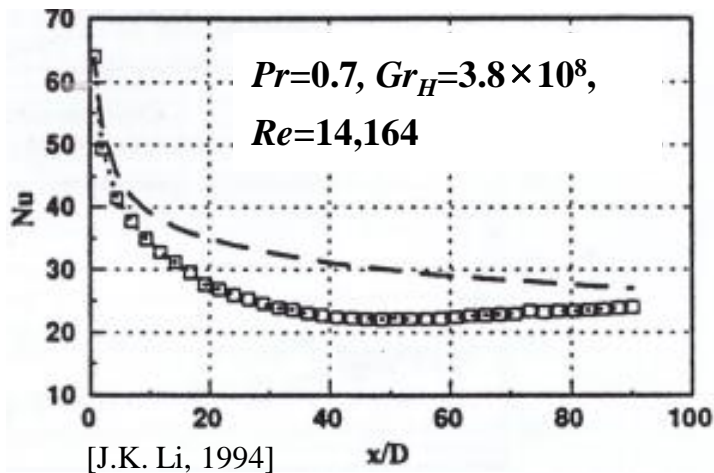
- Turbulence production



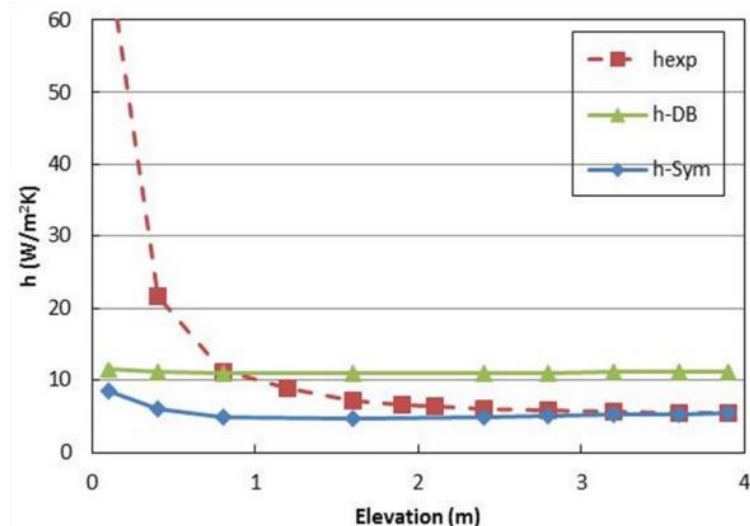
- The region of turbulence production is **Edge of viscous sublayer**
- Proportion of shear stress, velocity gradient

Analysis

- The local Nu of the axial position pipe was impaired in certain local Gr and Re range correspond to the forced convection (**Laminarization**)
- The local Nu is recovered or enhanced
 - This can be associated with the **recovery of turbulence production**



- The Nu distribution exhibits the non-monotonic behavior



[J.H. Kim et al., KAERI, 2015]

Mass transfer experiments using analogy concept

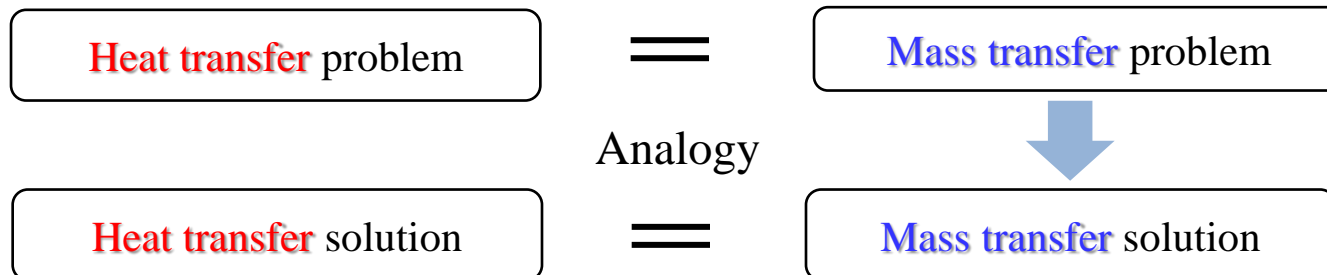
- Governing equations

Heat transfer	Mass transfer
$\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 0$	
$\rho \frac{Du}{Dt} = -\frac{\partial P}{\partial x} + \mu \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) + X$	
$\frac{DT}{Dt} = \alpha \nabla^2 T$	$\frac{DC}{Dt} = D_m \nabla^2 C$

- Dimensionless numbers

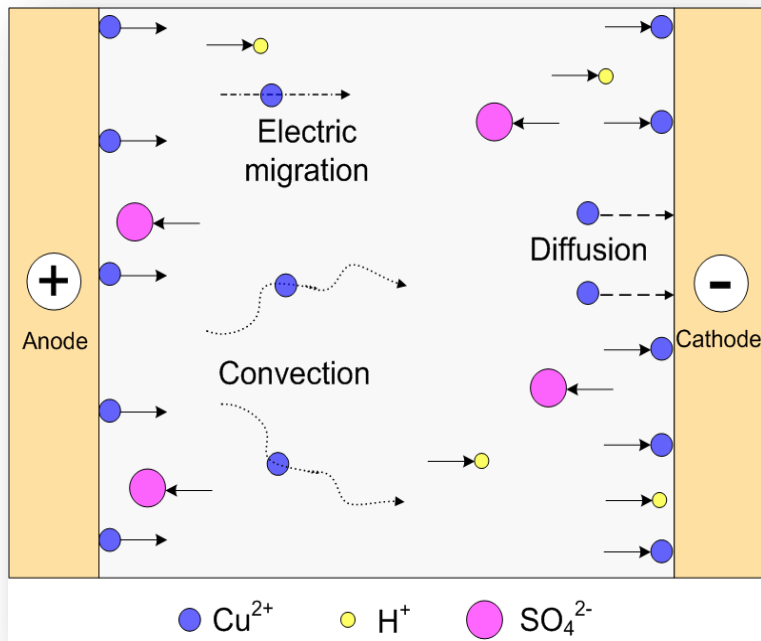
Heat transfer	Mass transfer
$Nu = \frac{h_h L}{k}$	$Sh = \frac{h_m L}{D_m}$
$Pr = \frac{\nu}{\alpha}$	$Sc = \frac{\nu}{D_m}$
$Ra = \frac{g \beta \Delta T L^3}{\alpha \nu}$	$Ra = \frac{g L^3 \Delta \rho}{D_m \nu \rho}$
$Re = \frac{u D_h}{\nu}$	

- Analogy concept



Copper Electroplating System

- Measurements were made using limiting electroplating current technique with $\text{CuSO}_4\text{-H}_2\text{SO}_4$



- Total mass transfer rate = Electric migration + **Diffusion** + **Convection**

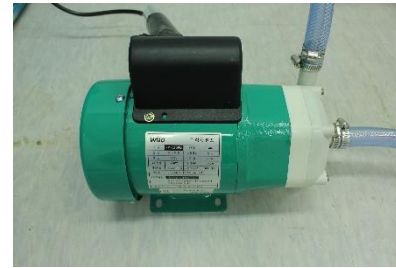
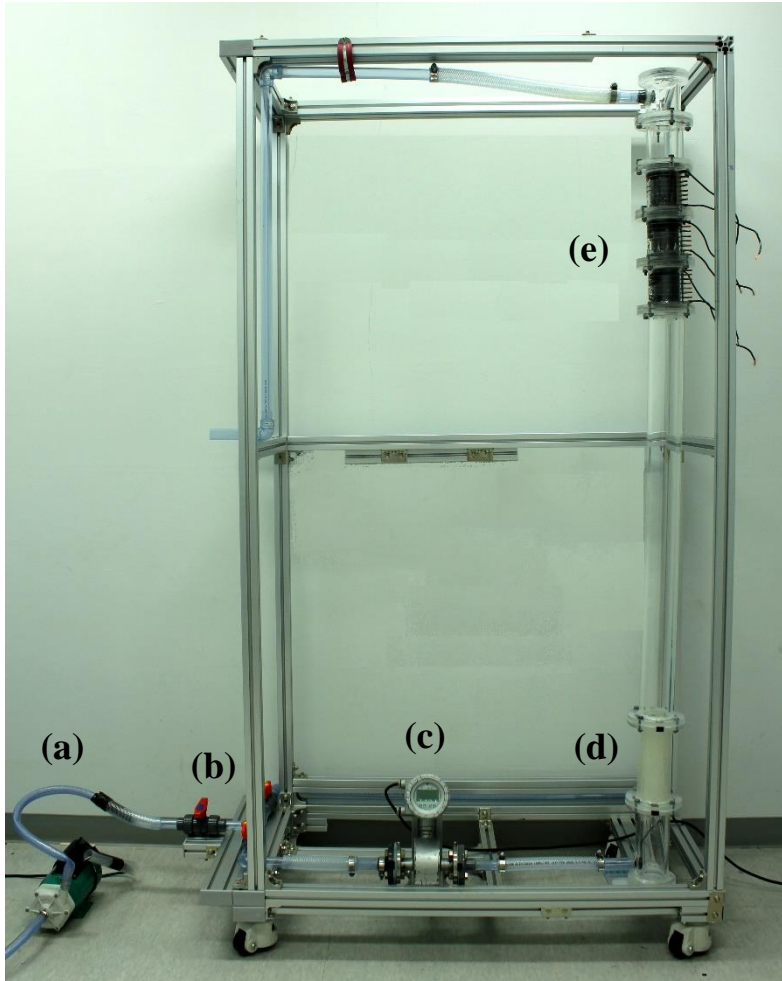
$$(N_T = N_{Em} + N_D + N_C)$$

Not exist in heat transfer, thus minimize it using H_2SO_4

- Mass transfer coefficient

$$h_m = \frac{(1-t_n)I_{lim}}{nF(C_b - C_s)} \rightarrow C_s \approx 0$$

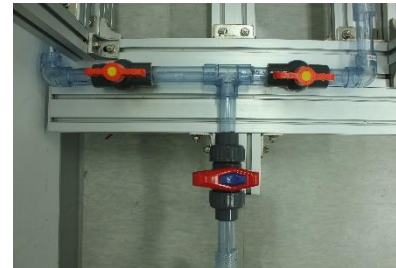
Experiments - Apparatus



(a) Electric pump



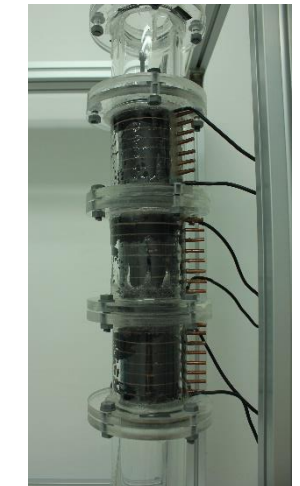
(d) Flow straightener



(b) Bypass valve

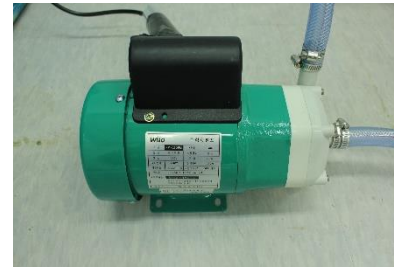
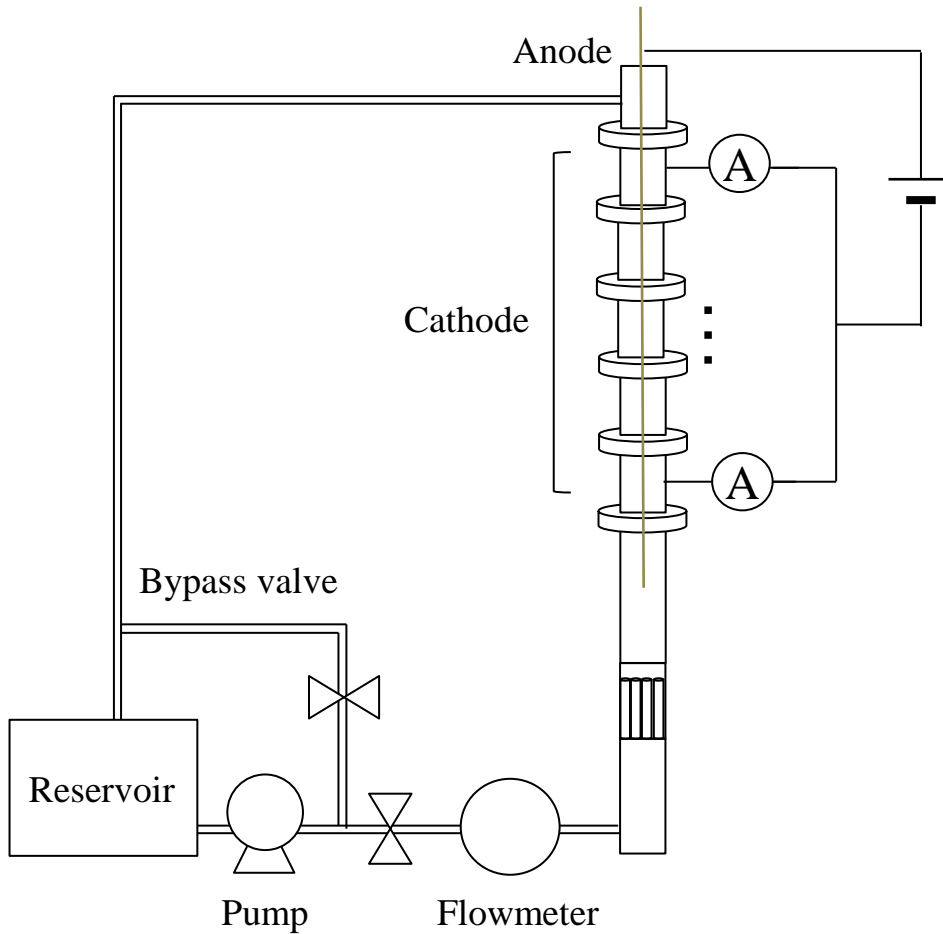


(c) Magnetic flowmeter



(e) Test section

Experiments - Apparatus



(a) Electric pump



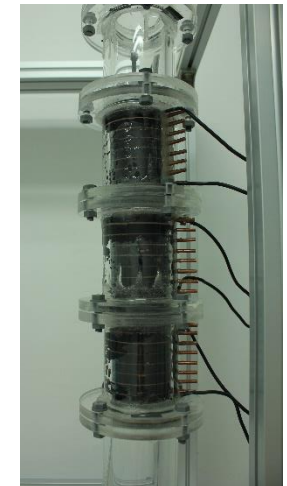
(d) Flow straightener



(b) Bypass valve

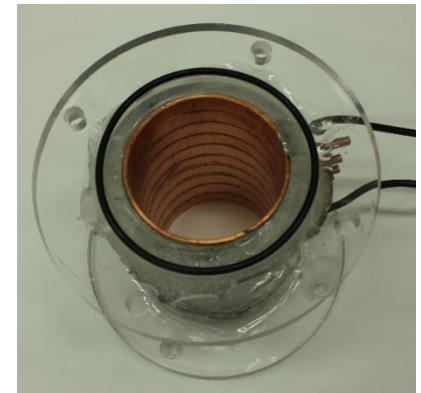
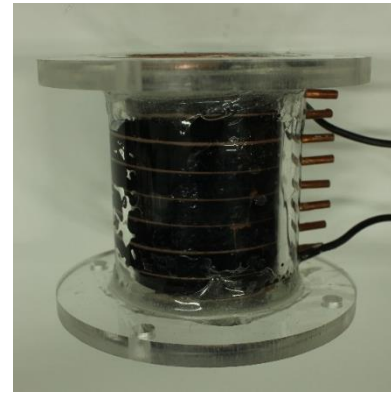
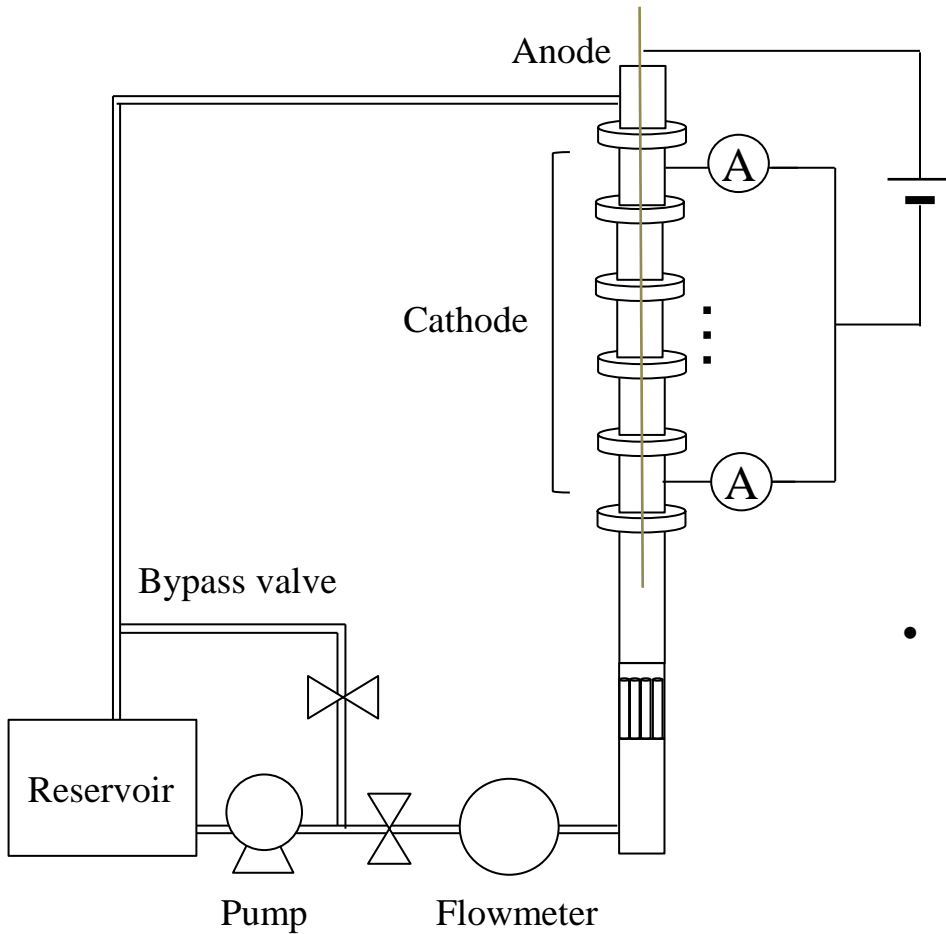


(c) Magnetic flowmeter



(e) Test section

Experiments - Apparatus



- Adopted piecewise electrodes in order to measure the *local average Nu*
– 0.01m × 15 piece (Total length 0.15m)

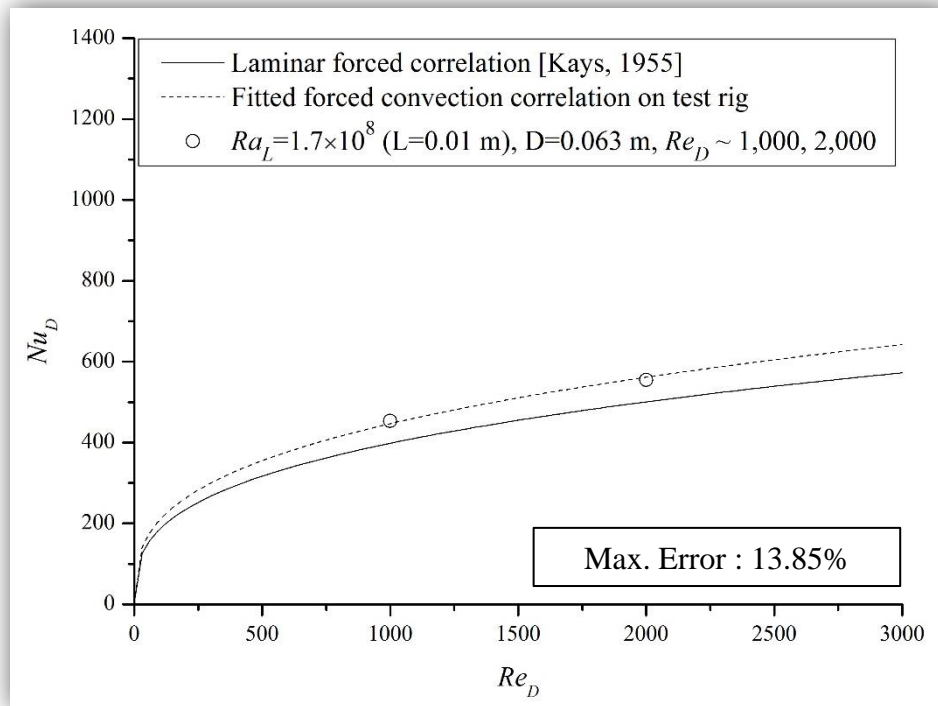
Experiments – Test matrix

	NACEF	Present test facility
Test section type	Rectangular duct	Circular duct
D (m)	0.04 (L=0.24)	0.063
D_h (m)	0.069	0.063
L (m)	4.0	0.15
Velocity (m/s)	1.9	0.11
Re_{Dh}	6,300	
Ra_L	5.7 × 10 ¹¹	
Gr_L	8.0 × 10 ¹¹	2.7 × 10 ⁸
Pr	0.7	2,094

Pr	D (m)	L (m)	Ra_L	Re_{Dh}
2,094	0.063	0.01	1.7 × 10 ⁸	1,000, 2,000, 6,300, 10,000, 12,800
		0.15	5.7 × 10 ¹¹	

Results : Comparison with correlation (1/3)

- Comparison of test results with forced convection correlation (Laminar)
 - Kays (1955) : Laminar forced convection correlation (Thermal developing, Hydrodynamic fully developed condition)
 - Fitted forced correlation developed on test rig



- Kays, 1955

$$Nu_D = 3.66 + \frac{0.0668Gz}{1 + 0.04Gz^{2/3}} \quad Pr \geq 5$$

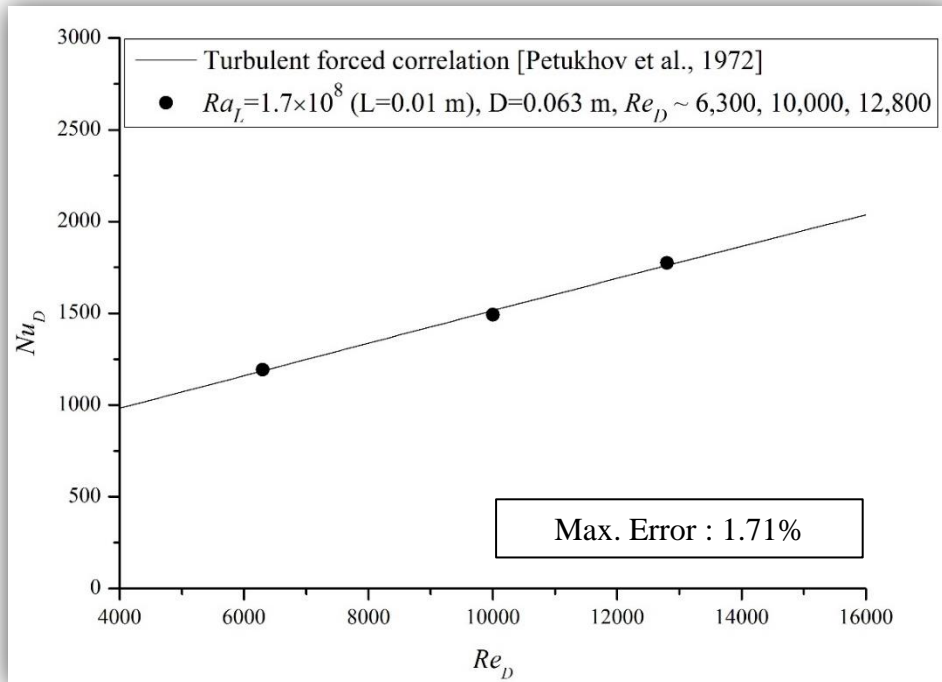
- Fitted correlation

$$Nu_D = 3.66 + \frac{0.075Gz}{1 + 0.04Gz^{2/3}}$$

$$Gz = Re_D Pr (D / L)$$

Results : Comparison with correlation (2/3)

- Comparison of test results with forced convection correlation (Turbulent)
 - Petukhov et al. (1972) : Turbulent forced convection correlation (Thermal developing, Hydrodynamic fully developed condition)



- Petukhov et al., 1972

$$Nu_D = C_{therm.} \times Nu_{fc}$$

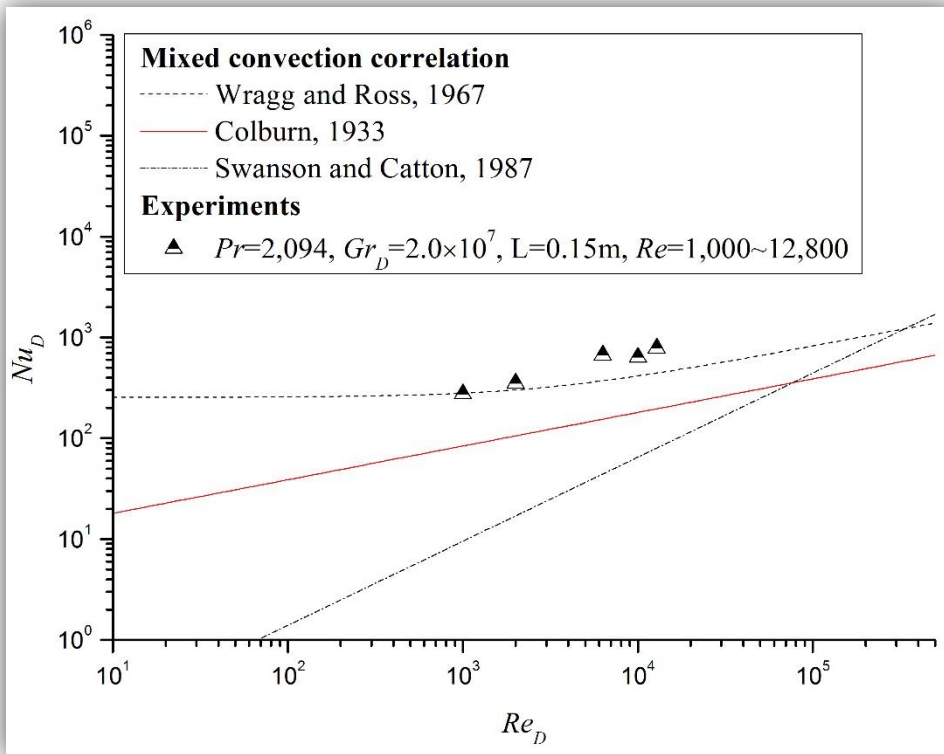
$$Nu_{fc} = \frac{Re \times Pr \times \left(\frac{f}{8}\right)}{1.07 + \left(\frac{900}{Re}\right) - \left(\frac{0.63}{1 + 10 \times Pr}\right) + 12.7 \times \sqrt{\frac{f}{8}} \times (Pr^{\frac{2}{3}} - 1)}$$

$$f = \left[1.82 \times \log\left(\frac{Re}{8.0}\right) \right]^{-2}$$

$$C_{therm.} = 1 + 0.48 \times \left(1 + \frac{3600}{Re \sqrt{x/D}} \right) \times \frac{e^{-0.17(x/D)}}{(x/D)^{0.25}}$$

Results : Comparison with correlation (3/3)

- Comparison of test results with mixed convection correlation
 - Similar to Wragg and Ross's correlation



- Wragg and Ross, 1967

$$Sh_D = 1.95 \left[Re_D Sc D / L + 0.0532 (Gr_D Sc D / L)^{0.75} \right]^{0.33}$$

- Colburn, 1933

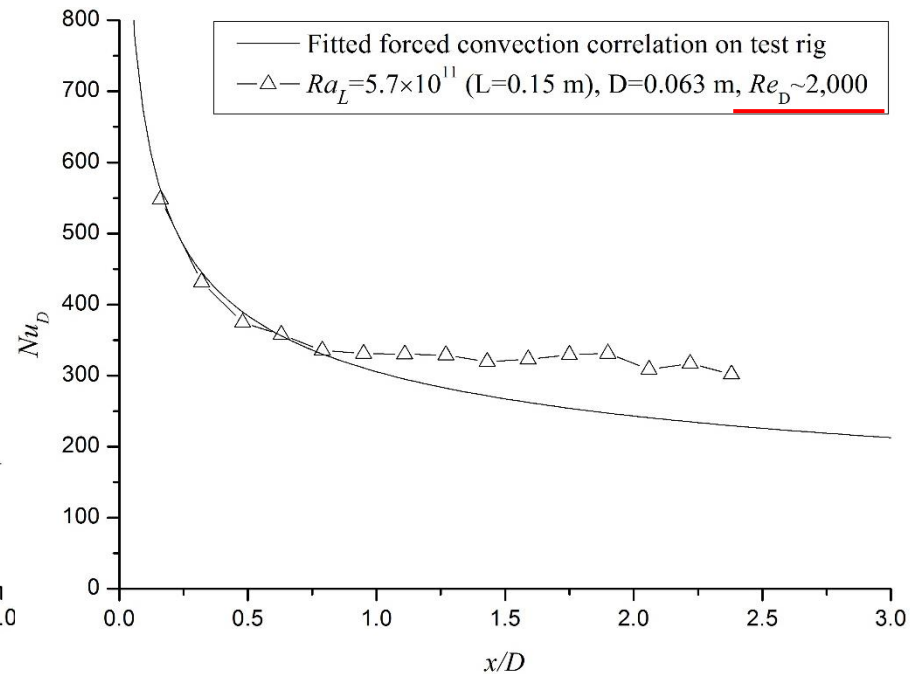
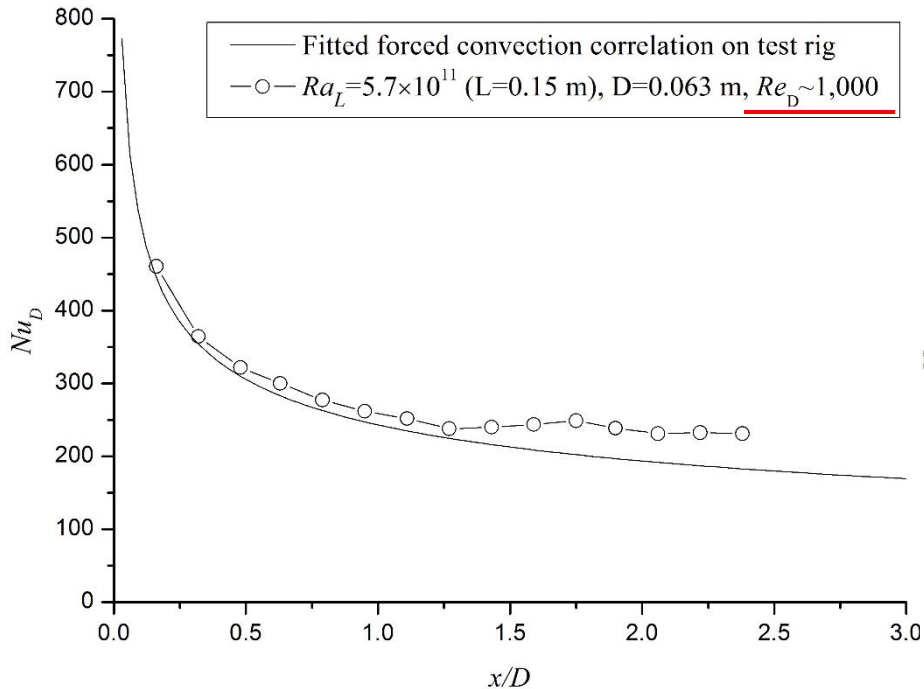
$$Nu_D = 1.65 (Re_D Pr D / L)^{1/3} [1 + 0.015 (Gr_D)^{1/3}]$$

- Swanson and Catton, 1987

$$Nu_D = 0.0115 Re^{0.8} Pr^{0.5} \left[1 + \left\{ 1 - \left(\frac{696}{Re_D^{0.8}} \right) + \left(\frac{8300 Gr_D}{Re_D^{0.26} Pr^{0.5}} \right) \right\}^{0.39} \right]^{-1/3}$$

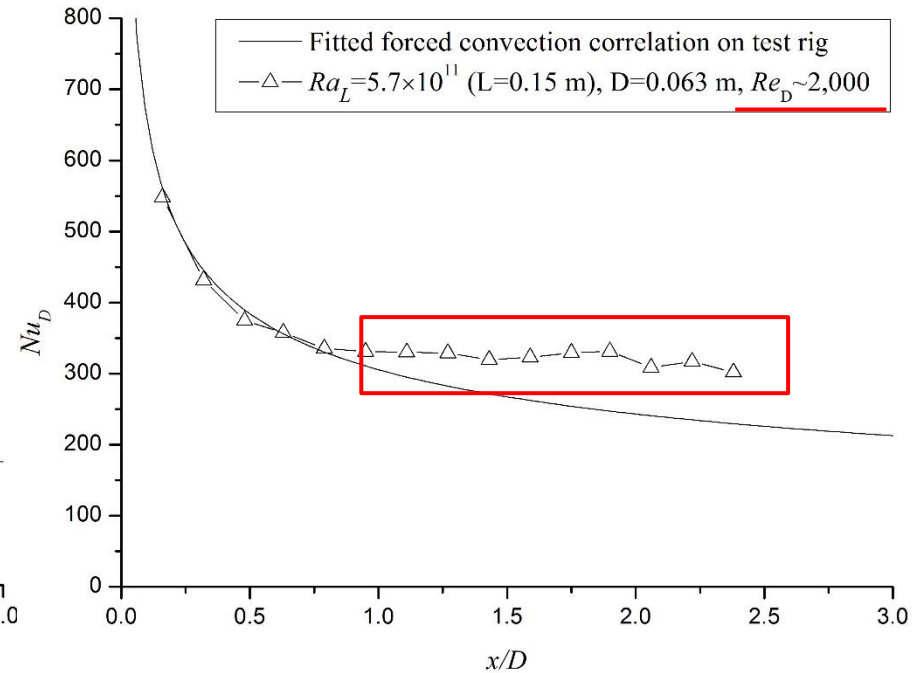
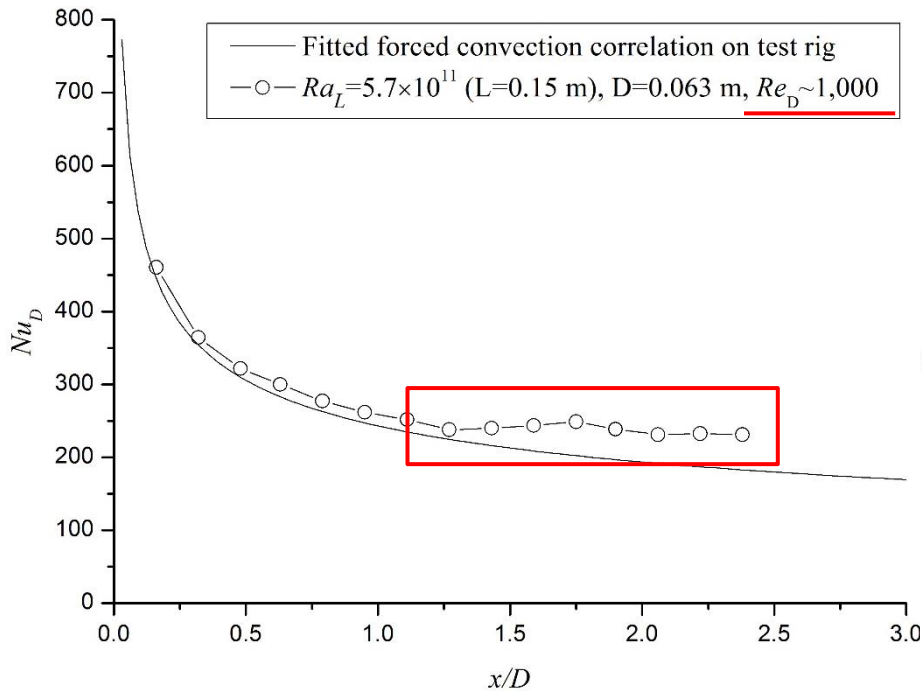
Results : x/D vs. Nu_D (1/4)

- x/D vs. Nu_D (Laminar flow)



Results : x/D vs. Nu_D (1/4)

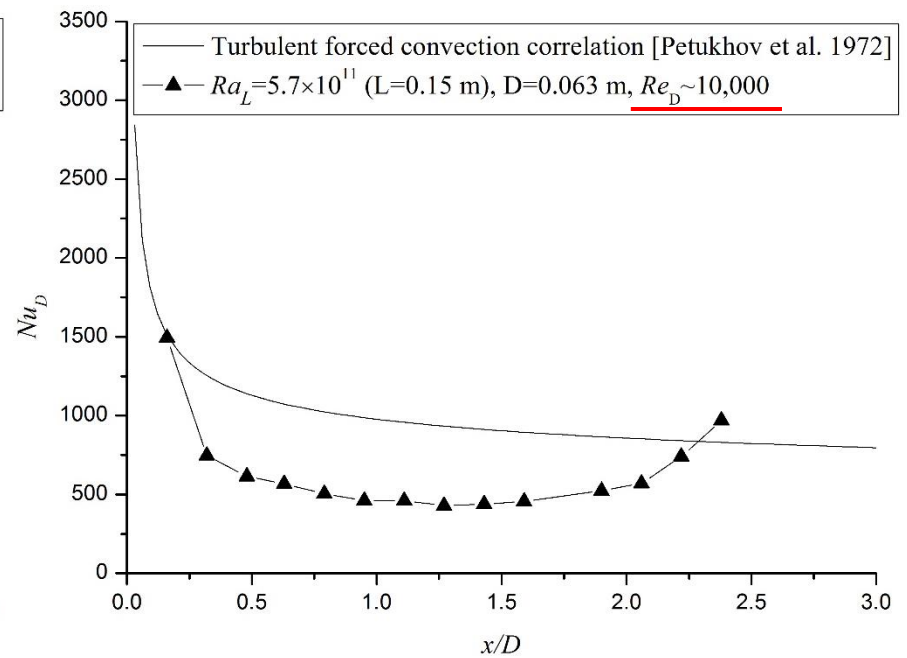
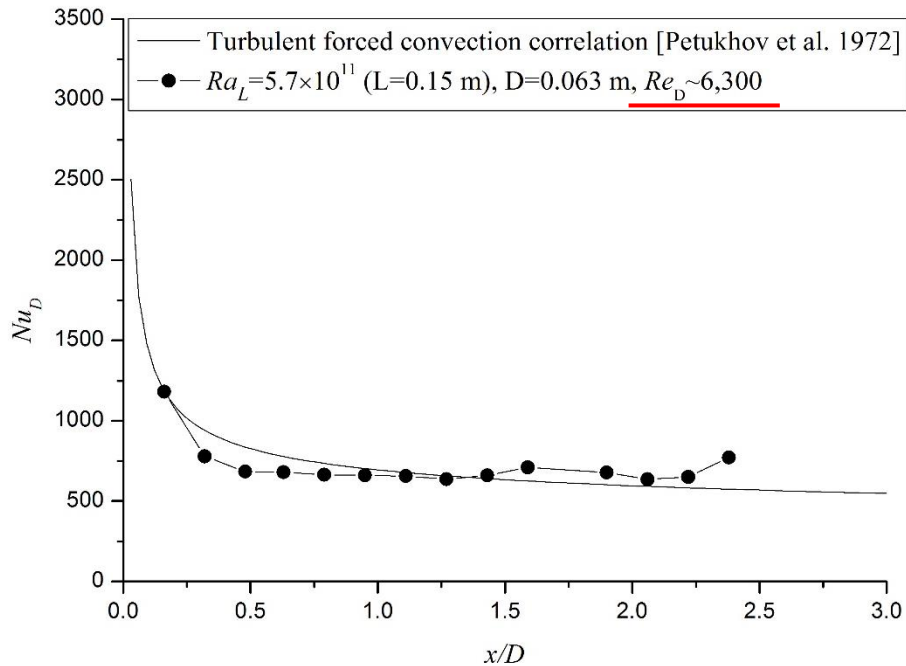
- x/D vs. Nu_D (Laminar flow)



- Increased x/D , Nu_D enhanced \rightarrow Initial velocity enhanced

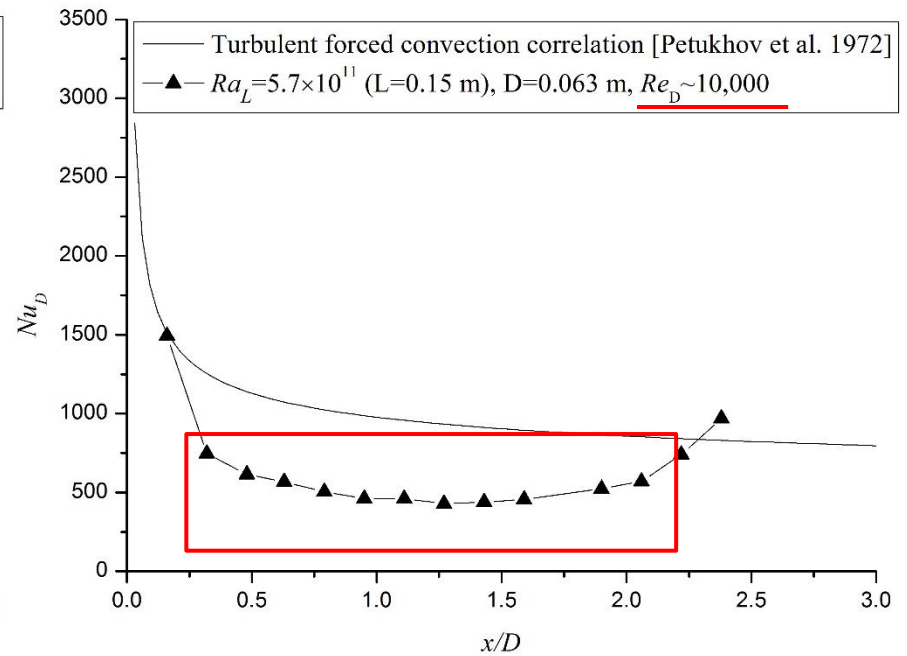
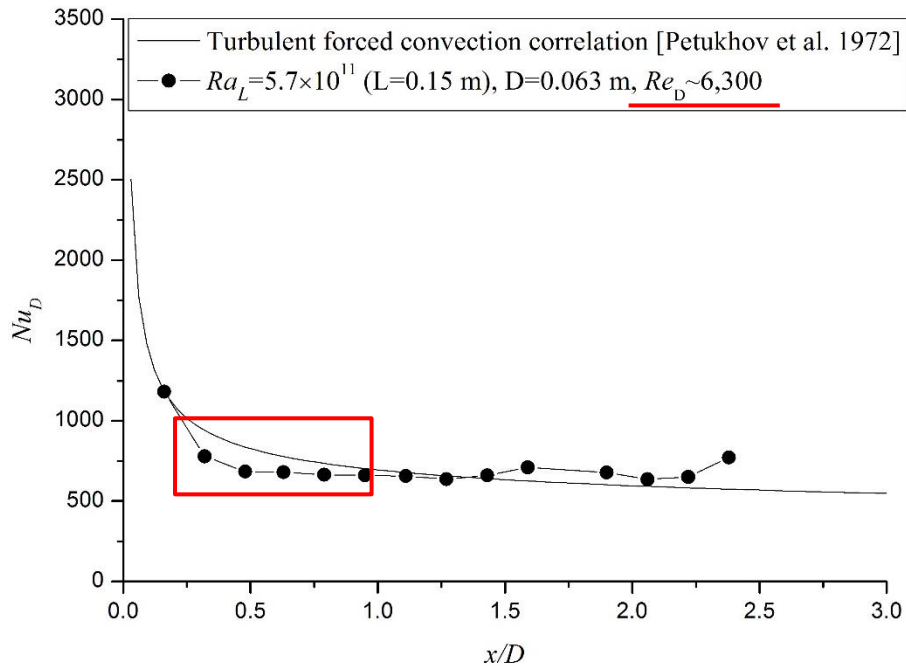
Results : x/D vs. Nu_D (2/4)

- x/D vs. Nu_D (Turbulent flow)



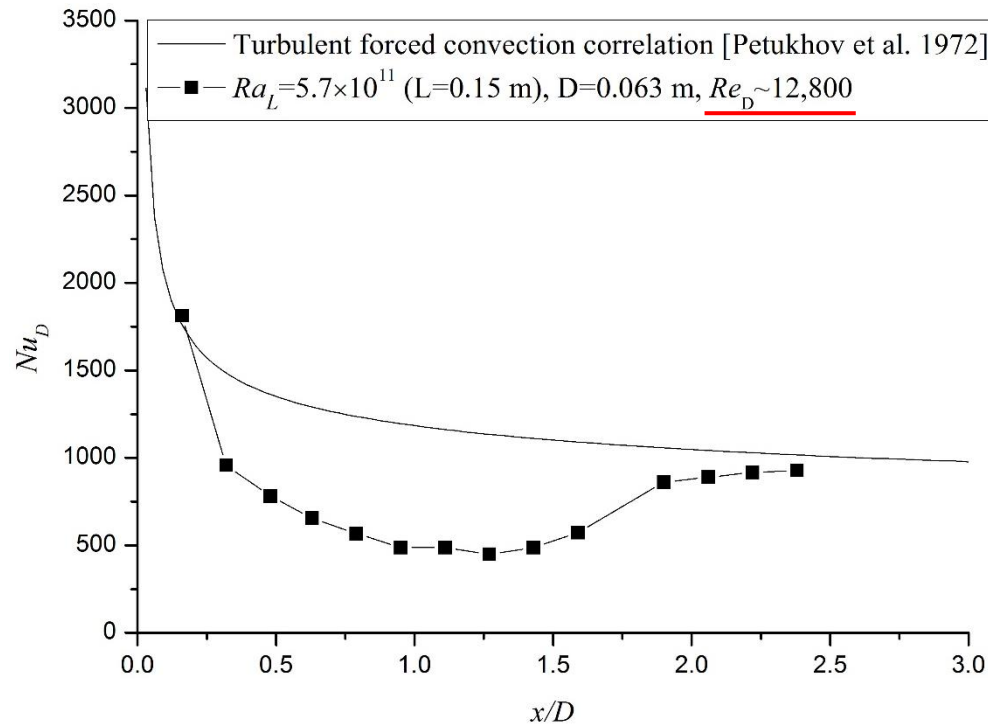
Results : x/D vs. Nu_D (2/4)

- x/D vs. Nu_D (Turbulent flow)



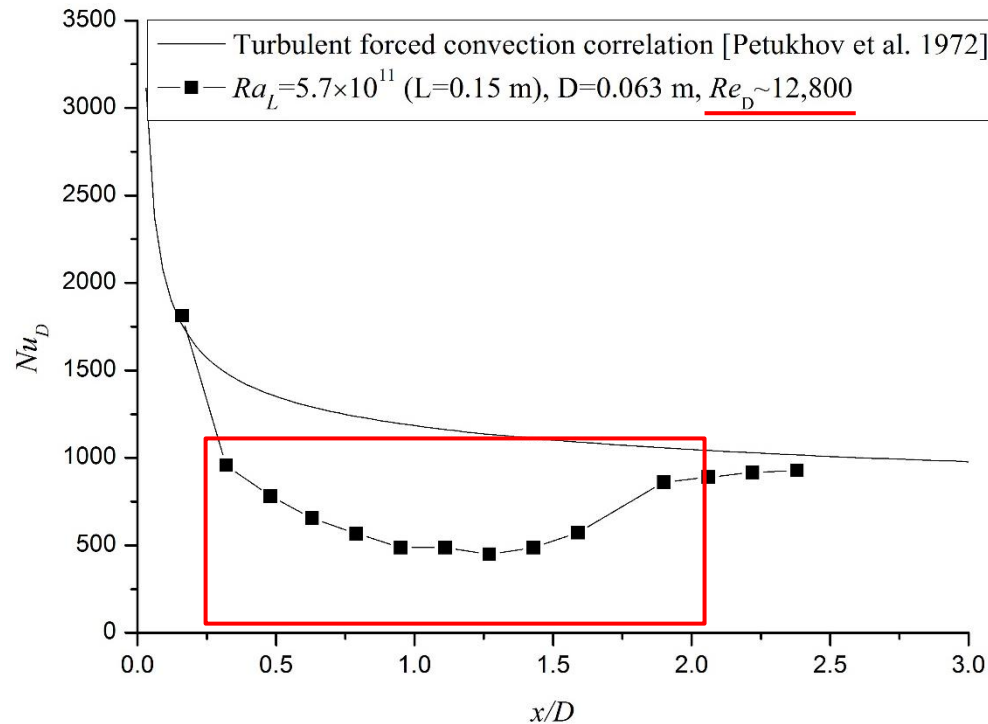
Results : x/D vs. Nu_D (3/4)

- x/D vs. Nu_D (Turbulent flow)



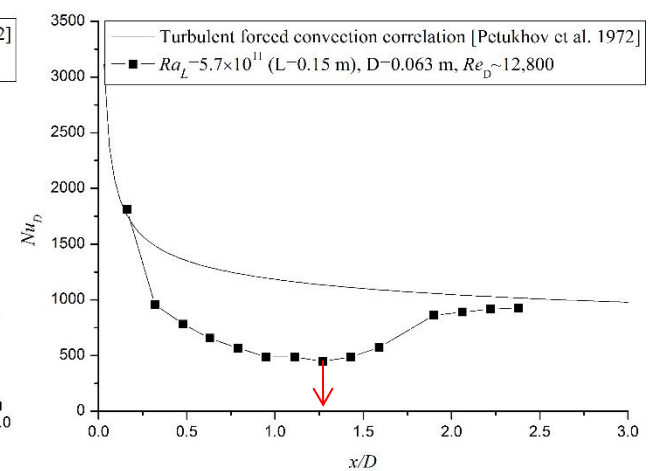
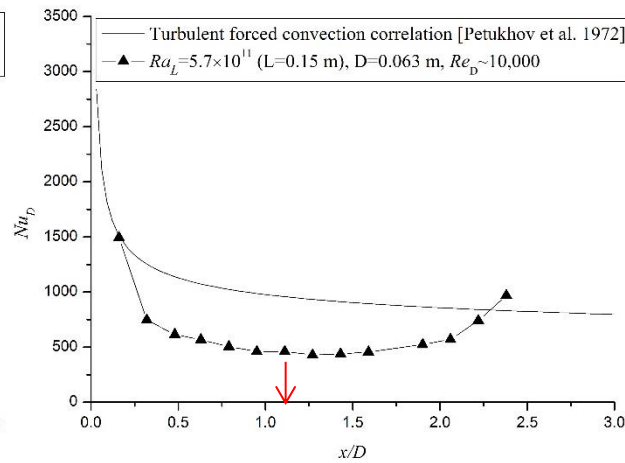
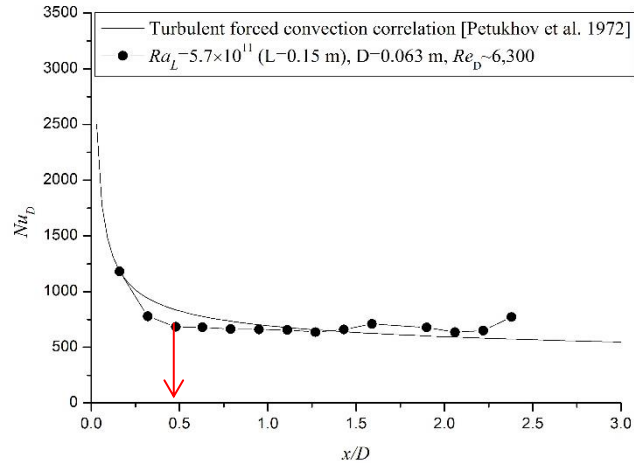
Results : x/D vs. Nu_D (3/4)

- x/D vs. Nu_D (Turbulent flow)



Results : x/D vs. Nu_D (4/4)

- x/D vs. Nu_D (Turbulent flow)



- Increased x/D , Nu_D impaired → **Laminarization**
- Increased x/D , Nu_D recovered or enhanced → **Recovery of turbulence production**
- Minimum $Nu_D - Re \uparrow$, $x/D \uparrow$ (18%, 54%, 56%)

Conclusions

- In the **Passive Cooling System devices, RCCS**, the buoyant flows are induced
 - *The local average Nu of natural convective flow can be impaired due to the mixed convective flow*
- This study measured the **Forced convection and Mixed convection heat transfer in a vertical circular duct** by mass transfer experiment using the analogy concept
 - Test range correspond to the Rayleigh number with NACEF
 - Adopting the Piecewise electrodes, Varying Reynolds number
- Comparison of heat transfer rates existing correlation and present data
 - Present data ($L=0.01\text{m}$) agreed with forced convection correlation (Laminar, Turbulent)
 - Present data ($L=0.15\text{m}$) agreed with mixed convection correlation for of Wragg and Ross



Conclusions

- x/D vs. Nu (Laminar flow)
 - *The local average Nu* : Enhanced compared on the forced convection due to **Velocity increased**
- x/D vs. Nu (Turbulent flow)
 - *The local average Nu* : Impaired compared to the forced convection due to **Laminarization**
 - And then, recovered and enhanced since the **turbulence production**
- This study is design of the test facility and experiments test scope for similarity with NACEF
- Extended the test range for **Reynolds number**, **Diameter** and **Length** of test section
 - Characteristic length of Gr
- The phenomenological analysis will be developed in the heat transfer of mixed convection with **laminarization** and **turbulence production**



Thank you !



Appendix I

