

## Thermophysical properties of liquid UO<sub>2</sub>, ZrO<sub>2</sub> and corium by molecular dynamics and predictive models

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### 1. Introduction

In severe accident of light-water reactors, lava-like molten mixture called corium (compounds of UO<sub>2</sub>, ZrO<sub>2</sub> and Zr) is created due to the radioactive decay and heat of fission. The analysis of such accidents (fate of the melt), requires accurate corium thermophysical properties data up to 5000 K [1]. In addition, the initial corium melt superheat melt, determined from such properties, are key in predicting the fuel-coolant interactions (FCIs) [2] and convection and retention of corium in accident scenarios, e.g., core-melt down corium discharge from reactor pressure vessels and spreading in external core-catcher [3,4]. Due to the high temperatures, data on molten corium and its constituents are limited, so there are much data scatters and mostly extrapolations (even from solid state) have been used [5]. Here we predict the thermophysical properties of molten UO<sub>2</sub> and ZrO<sub>2</sub> using classical molecular dynamics (MD) simulations (properties of corium are predicted using the mixture theories and UO<sub>2</sub> and ZrO<sub>2</sub> properties). The empirical interatomic potential models are critical in accurate MD prediction of the properties, and the molten corium constituent oxides, especially UO<sub>2</sub>, have several models developed for the solid phase(s), each tuned to different bulk properties. We compare the predictions and decipher the differences, compare with theoretical predictive models for these properties, and select the most relevant of these models. The predicted properties are density, heat capacity, compressibility, viscosity, thermal conductivity and surface tension up to 5000 K and their temperature-dependent useful correlations are provided.

### 2. Methods and Results

#### 2.1 Interatomic potential models for UO<sub>2</sub> and ZrO<sub>2</sub>

We used the LAMMPS [6] package for the MD simulations to predict liquid corium properties from atomistic approach. Liquid corium has no

microstructure, so microscopic properties can be the same as the measured macroscopic (bulk) ones. For predicting low symmetry (e.g., liquids) systems efficiently [7] the interatomic potential models have evolved, e.g., reactive force field [8] and 2NN MEAM [9] formalism. To describe the overlap of the atomic orbitals, the embedded-atom method (EAM) [10] for UO<sub>2</sub> and ZrO<sub>2</sub> is proposed by Cooper et al. (CRG) [11,12], while the traditional Buckingham model [13] for ZrO<sub>2</sub> is introduced by De *et al.* (Teter) [14]. The CRG models additionally consider the many-body perturbations to the Buckingham-Morse potentials. It models the coordinate-dependent bonding and violation of the Cauchy relation [15] by the many-body perturbations. The energy of atom *i* surrounded by atom *j* is

$$\varphi_i = \frac{1}{2} \sum_j \phi_{\alpha\beta}(r_{ij}) - G_\alpha \left[ \sum_j \sigma_\beta(r_{ij}) \right]^{\frac{1}{2}}, \quad (1)$$

where  $\alpha$  and  $\beta$  are elements of atoms *i* and *j*. In Eq. (1), The first term combines the short-range pairwise interaction using the Buckingham [13] and Morse [16] potentials and the long-range electrostatic Coulomb interactions, i.e.,

$$\phi_{\alpha\beta}(r_{ij}) = A_{\alpha\beta} \exp\left(-\frac{r_{ij}}{\rho_{\alpha\beta}}\right) - \frac{C_{\alpha\beta}}{r_{ij}^6} + D_{\alpha\beta} \left\{ \exp\left[-2\gamma_{\alpha\beta}(r_{ij}-r_o)\right] - 2 \exp\left[-\gamma_{\alpha\beta}(r_{ij}-r_o)\right] \right\} + \frac{q_\alpha q_\beta}{4\pi\epsilon_0 r_{ij}}. \quad (2)$$

The parameters for the short-range pairwise terms and the ionic charges of the Coulombic terms are listed in Table 1.

	U-U	Zr-Zr	U-O	Zr-O	O-O
$A_{\alpha\beta}$ (eV)	18600	18600	448.779	1147.471	830.283
$\rho_{\alpha\beta}$ (Å)	0.2747	0.23066	0.387758	0.32235	0.352856
$C_{\alpha\beta}$ (eVÅ <sup>6</sup> )	0.0	0.0	0.0	0.0	3.884372
$D_{\alpha\beta}$ (eV)	-	-	0.66080	1.2269	-
$\gamma_{\alpha\beta}$ (Å <sup>-1</sup> )	-	-	2.05815	1.4482	-
$r_o$ (Å <sup>-1</sup> )	-	-	2.38051	1.998	-
$q_U$ (e)	+2.2208				
$q_Zr$ (e)	+2.2208				

$q_o(e)$  -1.1104

The second term is a subtle many-body perturbation from the surrounding ions in the EAM formalism and was originally expressed as an approximate function of the electron density functional theory (DFT) for metals [17], with a mathematical analogy to the ionic systems [18], and is

$$\sigma_{\beta}(r_{ij}) = \left(\frac{n_{\beta}}{r_{ij}^{\delta}}\right) \frac{1}{2} \{1 + \text{erf}[20(r_{ij}-1.5)]\}, \quad (3)$$

where  $G_{\alpha}$  is embedding function or energy and  $\sigma_{\beta}$  is a set of pairwise functions. The error function prevents unrealistic dynamics when atoms are very close. The parameters for this many-body terms are listed in Table 2.

Table 2. Parameters of the many-body interactions in the CRG models [11,12].

	U	Zr	O
$G_{\alpha}$ (eV $\text{\AA}^{-1.5}$ )	1.806	1.597	3450.995
$n_{\beta}$ ( $\text{\AA}^5$ )	0.690	1188.786	106.856

The Teter potential describes the interaction for  $\text{ZrO}_2$  using the short-range Buckingham potential model with the long-range Coulombic interaction.

$$\phi_{\alpha\beta}(r_{ij}) = A_{\alpha\beta} \exp\left(-\frac{r_{ij}}{\rho_{\alpha\beta}}\right) - \frac{C_{\alpha\beta}}{r_{ij}^6} + \frac{q_{\alpha}q_{\beta}}{4\pi\epsilon_0 r_{ij}} \quad (4)$$

	Zr-O	O-O
$A_{\alpha\beta}$ (eV)	7747.1834	2029.2204
$\rho_{\alpha\beta}$ ( $\text{\AA}$ )	0.252623	0.343645
$C_{\alpha\beta}$ (eV $\text{\AA}^6$ )	93.109	192.58
$q_U$ (e)	+2.4	
$q_O$ (e)	-1.2	

Table 3. Parameters of the Buckingham potentials for the Teter model [14], and related ionic charges in the Coulombic interactions.

## 2.2 Melting procedure

The  $\text{UO}_2$  and  $\text{ZrO}_2$  systems are fluorite crystals and are first melted at very high temperatures (around 5000 K) under the  $NPT$  ensemble for 20 ps with periodic boundary conditions (PBC) and 12000 atoms. The Nose-Hoover thermostat [25,26] and the Parrinello-Rahman barostat [27] are used for controlling temperature and pressure. The liquid state is verified from the atomic structure, trajectories of atoms and the radial distribution function (RDF). Figure 1 show snapshots using OVITO [28] and radial distribution functions for liquid  $\text{UO}_2$  and  $\text{ZrO}_2$  at 4000 K.

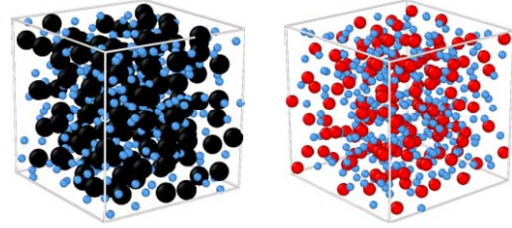


Fig.1. Atomic structures for liquid (a)  $\text{UO}_2$  (left) and  $\text{ZrO}_2$  (right) at 4000K, showing liquid state. Black, red and blue spheres denote U, Zr and O atoms.

## 2.3 Density

Densities of liquid  $\text{UO}_2$  (black squares) and  $\text{ZrO}_2$  (red squares) depending on are predicted by MD simulations using the CRG potential model (Fig. 6). Temperature range of prediction is from near the melting point (3200 K for  $\text{UO}_2$  and 3000K for  $\text{ZrO}_2$ ) to 5000 K.

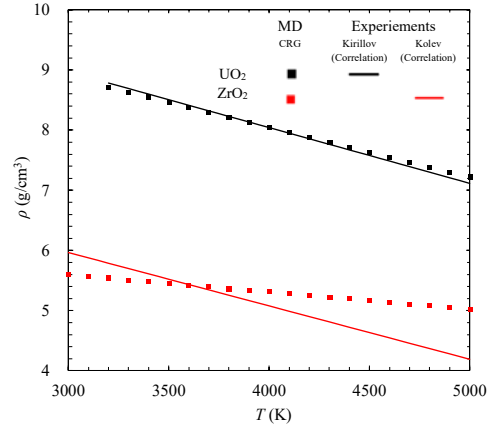


Fig. 2. Variations of MD predicted liquid  $\text{UO}_2$  and  $\text{ZrO}_2$  density with temperature, using the CRG potential model and comparison with experiments

## 2.4 Heat capacity

Heat capacity of liquid  $\text{UO}_2$  and  $\text{ZrO}_2$  are predicted. In MD simulations, heat capacity is attained from total energy slope, which can be calculated with increasing system temperature up to 5000K. Predicted heat capacities are compared with reported experimental result for both  $\text{UO}_2$  and  $\text{ZrO}_2$ . Heat capacity for  $\text{ZrO}_2$  is proposed to 815 J/kg-K as the constant.

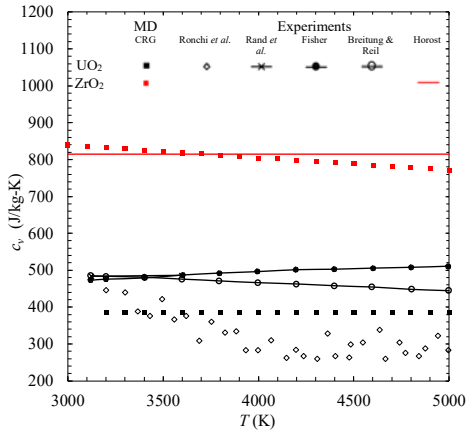


Fig. 3. Variations of MD predicted of liquid UO<sub>2</sub> and ZrO<sub>2</sub> specific heat at constant volume with temperature, and comparison with experimental results.

### 2.5 Isothermal compressibility

Isothermal compressibility of liquid UO<sub>2</sub> and ZrO<sub>2</sub> are predicted by equilibrium MD simulations using the CRG and the Teter potentials. In the MD simulations, isothermal compressibility is attained from the volume fluctuation under NPT ensemble, i.e.,

$$\langle \delta V^2 \rangle_{NPT} = \kappa V k_B T, \quad (5)$$

where  $\kappa, V, k_B$  and  $T$  are compressibility, volume of the system, Boltzman constant and temperature respectively.  $\langle \delta V^2 \rangle$  denotes averaging value with time.

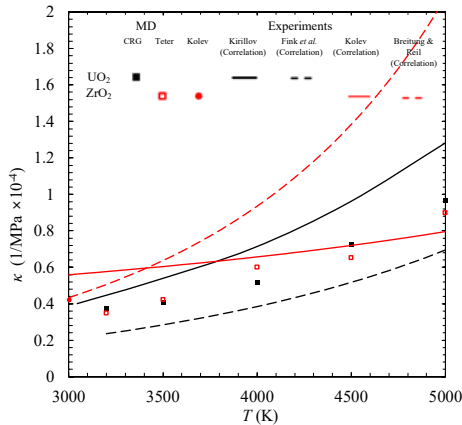


Fig. 4. Variations of MD predicted liquid ZrO<sub>2</sub> compressibility with temperature, using two different sets of interatomic potential models, and comparison with experiments.

### 2.6 Viscosity

Based on Green-Kubo formula explained in section 4.1.1, viscosity of liquid UO<sub>2</sub> (black squares) and ZrO<sub>2</sub> (red squares) are predicted by MD simulations (see Fig. 5.). Size effect is checked negligible in overall systems on applying Green-Kubo formula for viscosity. Predicted viscosities are compared to reported experimental result and predictive Andrade model

(solid lines). Andrade models shows good agreement with MD simulation results for both UO<sub>2</sub> and ZrO<sub>2</sub>.

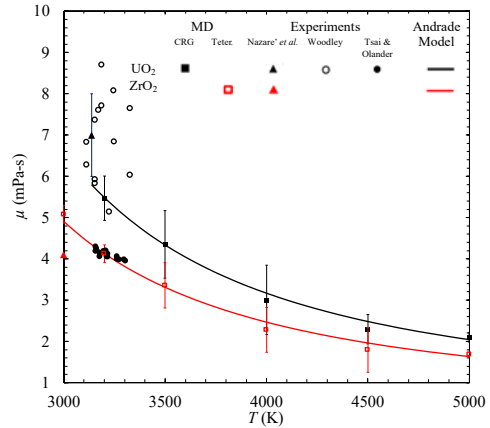


Fig. 5. Variations of MD predicted liquid UO<sub>2</sub> and ZrO<sub>2</sub> viscosity with temperature, and comparison with experiments and with predictive model.

Figure 6 shows viscosity of liquid UO<sub>2</sub>-ZrO<sub>2</sub> mixture (corium) depending on temperature and compositions. Blending equation is applied for Andrade models for UO<sub>2</sub> and ZrO<sub>2</sub>

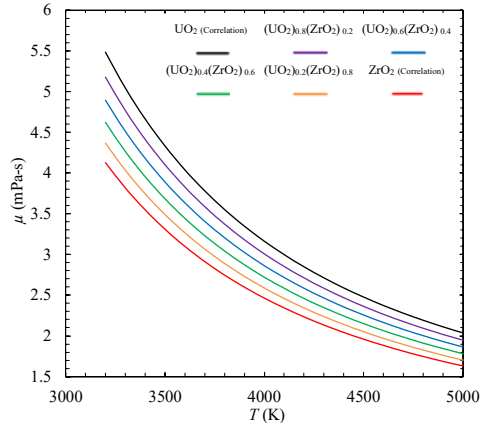


Fig. 6. Variations of liquid UO<sub>2</sub>-ZrO<sub>2</sub> mixture (corium) viscosity with temperature, and for several compositions

### 2.7 Surface tension

Surface tension of liquid UO<sub>2</sub> is predicted by MD simulation. Surface tension is obtained using methodology explained in Eq. (32) in section 5.1. Temperature dependence of surface tension by MD simulations (black squares) is shown in Fig. 18 with experiments (black solid line). Predicted UO<sub>2</sub> surface tension have nearly same values and trends with experimental relation.

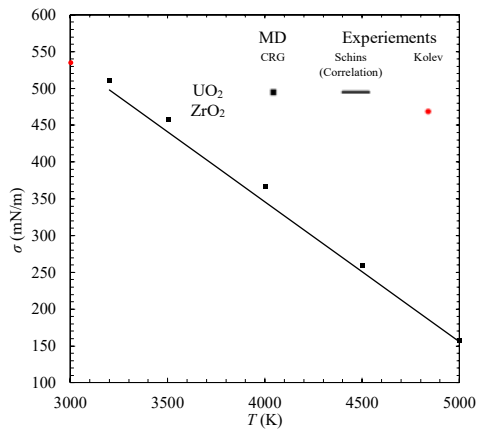


Fig. 6. Variations of MD predicted liquid  $\text{UO}_2$  surface tension with temperature, and comparison with experiments ( $\text{UO}_2$  and  $\text{ZrO}_2$ ).

### 3. Conclusions

The thermophysical properties (density, compressibility, heat capacity, viscosity and surface tension) of liquid  $\text{UO}_2$  and  $\text{ZrO}_2$  are predicted using classical molecular dynamics simulations, up to 5000 K. For atomic interactions, the CRG and the Teter potential models are found most appropriate. The liquid behavior is verified with the random motion of the constituent atoms and the pair-distribution functions, starting with the solid phase and raising the temperature to realize liquid phase. The viscosity and thermal conductivity are calculated with the Green-Kubo autocorrelation decay formulae and compared with the predictive models of Andrade and Bridgman. For liquid  $\text{UO}_2$ , the CRG model gives satisfactory MD predictions. For  $\text{ZrO}_2$ , the density is reliably predicted with the CRG potential model, while the compressibility and viscosity are more accurately predicted by the Teter model. The surface tension for  $\text{UO}_2$  is reasonably predicted compared to experimental results, whereas the predicted  $\text{ZrO}_2$  results by the CRG and the Teter models do not appear reasonable. Newly proposed temperature-dependent correlations for liquid  $\text{UO}_2$  and  $\text{ZrO}_2$  and corium density, compressibility, heat capacity, viscosity, surface tension, and thermal conductivity are provided in Table 5.

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