# An Assessment of Uncertainty for a Head End Process in the Pyroprocessing <br> Wonjong Song, Hoyoung Shin, Myeonghyeon Woo, and Moosung JAE' <br> Department of Nuclear Engineering, Hanyang University, Seoul, 04763, Korea <br> *Corresponding author: jae@hanyang.ac.kr 

## 1. Introduction

- Korea has been developing the pyroprocessing that changes spent fuels of a LWR to fresh fuels of a SFR.
- In the pyroprocessing, a non-destructive analysis, like a ( $\mathrm{Pu} /{ }^{244} \mathrm{Cm}$ ) mass ratio method showed in Eq. (1), is usually used because nuclear material accountancy is controlled by weight unit.
- Heterogeneous $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio of spent fuel rods appears by height when a fuel assembly are burned.
- In this study, we analyzed the heterogeneous the $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio by height of spent fuels according to burnup and cooling periods based on computer simulations, and calculated a uncertainty of the $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio in a head process of the pyroprocessing by random samplings

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\begin{equation*}
\text { Pu mass }=\left(\frac{\text { Pu mass }}{{ }^{244} \mathrm{Cm} \text { mass }}\right) \times{ }^{244} \mathrm{Cm} \text { mass } \tag{1}
\end{equation*}
$$

## 2. Methods and Results

### 2.1 Reference Reactor

- OPR1000 was selected as a type of reference reactor.
- By analyzing the nuclear design report of OPR1000, we found core design characteristics and selected typical 3 fuel assemblies which are shown in table 1.

Table 1. Information of typical fuel assemblies

| Fuel assembly type | Enrichment <br> $\left[{ }^{[ } \%{ }^{235} \mathrm{U}\right]$ | Burnup <br> $[\mathrm{MWd} / \mathrm{kgU}]$ | Number of <br> fuel rods |
| :---: | :---: | :---: | :---: |
| A0 | 1.42 | $11.6 \sim 14.2$ | 236 |
| B0 | $2.92 / 2.42$ | $37.1 \sim 39.7$ | $\mathbf{1 8 4 / 5 2}$ |
| C0 | $3.43 / 2.93$ | $33.8 \sim 4.1$ | $\mathbf{1 8 4 / 5 2}$ |

### 2.2 Computer codes

- MCNP based on Monte Carlo method is a particle transport analysis code that generates random numbers to describe behavior of particles and estimate a solution of the Boltzmann transport equation.
- CINDER`90 performs a reactor irradiation calculation and solves the Bateman equation to track nuclide change in materials.
- A link system was used to simulate the fuel assembly burnup calculations between MCNP and CINDER` 90 showed in figure 1.
- In the link system, Predictor-Corrector method was used which calculates a ratio of nuclide at the midpoint of each time step to mitigate a oscillation of neutron flux by ${ }^{135} \mathrm{Xe}$.


Figure 1. Link system between MCNP and CINDER'90

### 2.3 Input file for the computer codes

- To find out the heterogeneous $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio by height of the fuel assembly, middle burnup region was divided into long meshes, and end burnup regions were divided into short meshes
- The burnup periods were set to 400, 500, 600, 700, and 800 days, and the cooling periods were set to $0,10,20,30$, and 40 years.
2.4 Heterogeneous results by height of the fuel assembly
- As a result of the fuel assembly burnup process, heterogeneous results by height appeared for 4 fuel assemblies showed in figure 2.
- The lower the enrichment, the smaller the average $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio and the greater the $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio difference.


Figure 2. ( $\mathrm{Pu} /{ }^{244} \mathrm{Cm}$ ) mass ratio results of each fuel assembly

### 2.5 Uncertainty analysis using 1,000 random samplings

- We assumed that a fuel assembly is divided into 89,916 pellets in the chopping step, and 9,144 pellets are randomly selected to be oxidized corresponding to $50 \mathrm{kgHM} /$ batch.
- Random samplings of selecting 9,144 pellets out of 89,916 pellets were conducted 1,000 showed in figure 3.
- Uniform probability mass function was used for random samplings.
- Error propagation was used times to calculate uncertainty of the $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio.


Figure 3. Random samplings using uniform PMF

Table 2. Uncertainty of the ( $\mathrm{Pu} / 244 \mathrm{Cm}$ ) mass ratio by random samplings

| Fuel assemb -ly | Cooling <br> Period [yr] | Burnup period [days] |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 400 |  | 500 |  | 600 |  | 700 |  | 800 |  |
|  |  | ratio | SD | ratio | SD | ratio | SD | ratio | SD | ratio | SD |
| A0 | 0 | 1212.8 | 7.8 | 560.8 | 3.4 | 310.4 | 1.7 | 190.2 | 1.0 | 128.5 | 0.6 |
|  | 10 | 1723.3 | 11.4 | 793.3 | 4.6 | 438.0 | 2.4 | 267.9 | 1.4 | 180.8 | 0.9 |
|  | 20 | 2454.8 | 17.1 | 1128.3 | 6.8 | 621.4 | 3.2 | 379.9 | 1.9 | 256.0 | 1.2 |
|  | 30 | 3538.0 | 22.8 | 1621.4 | 9.9 | 890.9 | 4.9 | 544.8 | 2.8 | 367.2 | 1.9 |
|  | 40 | 5126.4 | 31.9 | 2345.8 | 13.9 | 1288.8 | 7.0 | 787.0 | 4.1 | 530.3 | 2.7 |
| B0 | 0 | 5922.0 | 33.2 | 2296.4 | 11.6 | 1092.6 | 5.2 | 599.2 | 2.7 | 363.5 | 1.5 |
|  | 10 | 8467.1 | 47.1 | 3262.6 | 16.2 | 1544.8 | 7.4 | 844.3 | 3.6 | 510.4 | 2.2 |
|  | 20 | 12137.3 | 66.0 | 4659.4 | 23.6 | 2199.1 | 10.5 | 1199.0 | 5.5 | 724.0 | 3.0 |
|  | 30 | 17553.6 | 90.3 | 6718.7 | 33.7 | 3164.0 | 14.9 | 1722.4 | 7.7 | 1037.8 | 4.3 |
|  | 40 | 25503.9 | 137.3 | 9747.9 | 48.7 | 4581.0 | 21.4 | 2491.4 | 11.5 | 1500.7 | 6.5 |
| C0 | 0 | 8743.4 | 46.7 | 3351.2 | 16.6 | 1564.0 | 7.6 | 846.0 | 3.7 | 501.3 | 2.1 |
|  | 10 | 12528.6 | 67.4 | 4772.6 | 23.4 | 2213.8 | 10.6 | 1193.9 | 5.4 | 705.0 | 3.1 |
|  | 20 | 18009.0 | 96.2 | 6829.9 | 33.6 | 3156.8 | 15.0 | 1697.3 | 7.4 | 999.8 | 4.3 |
|  | 30 | 26049.2 | 140.4 | 9852.1 | 49.1 | 4545.8 | 21.8 | 2439.2 | 10.8 | 1434.5 | 6.1 |
|  | 40 | 37894.6 | 202.8 | 14297.8 | 73.9 | 6590.0 | 31.6 | 3530.3 | 15.7 | 2074.7 | 8.9 |

## 3. Conclusion

- It is confirmed that the heterogeneous $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio appears in the spent fuel assemblies.
- Uncertainty of the $\left(\mathrm{Pu} /{ }^{244} \mathrm{Cm}\right)$ mass ratio was calculated by the 1,000 random samplings using uniform probability mass function.
- A methodology of this study could be used to enhance accuracy of the nuclear material accountancy.

