# Study of Condensation Heat Transfer and Pressure drop of CO2 near the critical point

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### 1. Introduction

A supercritical carbon dioxide (S-CO<sub>2</sub>) cycle has many advantages such as a high thermal efficiency at relatively low temperature, compactness of major components, and a simple layout. Those merits are come from its low compressing work by pressurizing the CO<sub>2</sub> near the critical point, which the cycle reduces the compressing work due to its high density and low compressibility at that point [1-4]. However, this design point close to the critical point or under the critical point for a trans-critical cycle case would cause the system operating condition to be under two-phase conditions during off-design or on-design operating conditions [5].

To analyze the  $CO_2$  condensation for S-CO<sub>2</sub> cycles, the appropriate condensation heat transfer and wall frictional loss models are necessary. Thus, in this study, several condensation models were evaluated from the literature which performed the studies related with  $CO_2$ condensation.

The experiment for the CO<sub>2</sub> two-phase flow were performed with the CO<sub>2</sub> pressurizing and heat transfer test loop in KAIST called SCO2PE (Supercritical CO<sub>2</sub> Pressurizing Experiment) in this study. The heat transfer experiments were carried out with the PCHE (Printed Circuit Heat Exchanger) type pre-cooler of the facility. The pressure drop test section is the pipe, having 1 1/2'' inner diameter, between the PCHE and the compressor of SCO2PE loop. The experiment range is from 26.4 to 27.5, 6.65 to 6.82 MPa and the mass flux was 880 kg/m<sup>2</sup> s.

### 2. Test facility review

### 2.1 Heat transfer test section

The heat transfer test was performed with the PCHE designed with 896 channels having a 1.8mm diameter on each side [6]. The PCHE geometry information are shown in Figs. 1 and 2, respectively the overall view and the schematic diagram of the PCHE of SCO2PE [6]. The size of the PCHE is 200mm x 99.2mm x 84mm and it is composed of semi-circular zigzag flow channels. Each plate has 1.5mm thickness and 0.75mm minimum thickness and made by SS316L.



Fig. 1. The PCHE of SCO2PE facility. [6]



Fig. 2. The schematic diagram of the PCHE of SCO2PE facility [6]

The test section of the pressure drop experiment was the pipe, having  $1 \frac{1}{2}$  inner diameter, which connects the PCHE and the compressor of SCO2PE. The overall view and schematic diagram of the test section are shown in Fig. 3. For modeling the test section, the authors assumed the pipe roughness to be  $45 \times 10^{-6}$  m and 0.7 form loss coefficient at each standard 90° elbow.



Fig. 3. The overall view and schematic diagram of the test section for the pressure drop test

# 3. Evaluation of heat transfer and pressure drop models for CO<sub>2</sub> two-phase conditions

## 2.1 Heat transfer model evaluation

Five heat transfer correlations were evaluated, Dittus-Boelter [7] as a reference, the PCHE correlation by S. Baik [6], Shah's correlation [8], Thome's correlation [9] and Holaman correlation [10]. The heat transfer correlations are showed in Table I. Fig. 4 represents the comparison between the measured data and the predictions from the five heat transfer correlations. The methods of Baik and Shah predicted the results with higher accuracies compared the experimental data within about -5%. The Dittus-Boelter correlation also gives good performance within about -10% gaps.

evaluated in this study.		
Heat transfer correlations		
Author(s)	Methods	
Thome	$h = \frac{\lambda_l}{D_h} 0.003 R e_l^{0.74} P r_l^{0.5} f_l$	
Holaman	$h = 0.725 \left[ \frac{\rho_l (\rho_l - \rho_g) g h_{lg} k_l^3}{D_h \mu_l (T_{sat} - T_w)} \right]^{\frac{1}{4}}$	
Shah	$h = h_{sf} \left( 1 + \frac{3.8}{Z^{0.95}} \right)$	
Baik	$Nu = 0.8405 R e^{0.5704} Pr^{1.08}$	
Dittus-Boelter	$Nu = 0.023 Re^{0.8} Pr^{0.4}$	

Table I: The lists of the heat transfer correlations



Fig. 4. The comparison results of the measured and predicted heat transfer according to the heat transfer correlations

### 2.2 Pressure drop model evaluation

To select the appropriate correlation for the pressure drop in  $CO_2$  two-phase flow, hree wall frictional loss models, Friedel [11], Müller-Steinhagen and Heck [12], Churchill [13] models, were compared with the experimental data from SCO2PE. Table II shows the lists of the pressure drop correlations for the  $CO_2$  twophase flow evaluated in this study. The comparison

16

results for the pressure drop during the  $CO_2$  two-phase flows in the test section are shown in Fig. 5. As a result, the model of Müller-Steinhagen and Heck gives the best agreement within about 30% gaps, outperforming the other methods.

Table II: 7	The lists of the pressure drop correlations	
evaluated in this study.		

Pressure drop correlations		
Author(s)	Methods	
	$\left(\frac{dP}{dx}\right)_{f,tp} = \beta (1-x)^{1/3} + Bx^3$	
Müller- Steinhagen and Heck	$\beta = A + 2(B - A)x$	
	$\left(\frac{dP}{dx}\right)_f = f_f \frac{G^2}{2\rho_f D_h} = A$	
	$\left(\frac{dP}{dx}\right)_g = f_g \frac{G^2}{2\rho_g D_h} = B$	
Churchill	$f_{Lo} = 8 \left[ \left( \frac{8}{R e_{Lo}} \right)^{12} + \frac{1}{(A+B)^2} \right]^{\frac{1}{12}}$	
	$A = \left\{-2.457 \ln \left[\left(\frac{7}{\text{Re}_{\text{Lo}}}\right)^{0.9} + 0.27 \frac{\epsilon}{D_{\text{h}}}\right]\right\}$	
	$\mathbf{B} = \left(\frac{37530}{\mathrm{Re}_{\mathrm{Lo}}}\right)^{16}$	
	$\varphi^2 = \left(\frac{1-x}{1-\alpha}\right)^{1.75}$	
Friedel	$f_{Lo} = \frac{0.316}{R e_{Lo}^{0.25}}$	



Fig. 5. The comparison results of the measured and predicted pressure drop according to the pressure drop correlations

#### 3. Conclusions

In this study, several heat transfer and pressure drop models were investigated and evaluated with the experimental data near the critical point of  $CO_2$  from SCO2PE facility in KAIST.

As comparison results of the several previously suggested models, the heat transfer correlation of Baik's study and the wall frictional method of M  $\ddot{\mathbf{u}}$  ller-Steinhagen and Heck showed the best-performances in this region. The interesting thing is that the Baik's correlation gives the best fit of the CO<sub>2</sub> two-phase flow data even if it was originally developed and evaluated under CO<sub>2</sub> single-phase conditions. It means that the two-phase conditions of CO<sub>2</sub> near the critical point would be not much different in CO<sub>2</sub> single-phase condition in terms of heat transfer.

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