

Requirement for Seismic PSA Quantification. Software under Development in KAERI

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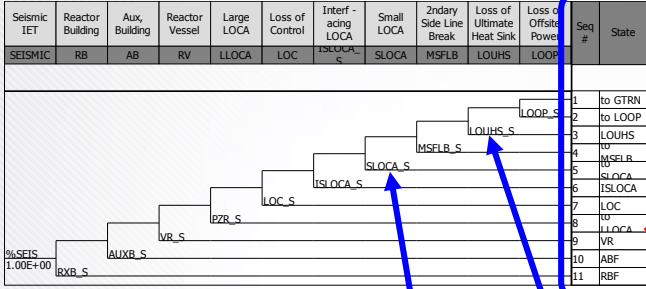
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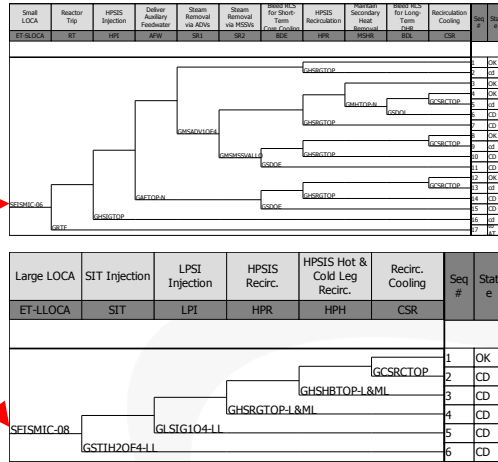
1. 개요 - Seismic PSA 절차

Seismic Initiating Event Analysis

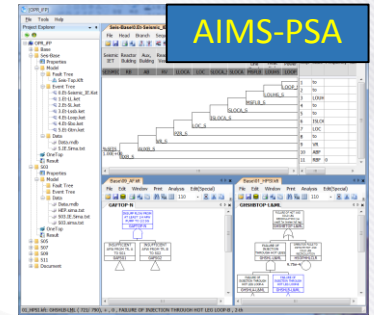
- Seismic Induced IE Analysis



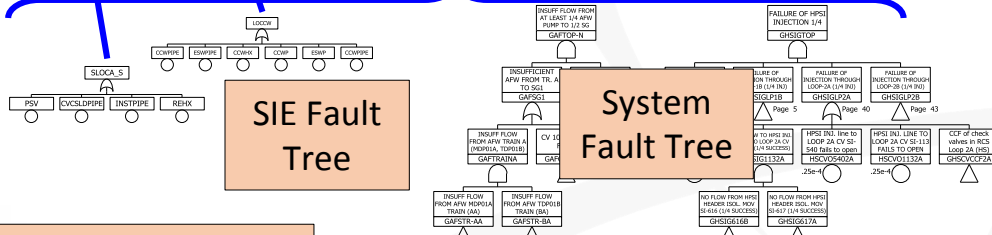
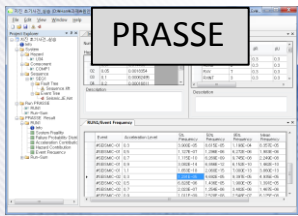
Event Tree for each Seismic IE



Quantification



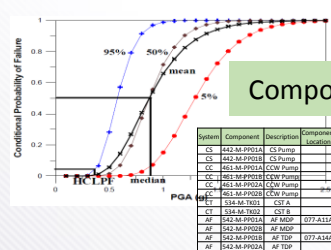
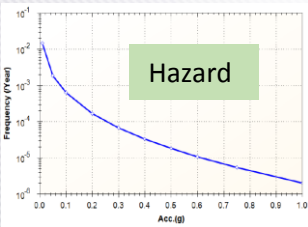
Seismic Initiating Event Analysis



SIE Fault Tree

System Fault Tree

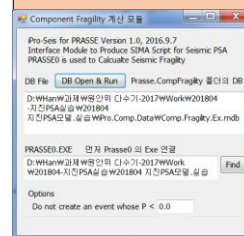
Seismic Hazard & Fragility Data



Component Fragility

System	Component	Description	Component Fragility	Mapping	Acc	Br	Br	HCLPF	SeismicEvent	ContributionLevel
CS	RA2-M-PHSA	CS Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CS	RA2-M-PS2A	CS Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2B	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2C	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2D	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2E	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2F	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2G	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2H	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2I	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2J	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2K	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2L	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2M	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2N	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2O	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2P	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2Q	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2R	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2S	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2T	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2U	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2V	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2W	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2X	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2Y	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL
CC	RA2-M-PS2Z	CCW Pump	COMPRESSOR	2.00E+03	0.1	0.05	0.05	0.05	SS_COMPRESSOR	SS_COMPR-ALL

Component Failure Proba.



FTREX



FTeMC

Fragility Function & Correlation

- **Ground Acceleration Capacity, A, is given by:**

- $A = A_m e_R e_U$
- e_R, e_U : random variables
 - median = 1.0, logarithmic standard deviations of β_U and β_R
- A_m : Median
- β_U : Inherent randomness (also known as *aleatory uncertainty*)
- β_R : the state of knowledge uncertainty (also known as *epistemic uncertainty*)

- **Conditional probability of failure, f_0 , for a given PGA level, a**

- $f' = P(A < a)$, (Capacity < Response)
 - $f' = \Phi\left(\frac{\ln\left(\frac{a}{A_m}\right) + \beta_U \Phi^{-1}(Q)}{\beta_R}\right)$ with Q uncertainty level, or
 - $f' = \Phi\left(\frac{\ln\left(\frac{a}{A_m}\right)}{\beta_C}\right)$, with composite uncertainty $\beta_C = (\beta_R^2 + \beta_U^2)^{1/2}$
 - $\Phi(\cdot)$: the standard Gaussian cumulative distribution function

A	B	C	D
PGA	Am	Bc	Fail.Proba
0.7	1.5	0.4	=NORMSDIST(LN(A2/B2)/C2)

- **Correlation Coefficient**

- Correlation between 2 Variables
- $\rho = \frac{\sum((x_i - \bar{x})(y_i - \bar{y}))}{(\sqrt{\sum(x_i - \bar{x})^2} \sqrt{\sum(y_i - \bar{y})^2})}$

Correlation Matrix			
	A	B	C
A	1		
B	0.5	1	
C	0.5	0.5	1

2. Seismic PSA 정량화 S/W 기본 요건

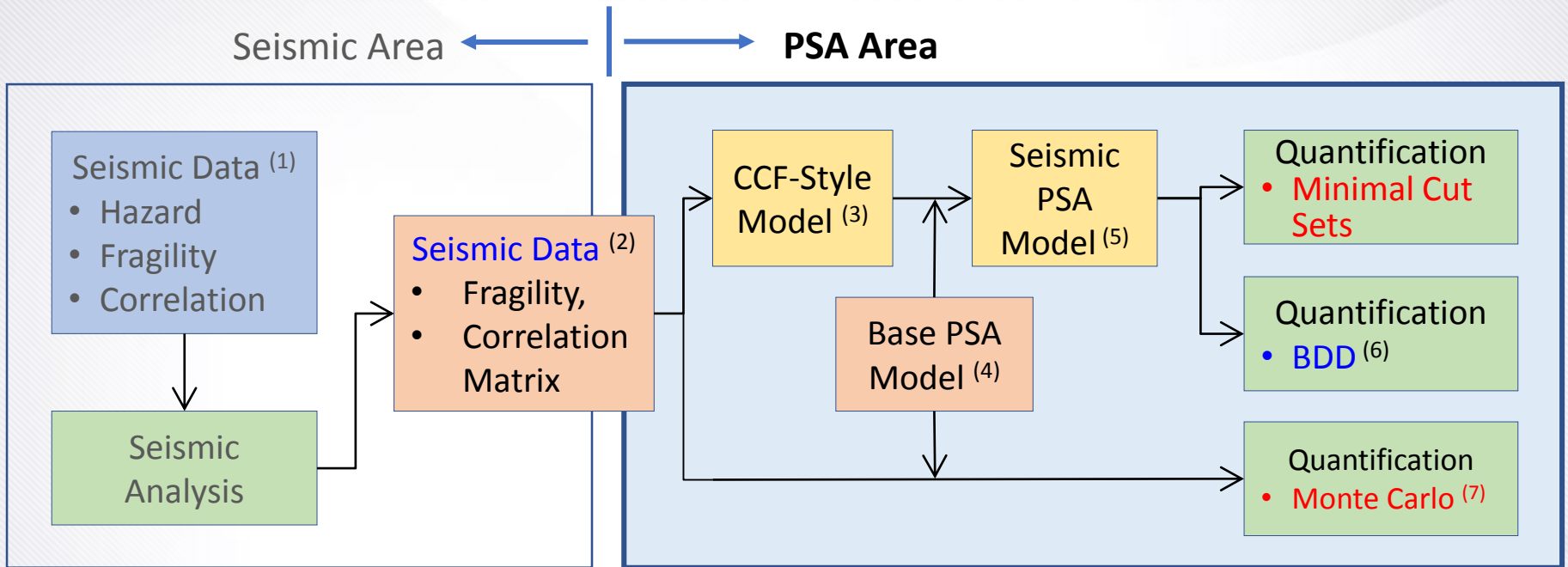
■ Seismic PSA 정량화 S/W 기본 요건

- Seismic Failure
 - Seismic Hazard / Fragility / Correlation
- 리스크 정량화
 - 리스크 평가 (Total, 주요 시나리오별, 다수기 시나리오)
 - Uncertainty, Importance 평가

■ 2 Approaches

- Traditional PSA + CCF-Style Approach
 - Cut Set Approach
 - (BDD Approach)
- Monte Carlo Approach
 - Cut Set Approach 의 결과 검증

Seismic PSA 정량화 S/W 구성



Note)

- 1) 다양한 입력 양식 허용 (SSMRP, Reed-McCann, ...)
- 2) Am, Br, Bu + Correlation Matrix (Br, Bu) 형태로 정리 (하나의 입력을 모든 경우에 활용)
- 3) 각 seismic correlation group 을 CCF-Style Fault Tree 로 변환
- 4) Seismic failure data 가 포함되지 않은 Base PSA model.
- 5) Base PSA Model + CCF-style fault trees → seismic PSA model
- 6) 소규모 모델에 대해 BDD 해석
- 7) Fault Tree Evaluation using Monte Carlo simulation (FTeMC)

Seismic Data 요건 / 입력 정보

■ 요건

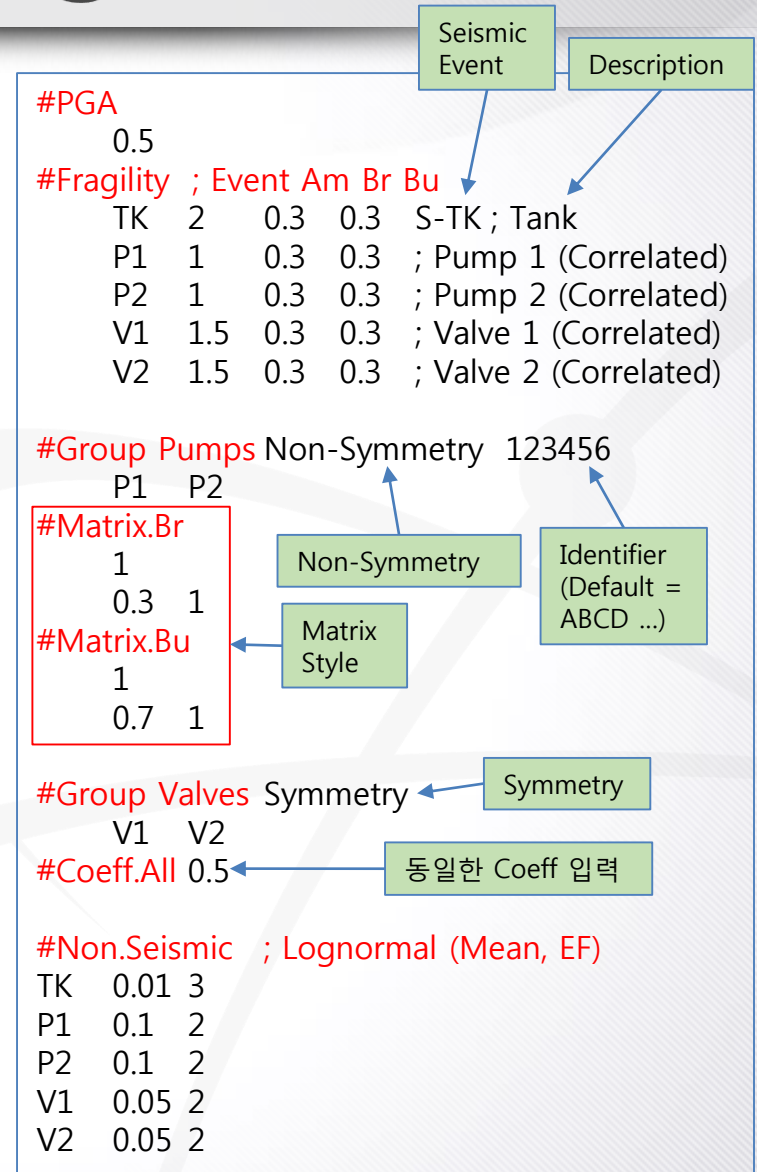
- 통일된 Seismic Data 입력
- Failure Probability 계산
- CCF Model 생성
- Seismic Event Mapping 처리
- Uncertainty Analysis

■ Seismic Data

- PGA
- Fragility
 - Am, Br, Bu
- Correlation Group
 - Group 에 속하는 Event 목록
 - Br, Bu 에 대한 Correlation Coefficient

■ Non-Seismic Data

- Distribution for Uncertainty Analysis



3. 기본 계산 모듈 개발

- Correlated Monte Carlo Technique
- CCF-Style Fault Tree 생성 (최대 12 Comp)

Calculate Capacity C_i for each component

- $r_i \leftarrow U(0,1)$ ' Uniform Random Number
- $X_i \leftarrow \Phi^{-1}(r_i)$ ' Inverse Normal
- $Z_i = M X_i$ ' Incorporate Correlation
 - $M M^T = \Sigma$
 - $M = \Sigma^{1/2}$: Result of Cholesky Decomposition
 - Σ : Coefficient Matrix
- $C_i \leftarrow Am_i \exp(Z_i \beta c_i)$ ' Capacity C_i
 - Am_i : Median Capacity
 - βc_i : Composite Uncertainty

Determine the State of each component

- If $(C_i < PGA)$ then $S_i = \text{True}$, Else $S_i = \text{False}$

Seismic PSA Support Calculator Rev. β (Developed by KAERI, 2019.5.2)

of Comp= 3 pga= 0.6 , Trial #= 1000000 Monte Carlo

Data	Am	Br	Bu
A	1.0	0.3	0.3
B	1.0	0.3	0.3
C	1.0	0.3	0.3

Br : Set All $\rho = 0.5$

Corr.	Br
1	
0.5	1
0.5	0.5 1

Bu : Set All $\rho = 0.5$

Corr.	Bu
1	
0.5	1
0.5	0.5 1
0.5	0.5 0.5 1

Non-Symmetry Symmetry

	Combin	P(OR)	P(AND)	P(Only)	P(CCF)
1	A	0.11447	0.11447	0.055561	0.0685028
2	B	0.113719	0.113719	0.054978	0.0678327
3	C	0.114295	0.114295	0.055384	0.0682994
4	AB	0.1891	0.039089	0.01965	0.0176209
5	AC	0.189506	0.039259	0.01982	0.0177675
6	BC	0.188923	0.039091	0.019652	0.0176411
7	ABC	0.244484	0.019439	0.019439	0.0147912

of Combination = 7 (3 Components)
0.92 sec for Monte Carlo simulation ---

FModel -----

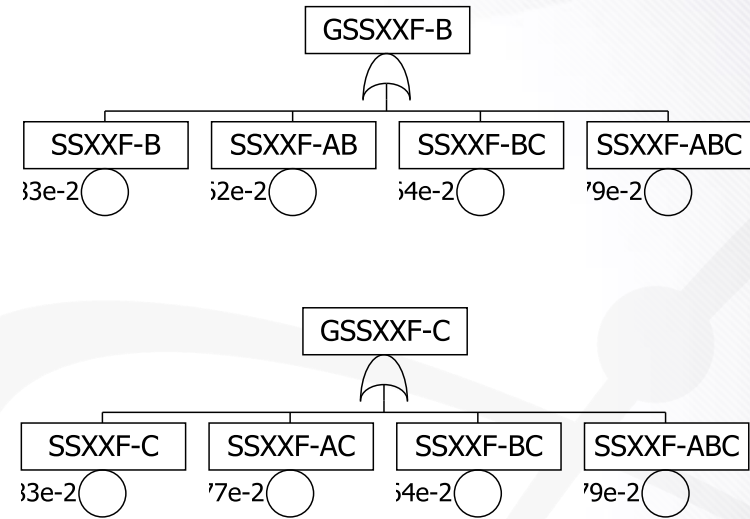
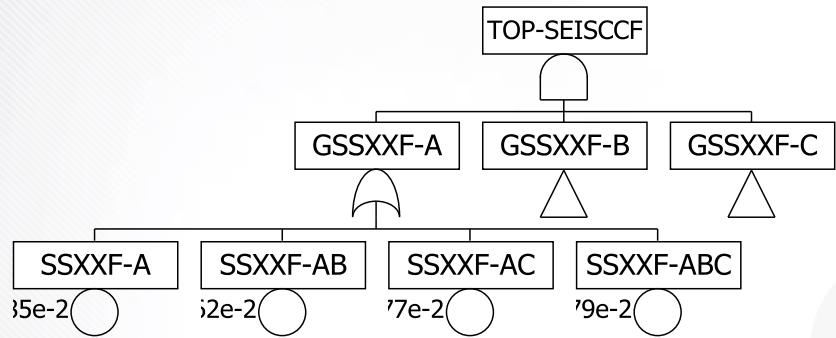
1 (1)	A	AB	AC	ABC			
2 (1)	B	AB	BC	ABC			
3 (1)	C	AC	BC	ABC			
4 (2)	A	B	AB	AC	BC	ABC	
5 (2)	A	C	AB	AC	BC	ABC	
6 (2)	B	C	AB	AC	BC	ABC	
7 (3)	A	B	C	AB	AC	BC	ABC

Solving - Non-Symmetry ---
0.015 sec for CCF Calculation

Non-Symmetry CCF Calculation Done

CCF-Style Model

■ CCF-Style Model



■ 정량화 결과 비교

Case	Monte Carlo	CCF-Style → BDD
A * B * C	0.01944	0.01944
A + B + C	0.2445	0.2445

- 동일한 정량화 결과 ← 같은 값을 가지도록 CCF Model 을 생성

CCF 값 계산 방법

Zk	Ce (CCF Event 들)						
A	A	AB	AC	ABC			
B	B	AB	BC	ABC			
C	C	AC	BC	ABC			
A + B	A	B	AB	AC	BC	ABC	
A + C	A	C	AB	AC	BC	ABC	
B + C	B	C	AB	AC	BC	ABC	
A + B + C	A	B	C	AB	AC	BC	ABC

Component 별 CCF Model

- $X_i = C_i + \sum_{j=1, j \neq i}^m C_{ij} + \sum_{j=1, j \neq i}^m \sum_{k=j+1, k \neq i}^m C_{ijk} + \dots$
 - 예) $X_A = C_A + C_{AB} + C_{AC} + C_{ABC}$
 - C_e : CCF Event 들 (CCF Event의 수 = $2^m - 1$)

기기들의 OR 조합에 대한 모델

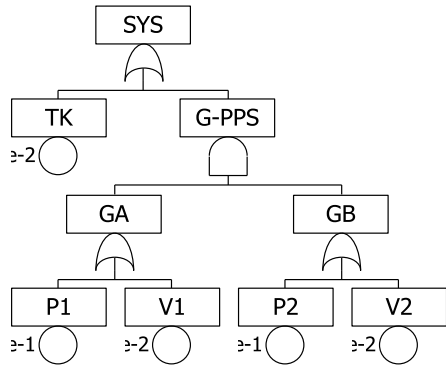
- $Z_i = X_i, Z_{ij} = X_i + X_j, Z_{ijk} = X_i + X_j + X_k, \dots$ ($2^m - 1$ 조합)
 - 예) $Z_{A+B} = C_A + C_B + C_{AB} + C_{AC} + C_{BC} + C_{ABC}$
- $Z_k = \sum_{C_e \in Z_k} C_e$: Z_k 에 속한 모든 CCF Event 들의 합
- $P(Z_k) = 1 - \prod_{C_e \in Z_k} (1 - P(C_e))$: 확률 계산 식 (independent Event 들)
 - $P(Z_k)$: Correlated Monte Carlo 방법으로 계산된 값

Negate 확률 + Log 변환 → 다항 1차식

- $1 - P(Z_k) = \prod_{C_e \in Z_k} (1 - P(C_e))$: Negate 확률로 변환
- $\log(1 - P(Z_k)) = \sum_{C_e \in Z_k} \log(1 - P(C_e)) = \sum_{C_e \in Z_k} R_e$: 다항 1차식
 - $R_e = \log(1 - P(C_e))$

4. PSA 적용 예제 (1)

Input Model/Data



#PGA
0.5

#Fragility

TK	2	0.3	0.3	S-TK
P1	1	0.3	0.3	
P2	1	0.3	0.3	
V1	1.5	0.3	0.3	
V2	1.5	0.3	0.3	

#Group Pumps
P1 P2

#Matrix.Br

1	
0.3	1

#Matrix.Bu

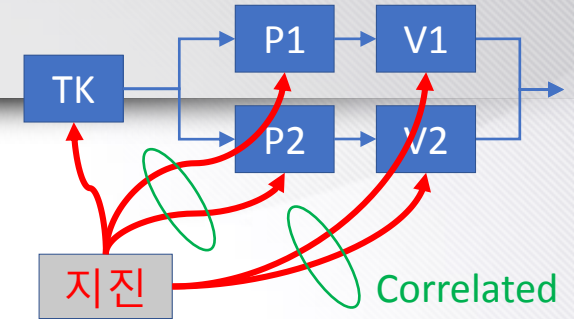
1	
0.7	1

#Group Valves
V1 V2

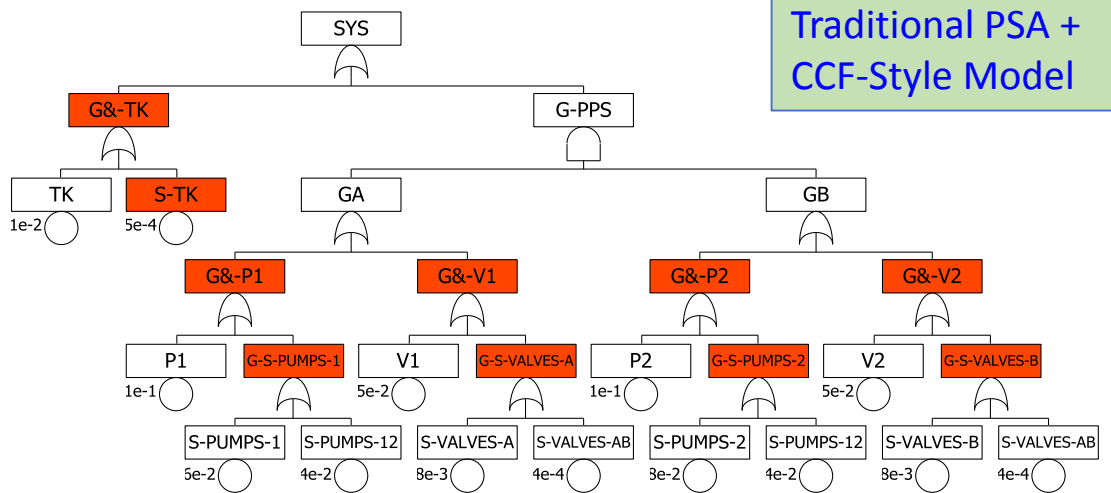
#Coeff.All 0.5

Monte Carlo Approach
($n=1e8$, FTeMC)
→ $5.466e-2$

Traditional PSA + CCF-
Style Approach
(SPSA.Supp.Calc + BDD)
→ $5.469e-2$ (0.05% 차이)



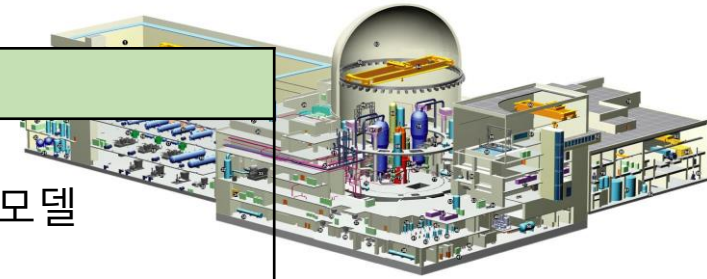
→ 여러 Seismic Group 과 Non-Seismic 으로 구성된 경우에도, 두 방법이 같은 결과를 산출함



PSA 적용 예제 (2)

■ Pilot Seismic PSA Model

Model	Description
Internal PSA Model	Pilot Plant PSA Model 원전 주요 계통 및 기기 포함한 단순화 모델 160 여 개의 Basic Event
Seismic Initiating Event Tree	7개 IE 고려 (R/B Failure, LLOCA, SLOCA, Loss of Control, LOUHS, LOOP, GTRN)
Seismic Correlation	$\rho = 0.5$ (주요 Pump, EDG/AAC, SDS V/V, CST) Fragility 는 기기별로 임의의 값을 가정
Calculation	PGA = 0.6 에 대한 CCDP

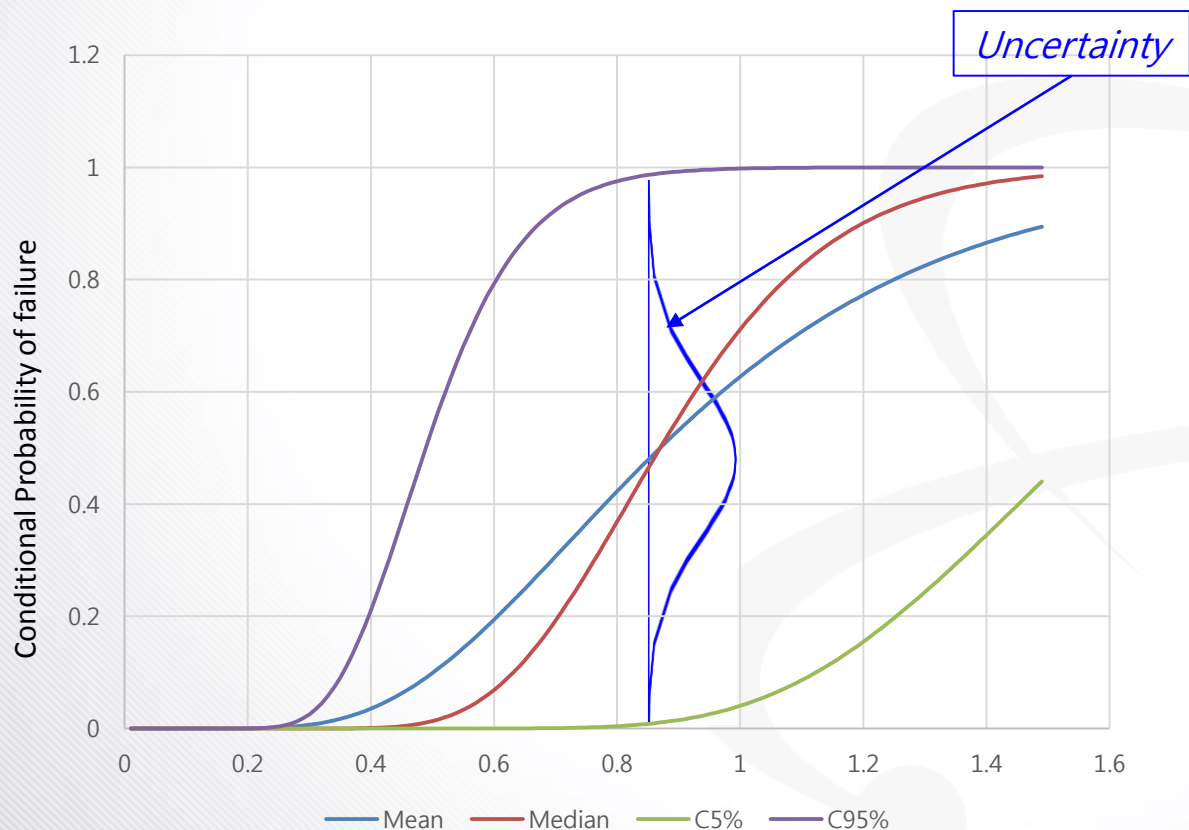


방법	정량화 결과	비고
Monte Carlo (FTeMC)	3.1043e-2	N=1e8 (샘플 수)
CCF-Style Model (FTREX/BDD)	3.1086e-2 (0.14% 차이)	N=1e8 (CCF Event 계산 샘플 수) REA=3.321e-2

→ Pilot Plant Seismic PSA 모델에서도 두 방법이 같은 결과를 산출함

5. PGA Level + Uncertainty 평가 방법

- 지진 리스크 평가 = 주어진 System에 대한 Fragility Curve 평가
 - PGA level 에 따른 파손확률
 - 파손확률의 Mean + 불확실성 (Median, 5%, 95%) 평가



$$f' = \Phi\left(\frac{\ln\left(\frac{a}{A_m}\right) + \beta_U \Phi^{-1}(Q)}{\beta_R}\right)$$

$$A = A_m' e_U$$

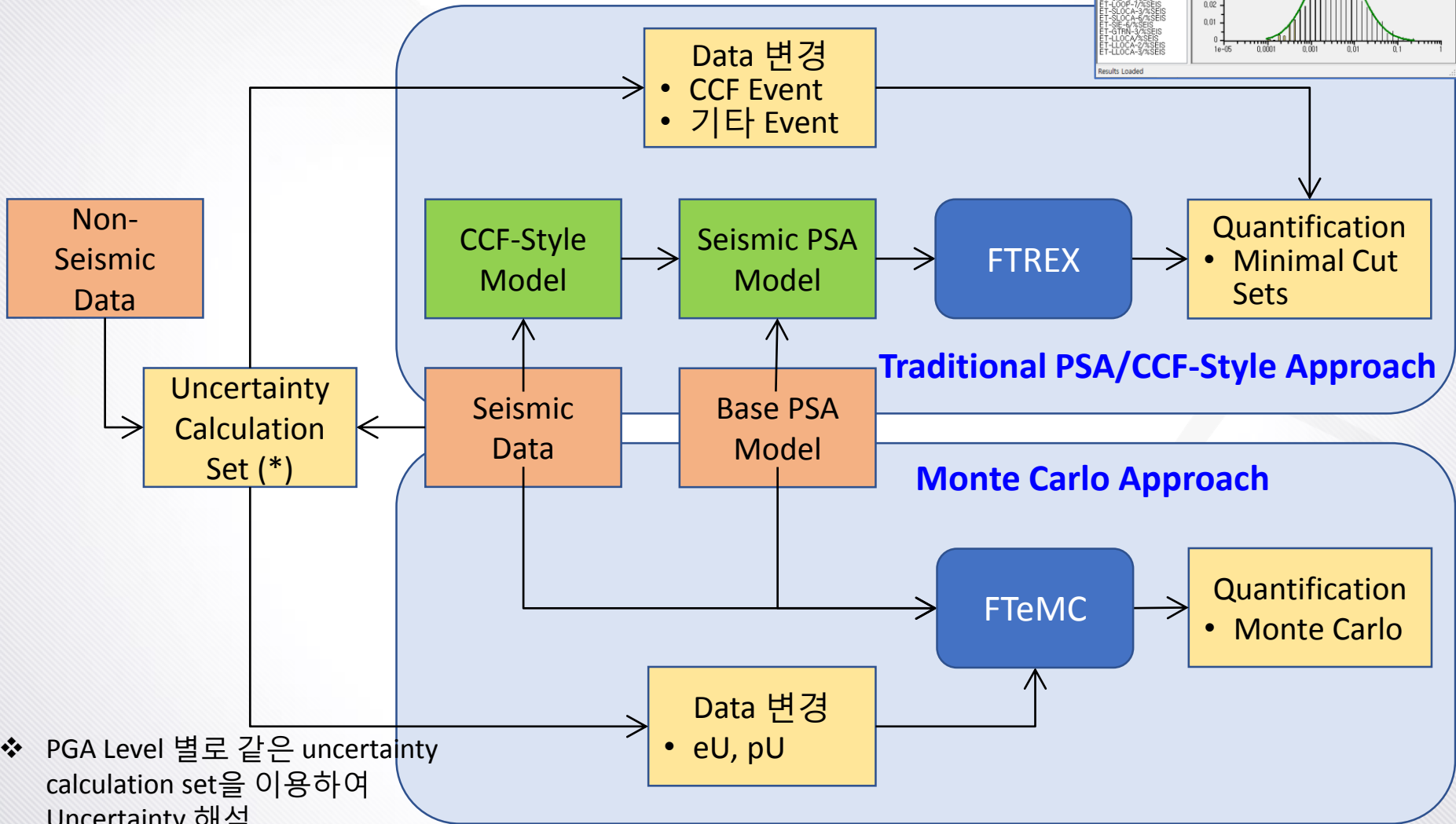
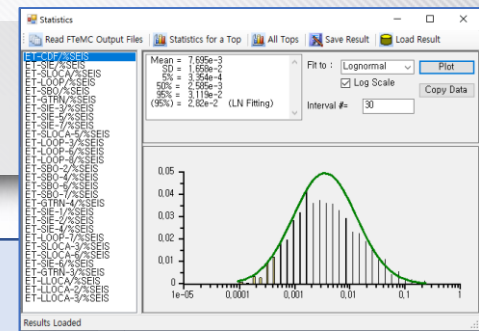
$$A = A_m' \exp(\beta_U * k_q)$$

- k_q : 확률 q에 해당하는 inverse normal 값 : $\Phi^{-1}(Q)$

평가 절차

- 각 PGA level 에 대해
- A_m, B_r 을 이용하여 파손확률 평가
- B_u 를 이용하여 Sampling \rightarrow 위의 과정을 반복 \rightarrow 5%, 95%, Median, Mean 계산

Uncertainty 평가 방법



- ❖ PGA Level 별로 같은 uncertainty calculation set을 이용하여 Uncertainty 해석
- ❖ 그렇지 않은 경우, PGA Level 값이 역전되는 현상 발생 가능

6. 추후 연구 항목

■ Seismic PSA 정량화 S/W 개발 중

- 방법론 개발
- 주요 모듈 개발
- 시험
- 기능 요건 작성

■ Seismic 분야에서 필요한 Feature 필요 (PRASSE의 기능들)

■ 미해결 사항들

- 다양한 Fragility, Correlation 입력 방식의 처리
 - Am, Br, Bu / Correlation Coefficient Matrix 로 변환
- LHS Sampling 적용 검토
- CCF 변환 Tool 보완
 - 경우에 따라 음수로 나타나는 CCF Event 값 처리 (Monte Carlo 결과)
 - CCF Model 단순화 및 부분적인 Symmetry 처리 방법
 - Uncertainty 분석시 Group 내에서 Symmetry 가 크게 깨지는 현상 검토
- Cholesky Matrix 의 입력 오류 처리
 - $M M^T = \Sigma$ (M = $\Sigma^{1/2}$: Cholesky Matrix, Σ : Coefficient Matrix)



THANK YOU