

# Probabilistic Model of PWSCC in Alloy 690 Steam Generator Tubing

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## Background

- ◆ Primary water stress corrosion cracking (PWSCC) has been a threat for the safety of nuclear power plants (NPPs).
- ◆ PWSCC in Alloy 600 components

Some earliest Reported Occurrences of Alloy 600 PWSCC for Various PWR Component Items [1]

Component Item	Date PWSCC Initially Observed	Service Life (Calendar Years)
Steam Generator Hot Leg Tubes	1971	2
Steam Generator Cold Leg Tubes	1986	18
Pressurizer Heaters and Sleeves	1987	5
Steam Generator Channel Head Drain pipes	1988	1

And many others

[1] Materials Reliability Program (MRP), Resistance to Primary Water Stress Corrosion Cracking of Alloys 690, 52, and 152 in Pressurized Water Reactors (MRP-111), EPRI, Palo Alto, CA, U.S. Department of Energy, Washington, DC: 2004. 1009801.

- ◆ Replace Alloy 600 with Alloy 690
  - Alloy 690 has been “immune” to PWSCC, but
- ◆ Predict PWSCC initiation time in Alloy 690 !!
  - How?
  - Deterministic or probabilistic modeling?

Mr. Deterministic : “PWSCC will definitely initiate after 2 years, no sooner or later than that”

Mrs. Probabilistic : “See the table..”

## Method and Approach

- ◆ Base model: Weibull distribution

$$f(t) = \frac{\beta}{\eta} \left(\frac{t}{\eta}\right)^{\beta-1} \exp\left[-\left(\frac{t}{\eta}\right)^\beta\right] \quad F(t) = 1 - \exp\left[-\left(\frac{t}{\eta}\right)^\beta\right]$$

$\eta > 0$  is the scale parameter and  $\beta > 0$  is the shape parameter of the Weibull distribution

- ◆ Problem?

We have only *censored data* :

Testing time instead of time to PWSCC initiation is all we know about the “strong” Alloy 690 → zero-failure data.

- ◆ What can we do: Bayesian method

➤ Model parameters are treated as random variables with certain probabilistic dist.

➤ Formulation:

$$f(\theta|t) = \frac{g(t|\theta) h(\theta)}{\int g(t|\theta) h(\theta) \partial \theta}$$

➤ where  $f(\theta|t)$  is the posterior distribution of parameter  $\theta$ ,  $g(t|\theta)$  is the likelihood function of the observed data  $t$  given parameters  $\theta$ ,  $h(\theta)$  is the prior distribution of  $\theta$ .

➤ Likelihood:

$$g(t|\theta) = \prod_{i=1}^r f(t_i) \prod_{j=1}^{n-r} \{1 - F(t_j)\}$$

where  $r$  is number of failures,  $n$  is number of plants

➤ Prior distributions:

Alloy 600

$\eta \sim \text{gamma}(1/2, 0) \rightarrow$  Jeffrey prior

$\beta \sim \text{beta}(0, 0, 0, 5) \rightarrow$  Uniform prior

Alloy 690

$t_{1st} \sim \text{Normal}(18.91, 5)$

$\beta \sim$  posterior  $\beta$  of Alloy 600

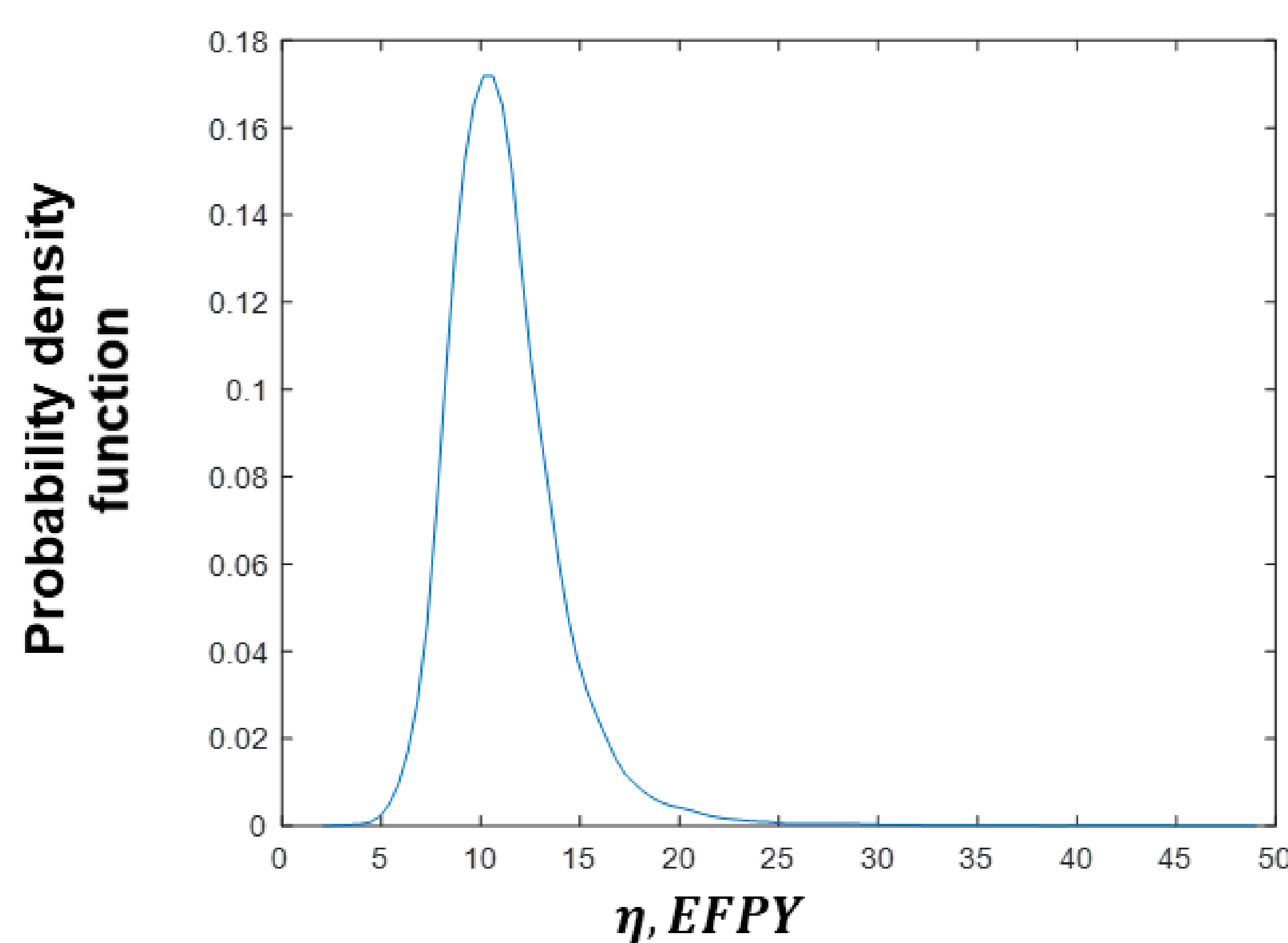
where  $t_{1st}$  is time to the earliest failure

## Numerical Simulations and Results

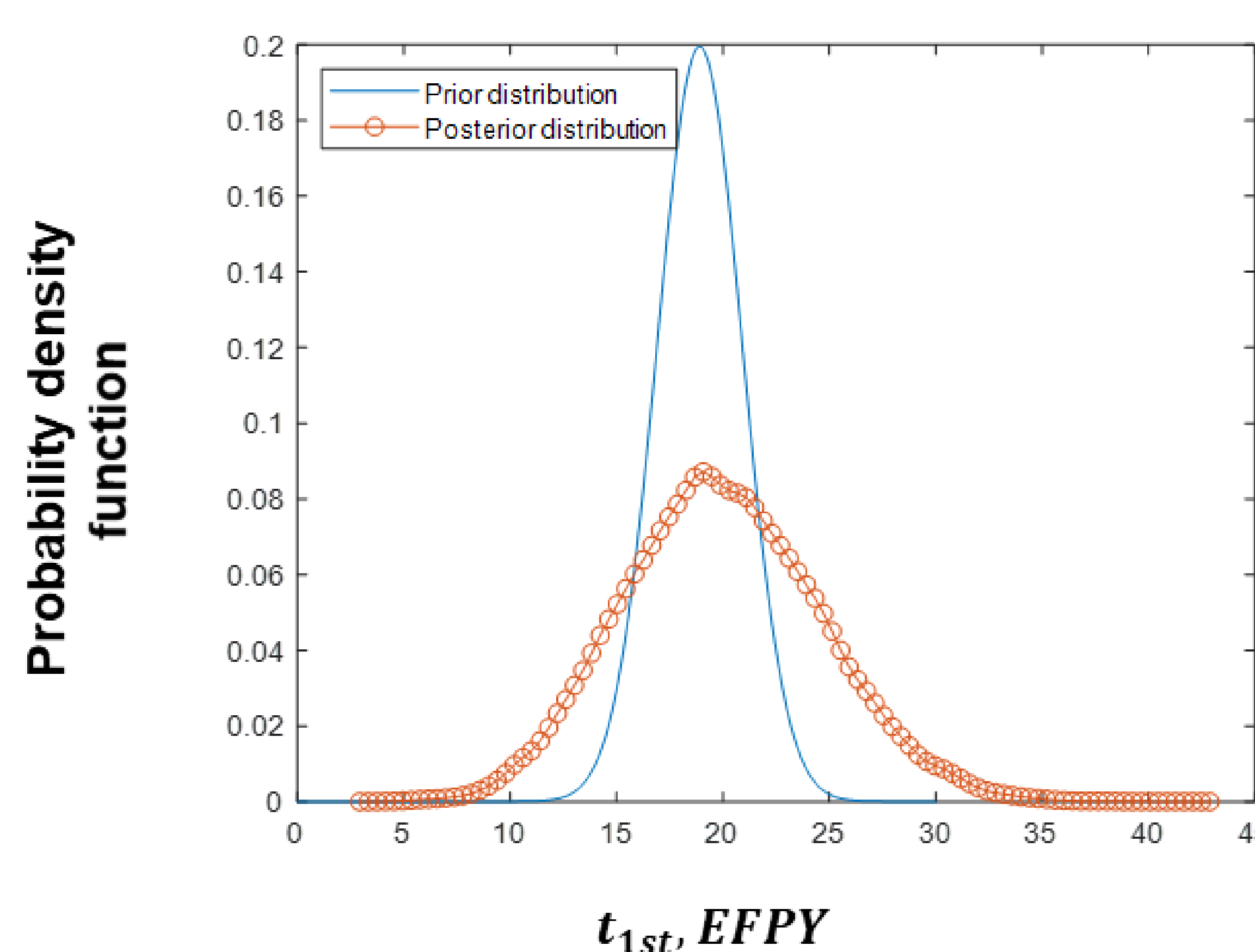
- ◆ Database on in-service experience of Alloy 600 MA and 690 TT steam generator tubing up to the year of 2008 summarized in [2]

- ◆ Results:

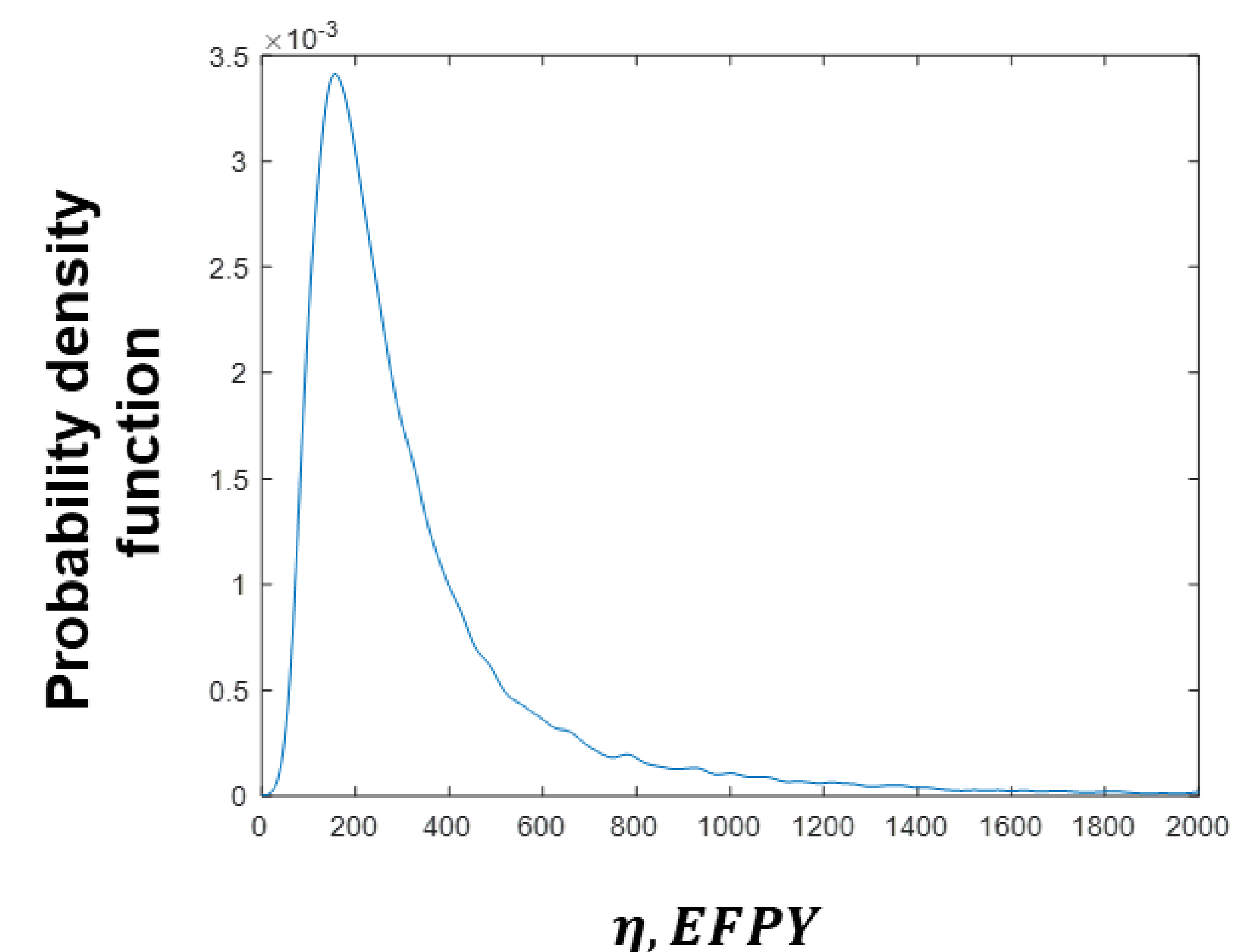
$\eta$  of Alloy 600



$t_{1st}$  of Alloy 690



$\eta$  of Alloy 690



[2] Steam Generator Management Program: Improvement Factors for Pressurized Water Reactor Steam Generator Tube Materials. EPRI, Palo Alto, CA: 2009. 1019044.

## Future works

- ◆ Using some different priors to see the sensitivity of the results to the choice of priors