

## Hydraulic and thermal behaviors of diabatic two-phase flow through porous particle beds

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### 1. Introduction

The behaviors of two-phase flow through porous particle beds have been studied for decades in various industrial and engineering fields. Particularly in a nuclear reactor under the severe accident condition, the two-phase flow phenomena through the particle bed can be a critical issue for reactor safety. Therefore, a basic understanding of the relevant hydrodynamics with two-phase flow accompanying phase-change process through the porous particle beds is essential to the reactor safety analysis. In this study, we conducted the experiments for saturated steam-water flow (boiling) in various particle beds. The experimental data of two-phase pressure drop and dryout heat flux (DHF) were analyzed with the numerical results from existing hydrodynamic models and previous correlations.

### 2. Methods

#### 2.1 Experimental

Fig. 1 illustrates the experimental design. The particle beds formed within the cylindrical test section made of STS304 pipe (ID: 110 mm, thick.: 15 mm, and L: 400 mm). The test section was installed inside a rectangular water pool (inner dimension: 360 × 360 × 660 mm<sup>3</sup>). Four visualization windows made of transparent polycarbonate (PC windows) were mounted to the sides of the water pool. For heating the particle beds, twelve cartridge heaters (OD: 9.42 mm, L: 450 mm, Power: 2.0 kW) were inserted from the bottom of the test section at the same spacing of 25 mm (see Fig. 1). The thermal power ( $P_t$ ) to the particle beds was controlled using two AC power controllers, and was measured using the AC voltage and current meters, i.e.,  $P_t = V_s I_s$  where  $V_s$  and  $I_s$  are the voltage and current values applied into the heaters. The heat flux ( $q_b$ ) with respect to the cross-sectional area of the particle bed is calculated as  $q_b = P_t/A_s$  where  $A_s$  is the cross-sectional area excluding the internal structures in the test section, such as the cartridge heaters and thermocouples. Note that the experimental setup has an inherent limitation to simulate the real phenomena where the individual porous particles generate heat. For local temperature measurements and DHF ( $q_d$ ) detection, a total of thirty K-type thermocouples were inserted into the test section in both the axial and radial directions (see Fig. 1).  $q_d$  is defined as the heat flux at which the local overheating within the particle beds occurs. The boiling experiments were conducted under a saturated condition (saturation temperature:  $T_{sat} = 100$  °C) at the atmospheric pressure, and tap water was used as the working fluid. The two-phase pressure through the particle bed and the absolute

pressure at the bottom of the bed were measured using the pressure tabs at the top and bottom of the test section and the absolute and differential pressure transmitters. Table I and II list the operating and design conditions of the experiments, and test cases and specifications of the particle beds, respectively.

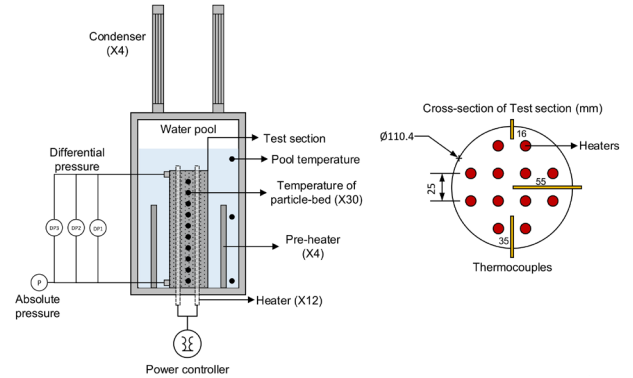


Fig. 1. Schematic of diagram of the experimental facility.

Table I: Operating and design conditions of saturated boiling experiments.

Fluid condition	Electric power (kW)	Vapor superficial velocity (m/s)	Heat flux (MW/m <sup>2</sup> )
Saturated at 1 atm	Operating: 0-17	Operating: 0-1.5	Operating: 0-2.0
	Design: 0-24	Design: 0-2.15	Design: 0-2.87

Table II: Experimental cases and specifications of the particle beds.

Case	Particle diameter, $D_p$ (mm)	Porosity ( $\epsilon$ )
BO-DP1	1	0.409
BO-DP3	3	0.409
BO-DP5	5	0.427
BO-DP6	6	0.428
BO-TROI	TROI distribution [1]	0.355

#### 2.2 Models and numerical methods for analyzing the experimental data

To analyze the model predictions for the two-phase pressure loss and DHF behaviors under the boiling condition, we solved numerically the steady-state one-dimensional momentum equations shown in Eqs. (1)-(3).

$$-\frac{dP_g}{dz} = \rho_g g + \frac{\mu_g}{KK_{rg}} J_g + \frac{\rho_g}{\eta\eta_{rg}} J_g |J_g| + \frac{F_l}{\alpha}, \quad (1)$$

$$-\frac{dP_l}{dz} = \rho_l g + \frac{\mu_l}{KK_{rl}} J_l + \frac{\rho_l}{\eta\eta_{rl}} J_l |J_l| - \frac{F_l}{1-\alpha}, \quad (2)$$

$$\frac{dP_g}{dz} = \frac{dP_l}{dz}, \quad (3)$$

where  $P$ ,  $z$ ,  $\rho$ ,  $g$ ,  $\mu$ ,  $K$ ,  $\eta$ ,  $J$ ,  $K_r$ ,  $\eta_r$ ,  $F_i$ ,  $\alpha$ , subscripts  $g$  and  $l$  are the fluid pressure, one-dimensional coordinate in upward direction, fluid density, gravity acceleration, dynamic viscosity, permeability, passability, fluid superficial velocity, relative permeability, relative passability, interfacial drag force (unit:  $N/m^3$ ), void fraction, vapor and liquid, respectively. In addition to Eqs. (1)-(3), the continuity equation based on the mass and energy balance due to the phase-change was used, i.e.,  $\rho_g J_g + \rho_l J_l = 0$ . In the previous studies [2-10], different types of the relations for  $K_r$ ,  $\eta_r$ , and  $F_i$  were applied into Eqs. (1) and (2) depending on the relevant flow regime. In this study, we adopted three types of the models for the two-phase pressure loss through the porous particle beds, i.e., Schulenberg and Müller model [3] (SM model), Tung and Dhir model [4] (TD model), and Schmidt model [2] (SC model). We developed the in-house codes written in MATLAB R2020a for solving the pressure balance equation from Eq. (3) based on the SM, TD, and SC models. Additionally, we compared the DHF data in the experimental cases with the previous correlations for counter-current flooding limit (CCFL) proposed by Wallis [11] and Schrock et al. [12].

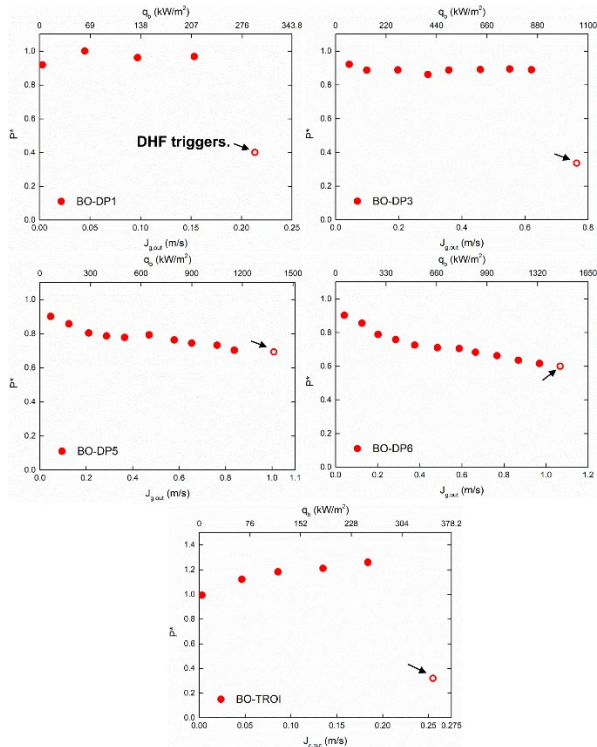


Fig. 2. Non-dimensional pressure gradients and DHFs in the boiling experiments ( $J_{g,out} : J_g$  at the outlet).

### 3. Results and discussion

As shown in the Table II, we conducted the saturated boiling experiments for the four types of uniform particle

beds and non-uniform particle bed with the TROI distribution [1]. Fig. 2 shows the behaviors of non-dimensional pressure gradient ( $P^*$ , Eq. (4)) in the boiling experiments.

$$P^* = \frac{-dP/dz}{(\rho_l - \rho_g)g}. \quad (4)$$

The hollow circles in the plots presented in Fig. 2 indicate the conditions at which the DHF ( $q_d$ ) phenomenon was triggered. The values of  $q_d$  increases with  $D_p$ . In the cases of BO-DP1 and BO-DP3, the sudden drop of  $P^*$  was observed, and it indicates the local flow regime transition from two-phase to single-phase vapor flow within the pores. For the cases of larger particles (BO-DP5 and BO-DP6), the transition might be milder than the former cases. Fig. 3 shows the transient variations of the local fluid temperatures (using 30 thermocouples) in the particle beds at  $q_d$ . In the particle bed under normal boiling condition, the local fluid temperatures were maintained near the saturation temperature (100 °C). However, they exhibit a significant temporal increase under the dryout heat flux conditions. In BO-DP5 case, a maximum rate of local temperature increase was recorded to 0.9 °C/s. As shown in the temperature contours (see the insets of Fig. 3), the dryout triggers at the local position in the particle beds, and it expands temporally. Interestingly, the local dryout was detected simultaneously at several local positions in the BO-TROI case. The DHF triggering position rises up as the particle diameter increases for the uniform particle beds.

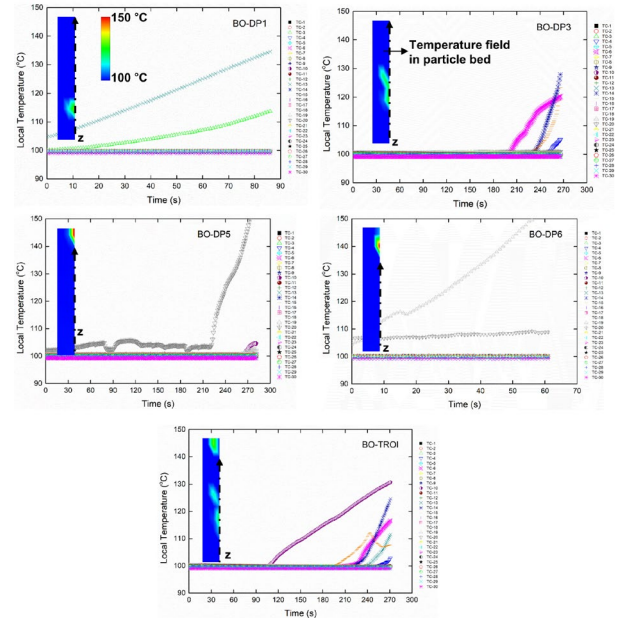


Fig. 3. Temporal variations of local fluid temperatures in the particle beds under DHF conditions.

We analyzed the model predictions for the two-phase pressure loss and DHF behaviors using the numerical codes based on SM, TD, and SC models. For considering

the spatial variations of  $J_g$ ,  $\alpha$  and flow regime through the particle beds under the phase-change condition, the calculation domain (particle beds) was divided into the 40 grid points (grid spacing: 10 mm) as shown in Fig. 4. In this figure, the experimental  $P^*$  data were compared with the predictions from SM, TD, and SC models. The predicted  $P^*$  data obtained by spatially averaging the  $P^*$  values at the grid points. For the uniform particle beds with relatively small  $D_p$  (BO-DP1 and BO-DP3 cases), the SC model shows very good agreements with the experimental  $P^*$  and  $q_d$  data.  $q_d$  values predicted by the models are marked with the  $\times$  symbols in the plots. For the larger  $D_p$  cases (BO-DP5 and BO-DP6), the models slightly underestimate the  $P^*$  from the experiments, and show qualitative agreements with the variation trends of experimental  $P^*$ . Overall, the TD model underestimates the experimental  $q_d$ . In the plot for the BO-TROI case, an unusual trend of the experimental  $P^*$  is shown. Theoretically, the one-dimensional steady-state and stable two-phase flow within the particle beds cannot be maintained under the condition  $P^* > 1$ . For the results, we guess that the multi-dimensional flow path may have formed within the particle bed due to the random packing of the particles with broadly distributed  $D_p$ .

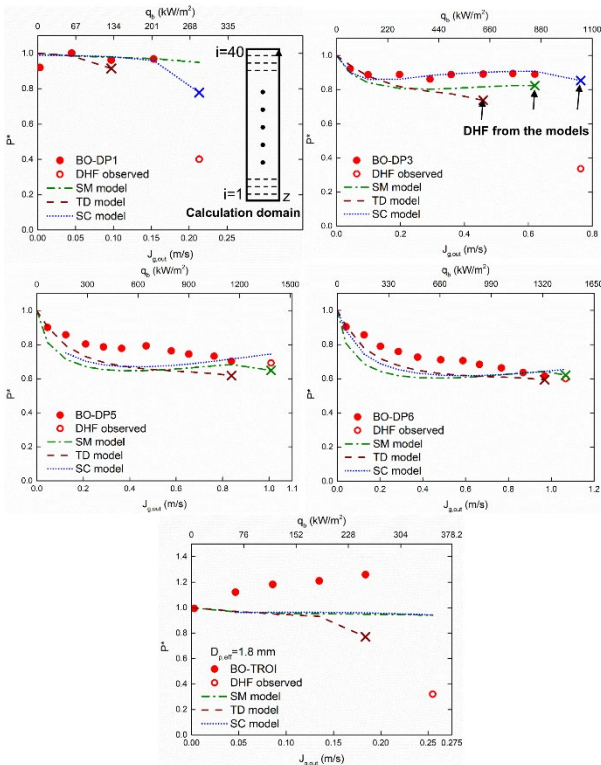


Fig. 4. Experimental and model prediction results for the non-dimensional pressure gradients and DHFs in the boiling experiments.

Fig. 5 shows the DHF prediction results of existing models with the present experimental data. For the SM, TD, and SC models, the DHF was defined as the heat flux at which the CCFL occurs at the top of the particle bed.

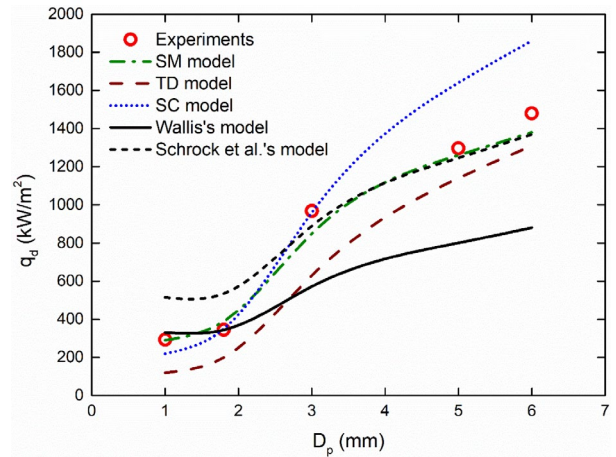


Fig. 5. Comparison of experimental DHFs and predictions from the previous models.

The SM model shows the best estimations to the experimental  $q_d$  data with the variation of  $D_p$ , while the SC model shows good agreements with the experiments for the cases of  $D_p$  smaller than 3 mm and overestimates the values of  $q_d$  for the large  $D_p$  ( $=5$  and  $6$  mm) cases. The TD model underestimates overall the experimental data. The DHF values for the fine particle beds ( $D_p < 3$  mm) agreed well with the Wallis model [11] in which only gas and liquid drag forces were considered into the model relation. The classical simplified models for the CCFL prediction from Wallis [11] (for the cases of  $D_p \geq 3$  mm) and Schrock et al. [12] show the large deviations from the experimental data in both qualitative and quantitative manners. In the classical models, the CCFL phenomenon was simplified with the relationship between the gas and liquid inertial drag forces and the gravity force, i.e., the viscous and interfacial drag forces were not considered properly in the model.

#### 4. Conclusions

The results of this study can be summarized as below:

- In the saturated boiling experiments through various particle beds, the two-phase pressure gradient through the beds continuously decreased with  $J_g$  before the occurrence of DHF phenomenon.
- With the onset of DHF, rapid increments of the local fluid temperatures in the particle beds were observed (maximum rate of local temperature increase:  $0.9$  °C/s). The existing models showed reasonably good agreements with the experimental pressure loss data, and the SM model predicted the DHF results best.

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