# Computation of Pressure Drop in Cross-flow through an In-line Tube Bundle 

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## 1. Introduction

Over the past decades, flow in tube bundles has received much attention from researchers because of its practical importance in the design of heat exchanger, steam generators, evaporators, etc. In particular, pressure drop performance of rod bundles has been of great interest to the design of nuclear reactors, so numerous studies have been made to understand the underlying physics of such flows [1,2] and to develop correlations for the pressure drop [3,4]. This paper numerically investigates the turbulent cross-flow over an in-line tube bundle, with an emphasis on the effects of longitudinal pitch-to-diameter ratio and Reynolds number.

## 2. Methods and Results

### 2.1 Computational Setup

Under an assumption that the flow of constantproperty Newtonian fluid is steady, incompressible, isothermal and turbulent, the following ReynoldsAveraged Navier-Stokes (RANS) equations are solved using a commercial CFD code, Fluent 12.0 [5].

$$
\begin{align*}
& \frac{\partial\left\langle u_{i}\right\rangle}{\partial x_{i}}=0  \tag{1}\\
& \rho \frac{\partial\left\langle u_{i}\right\rangle\left\langle u_{j}\right\rangle}{\partial x_{j}}=-\frac{\partial\langle p\rangle}{\partial x_{i}}+\frac{\partial}{\partial x_{j}}\left[\mu\left(\frac{\partial\left\langle u_{i}\right\rangle}{\partial x_{j}}+\frac{\partial\left\langle u_{j}\right\rangle}{\partial x_{i}}\right)-\rho\left\langle u_{i}^{\prime} u_{j}^{\prime}\right\rangle\right] \tag{2}
\end{align*}
$$

The computations are performed using a segregated solver, SIMPLE algorithm for pressure-velocity coupling, and second order upwind method for discretization. For the Reynolds stresses in Eq. (2), the realizable $k-\varepsilon$ turbulence model is used with enhanced wall treatment.

Table 1. Summary of grid dependency test

| Case | Number of <br> grid | Pressure loss <br> coefficient <br> $\left(\zeta=2 \Delta P / \rho U_{b}^{2}\right)$ | Deviation <br> w.r.t case <br> M4 (\%) |
| :---: | :---: | :---: | :---: |
| M1 | 409,600 | 12.876 | 3.44 |
| M2 | $1,446,000$ | 12.488 | 0.32 |
| M3 | $3,837,200$ | 12.452 | 0.03 |
| M4 | $6,280,400$ | 12.448 | - |

Figure 1 shows the computational domain, a subset of in-line tube bundles tested here, and corresponding boundary conditions. The tube bundle consists of 40 rows of rods arranged with a transverse pitch-todiameter ratio of $S_{T} / d=1.32$. The tube diameter is $d=10$ mm and length is $L=300 \mathrm{~mm}$. The simulations are conducted for various longitudinal pitch-to-diameter ratios $\left(S_{L} / d=1.08,1.18,1.28,1.38\right.$, and 1.48 ) and Reynolds numbers ( $R e=3,185$ to 25,484 ) based on the tube diameter and bulk velocity $U_{b}$ through the gap between the tubes.

### 2.2 Grid sensitivity study

For the grid dependency test, 3D simulations are firstly conducted for the flow at $R e=25,484$ on several meshes with different levels of refinement. The computational grid is clustered at the wall, at which the maximum $y^{+}$value is kept less than unity. Table 1 summarizes the details of the four meshes M1, M2, M3 and M4, and the results of mesh convergence study. The difference of pressure drop between the coarse (M1) and very fine meshes (M4) is found to be less than $4 \%$. It is also observed that a further grid refinement beyond M2 has insignificant influence on the pressure drop. Therefore, M2 is chosen for the following computations.


Fig. 1. Schematic of computational domain and boundary condition


Fig. 2. Comparison of pressure drop for an in-line tube bundle at $S_{L} / d=1.18$

### 2.3 Comparison with empirical correlation

Figure 2 compares the pressure drop for an in-line tube bundle at $S_{L} / d=1.18$ as a function of Reynolds number. Overall, 3D simulation provides a favorably good agreement with the empirical correlations [3,4], except for some discrepancies at Reynolds numbers less than 10,000 . On the other hand, 2D simulation underestimates the pressure drop and it gives less accurate prediction than 3D, particularly at $R e>10,000$. This is believed to be mainly due to the lack of 3D effect, implying that 3D simulation might be essential for better prediction of the pressure drop at high Reynolds number. So, in the rest of paper, we have conducted 3D simulations only.

### 2.4 Effect of longitudinal pitch and Reynolds number

Figure 3 shows the impact of longitudinal pitch and Reynolds number on the pressure drop performance of


Fig. 3. Pressure loss coefficient $v s$. Reynolds number relationships for various longitudinal pitch-to-diameter ratios
in-line tube bundles at $R e=3,185$ to 25,484 and $S_{L} / d=1.08$ to 1.48 . It is observed that the larger the longitudinal pitch, the greater the pressure drop. This is because the interaction effect between the rods becomes weak by the increase in longitudinal pitch at a given Reynolds number. It is therefore conjectured that the interaction between the rods in the streamwise direction might be beneficial to the pressure drop performance of in-line tube bundles. It is also seen in Fig. 3 that the pressure loss coefficient is less likely to be affected by the change of Reynolds number at $R e=13,000 \sim 25,484$. These results are consistent with the previous observations of Zukauskas and Ulinskas [4], thus supporting the validity of the present computation.

## 3. Conclusions

In this paper, we numerically investigate the flow through an in-line tube bundle consisting of 40 rows of rods arranged with a transverse pitch-to-diameter ratio of $S_{T} / d=1.32$. The steady, incompressible and turbulent flow are predicted by the commercial CFD code, Fluent 12.0 with different mesh resolutions, longitudinal pitch-to-diameter ratios and Reynolds numbers. It is observed that at the relatively high Reynolds number, 3D simulation provides better prediction of the pressure drop than 2D. The computed result also shows that the larger the longitudinal pitch, the greater the pressure drop. This confirms that the pressure drop performance of an in-line tube bundle is strongly influenced by the tube arrangement, so more extensive investigation will be pursued in the future study.

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